

CHEMISTRY 163A REVIEW TOPICS

The Chemistry 163A final will be based on quantitative (e.g., homework problems) and a conceptual understanding of the following topics.

- I. Failures of Classical Mechanics and the Advent of Quantum Mechanics
 - A. The Stern-Gerlach, Davisson-Germer, Rydberg, and Compton experiments with emphasis on the conflict between the observations and the predictions of classical mechanics.
 - B. Wave-particle duality
 - C. The important relationships involving energy, the frequency of electromagnetic radiation, linear momentum, the wavelength of a particle, etc.
 - D. Correspondence principle

- II. Fundamentals of Quantum Theory
 - A. Bohr's treatment of hydrogen atom
 - B. Mathematical foundation
 - 1. Operators
 - 2. Commutation
 - 3. Separation of variables technique
 - C. Postulates of quantum mechanics
 - 1. Schrödinger time-dependent wave equation
 - 2. Probability density and physical interpretation of the wavefunction
 - 3. "Well-behaved" wavefunctions
 - 4. Expectation values
 - 5. Eigenvalues and measurement theory
 - 6. Derivation of time-independent Schrödinger equation
 - 7. Orthonormality of eigenfunctions
 - 8. Commutation, mutual eigenfunctions, and uncertainty principles
 - D. Particle-in-a-box
 - 1. Importance of boundary conditions in determining the allowed energy levels (i.e., quantization)
 - 2. Orthonormality and expectation values using explicit wavefunctions
 - 3. Three-dimensional particle-in-a-box
 - a. Extension of Schrödinger equation to three dimensions
 - b. Separation of variables
 - c. Degeneracy
 - d. Model for translational motion (relative energy level spacing)
 - E. Harmonic oscillator
 - 1. Separation of equations for center-of-mass and relative motion

2. Boundary conditions
 3. $E_n = (n + 1/2)h\nu_0$, $\nu_0 = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}}$
 4. Features of the harmonic oscillator wavefunctions
 - a. Symmetry
 - b. Shapes of low energy wavefunctions
 - c. Extension beyond the classical turning point and tunneling
 - d. Relation of the higher states to the Correspondence Principle
 5. Model for vibrational motion
 - a. What determines k , ν_0
 - b. Relative energy level spacing
- F. Rigid rotor
1. Model for rotational motion (relative energy level spacing)
 2. $Y_{J,M_J}(\theta, \phi)$
 3. $E_J = \frac{h^2}{8\pi^2 I} J(J+1)$
 4. Degeneracy of $2J + 1$ values of M_J for each J

III. Quantum Mechanics of One-Electron Atoms

- A. Integration in spherical coordinates
- B. Mathematical origin of the n , ℓ , m_ℓ and m_s numbers
- C. Physical interpretations of the n , ℓ , m_ℓ and m_s numbers
- D. $E_n = -\frac{1}{n^2} \frac{Z^2 e^2}{8\pi\epsilon_0 a_0} = \frac{-Z^2}{2n^2}$ in a.u.
 $\hat{L}^2 \psi_{n\ell m} = \ell(\ell+1)\hbar^2 \psi_{n\ell m}$ $\hat{L}_z \psi_{n\ell m} = m\hbar \psi_{n\ell m}$
- E. Relationship of n and ℓ to radial and angular nodes of hydrogen-like orbital
- F. Real and complex Φ functions
- G. Nodal properties and shapes of orbitals
- H. Pauli spin functions $\alpha(\sigma)$, $\beta(\sigma)$

IV. Many-Electron Atoms

- A. The $1/r_{12}$ term prevents exact solution
- B. Variation theorem
- C. Independent electron approximation
 1. Screening and effective nuclear charge
 2. $E = -Z_f^2 / 2n^2$
 3. How penetration determines Z_f for s vs. p orbitals

- D. Pauli exclusion principle; Slater determinants
 - E. Singlet and triplet 1s2s excited states of helium
 1. Hund's rule $E_{\text{singlet}} > E_{\text{triplet}}$
 2. Singlet and triplet spin wavefunctions and vector model of spin coupling
 - F. Aufbau principle and periodic table (atomic radii, I.P.'s, etc.)
- V. Bonding in Molecules
- A. Born-Oppenheimer approximation
 - B. Hydrogen molecules
 1. What makes H_2 more stable than two H atoms?
 2. Molecular orbital
 - a. Bonding-antibonding m.o.'s
 - b. Constructing many-electron wavefunctions from a configuration of m.o.'s
 - C. Homonuclear diatomics
 1. Molecular orbitals
 2. Classification and symmetry
 3. Rationale for energy ordering
 4. Configuration and molecular properties
 - a. Stability
 - b. Vibrational frequency
 - c. Bond distance
 - d. Paramagnetism
 - D. Heteronuclear diatomics
 1. Which a.o.'s interact
 2. Unequal a.o. contribution to m.o.'s
- VI. Spectroscopy
- A. Spectral regions and relevant to molecular-electronic spectra
 - B. Probability of a transition
 - C. *General* spectra of:
 1. Rotational spectroscopy
 2. Vibrational spectroscopy
 3. Rotation-vibration spectra
 4. Electronic spectra
 5. Electronic-vibration spectra
 6. Raman spectroscopy
 - D. Spectroscopic vocabulary
 1. Non-radiative transition (radiationless decay)
 2. Fluorescence
 3. Phosphorescence
 4. Chemiluminescence