

## Harmonic Oscillator Wavefunctions and Probability Densities

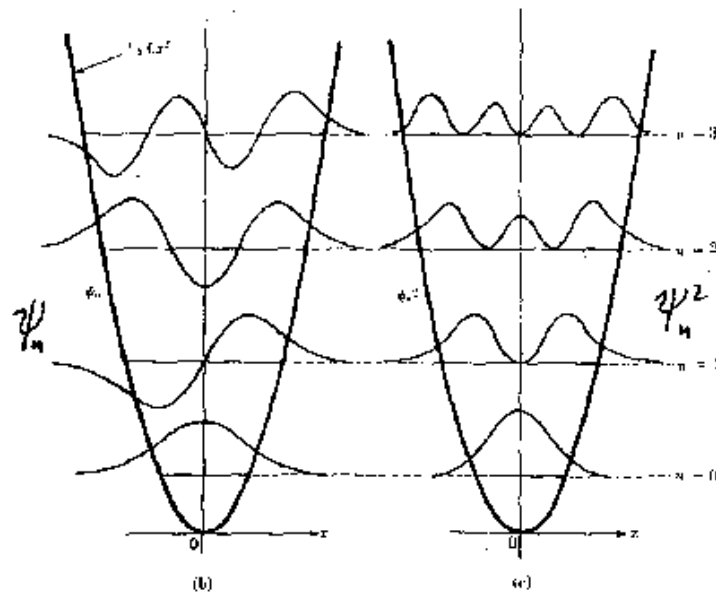


Fig. 2.20. Harmonic oscillator. (a) Ground-state wave function  $\psi_0$  and probability density  $\psi_0^2$ ; (b) potential-energy function  $\frac{1}{2}kx^2$ , wave functions  $\psi_n$ , and energy levels  $E_n$ ; (c) probability densities  $\psi_n^2$  and energy levels  $E_n$ .

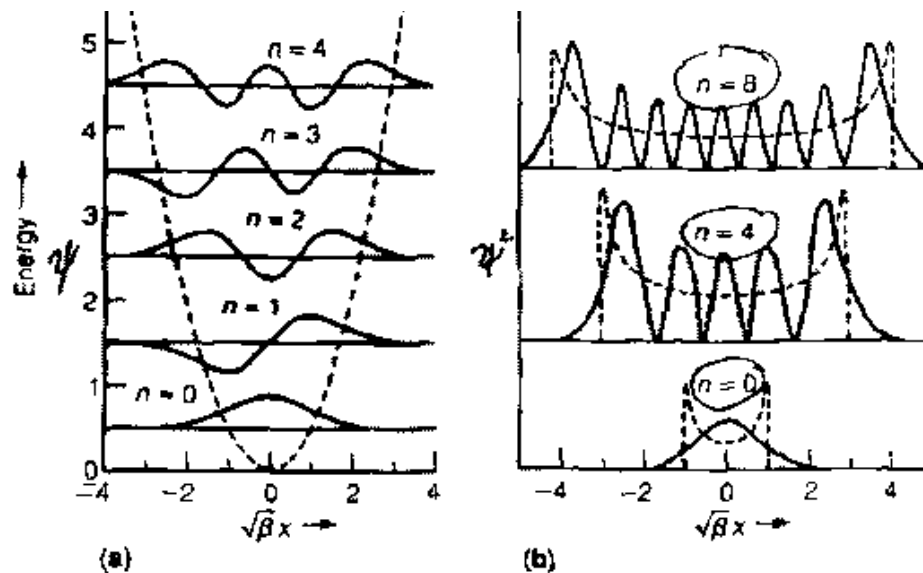
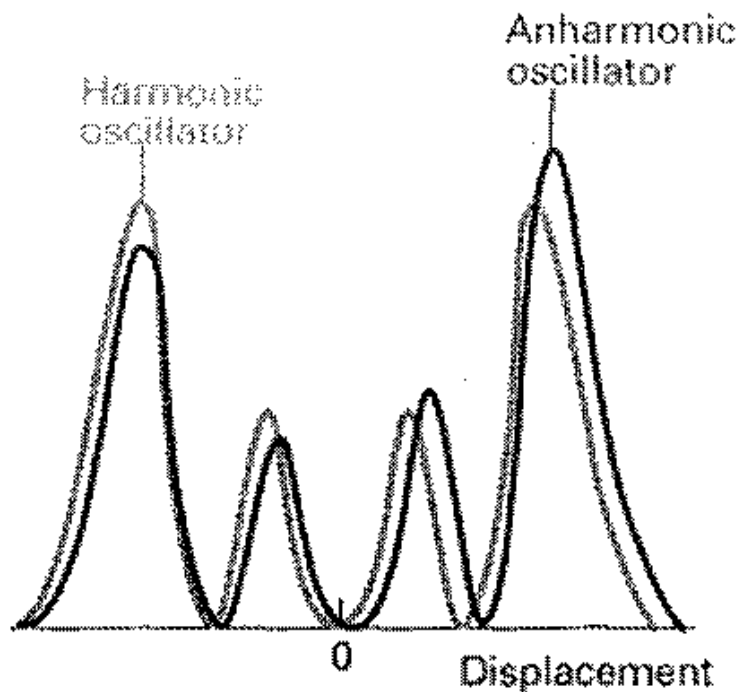


FIGURE 10-13

Wave functions for the harmonic oscillator. (a) The horizontal lines show the energy levels in units of  $h\nu$ . Superimposed on each line is the wave function for that level. The dashed line shows the potential-energy function. Note that the energy for level 0 is not zero. (b) Probability functions for levels  $n = 0, 4$ , and  $8$ . The solid lines show the quantum mechanical probability distributions,  $\psi_n^2$ . The dashed lines show the classical probability distributions computed from Equation 10-45, for the same energy  $E$ . (Reproduced from Kauzmann, 1957.)

Probability Distribution for Anharmonic Oscillator  
as Compared to Harmonic Oscillator



**16.36** The probability distribution ( $\psi^2$ ) of a slightly anharmonic oscillator compared with the probability distribution of a harmonic oscillator (in each case for  $v = 3$ ). The anharmonic oscillator (for a typical diatomic molecule) is more likely to be found at large extensions and less likely to be found significantly compressed than is a harmonic oscillator.

from: **Physical Chemistry, 5th Ed.**,  
by Peter Atkins, W.H. Freeman, N.Y.,  
pp. 572