Chemistry 163B

Lecture 4 Winter 2013

Challenged Penmanship

Notes

2

1st Law recapitulation

 $U \equiv internal energy$

 $dU_{sys} = dq_{sys} + dw_{sys} + dn_{sys}$ (n=number of moles; dn=0 for closed system)

 $dU_{sys} = -dU_{surr}$ (energy conserved)

dU is exact differential

U is a state function

completely general

for only P-V work and closed system (dn=0)

$$dU = d\bar{q} - P_{ext}dV$$

- Constant volume process $dU_V = dq_V \Delta U_V = q_V$
- Adiabatic process $dU = \frac{dw}{dt} \Delta U = w$

enthalpy: q for process at constant Pressure

H≡U+P_{int}V (definition of enthalpy, H)

since U is state function and P, V are state variables, H is also a

STATE FUNCTION

completely general

why a new state function you might ask??

 $dU_V = dq_V$; $\Delta U_V = q_V$ heat at constant volume

but most reactions and many physical processes are carried out at constant P

desire state function for q_p , heat at constant pressure

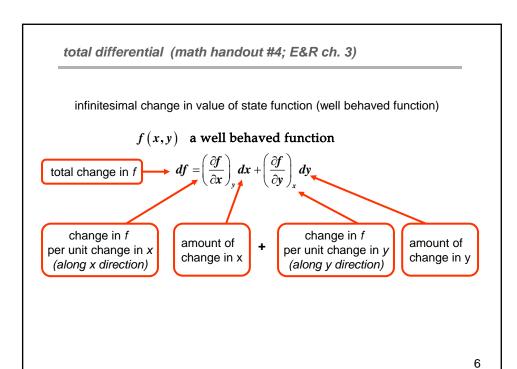
4

enthaply: H, a state function for heat transfer at constant pressure

$$H \equiv U + P_{\text{int}}V$$
 $dH = dU + PdV + VdP$
 $dH = d\bar{q} - PdV + d\bar{w}_{other} + PdV + VdP$
 $dH = d\bar{q} + VdP + d\bar{w}_{other}$
and at P=constant and $d\bar{w}_{other} = 0$
 $dH_P = d\bar{q}_P$
 $\Delta H_P = q_P$ as advertised!!

 $\Delta H_P = q_P$ at const P no w_{other} $\Delta H_P > 0$ endothermic (heat gained by system)

 $\Delta H_P < 0$ exothermic (heat lost by system)



manipulating thermodynamic functions: fun and games

for example: HW#2

12. Derive the following for any closed system, with only P-V work:

$$C_{V} = -\left(\frac{\partial U}{\partial V}\right)_{T} \left(\frac{\partial V}{\partial T}\right)_{U}$$

total differential for U(T,V,n) and H(T,P,n)

$$U(T,V,n_1,n_2,...,n_N)$$

$$dU = \left(\frac{\partial U}{\partial T}\right)_{V,n} dT + \left(\frac{\partial U}{\partial V}\right)_{T,n} dV + \sum_{i=1}^{N} \left(\frac{\partial U}{\partial n_i}\right)_{T,V,n_i \neq n_i} dn_i$$

$$H(T,P,n_1,n_2,...,n_N)$$

$$dH = \left(\frac{\partial H}{\partial T}\right)_{P,n} dT + \left(\frac{\partial H}{\partial P}\right)_{T,n} dP + \sum_{i=1}^{N} \left(\frac{\partial H}{\partial n_i}\right)_{T,P,n_i \neq n_i} dn_i$$

for now closed system all dn_i=0

8

H(T,P): some manipulations and relationships (closed system)

$$dH = dq + VdP$$
 closed system, $dw_{other} = 0$

'divide by dT, holding P constant'

$$\left(\frac{\partial H}{\partial T}\right)_{p} = \left(\frac{dq}{dT}\right)_{p} + V\left(\frac{\partial P}{\partial T}\right)_{p}$$

$$\left(\frac{\partial H}{\partial T}\right)_{p} = \left(\frac{dq}{dT}\right)_{p} = n\bar{C_{p}}$$

'divide by dP, holding T constant'

$$\left(\frac{\partial H}{\partial P} \right)_{T} = \left(\frac{dq}{dP} \right)_{T} + V \left(\frac{\partial P}{\partial P} \right)_{T}$$

$$\left(\frac{\partial H}{\partial P} \right)_{T} = \left(\frac{dq}{dP} \right)_{T} + V$$

$$dH = \left(\frac{\partial H}{\partial T}\right)_{P} dT + \left(\frac{\partial H}{\partial P}\right)_{T} dP$$

$$dH = n\overline{C}_{P} dT + \left(\frac{\partial H}{\partial P}\right)_{T} dP \quad \text{eqns. 3.30-3.32 E&R (p. 56 [52]_{2nd})}$$

U(T,V): some manipulations and relationships (closed system)

$$dU = dq - PdV$$
 closed system, $dw_{other} = 0$

'divide by dT, holding V constant'

$$\left(\frac{\partial U}{\partial T}\right)_{V} = \left(\frac{dq}{dT}\right)_{V} - P\left(\frac{\partial V}{\partial T}\right)_{V}$$

$$\left(\frac{\partial U}{\partial T}\right)_{V} = \left(\frac{dq}{dT}\right)_{V} = n\bar{C_{V}}$$

'divide by dV, holding T constant'

$$\left(\frac{\partial U}{\partial V} \right)_{T} = \left(\frac{dq}{dV} \right)_{T} - P \left(\frac{\partial V}{\partial V} \right)_{T}$$

$$\left(\frac{\partial U}{\partial V} \right)_{T} = \left(\frac{dq}{dV} \right)_{T} - P$$

$$dU = \left(\frac{\partial U}{\partial T}\right)_{V} dT + \left(\frac{\partial U}{\partial V}\right)_{T} dV$$

$$dU = n\overline{C}_{V} dT + \left(\frac{\partial U}{\partial V}\right)_{T} dV \qquad \text{eqn. 3.12-3.15 E&R (p 50 [46]_{2nd})}$$

10

save for later when we have tools from 2nd Law of Thermodynamics

$$dU = n\overline{C}_V dT + \left(rac{\partial U}{\partial V}
ight)_T dV$$
 need $2^{
m nd}$ Law to evaluate this in terms of P,V,T

$$\left(\frac{\partial U}{\partial V}\right)_{T} = T \left(\frac{\partial P}{\partial T}\right)_{V} - P \quad E \& R \quad eqn.3.19$$

many of the results in E&R ch 3 use this [yet] 'unproven' result; we will derive later class should use result in HW2 #13*

some important relationships between Cp and Cv

$$\frac{1}{n} \left(\frac{\partial H}{\partial T} \right)_{P} = \bar{C}_{P} \quad and \quad \frac{1}{n} \left(\frac{\partial U}{\partial T} \right)_{V} = \bar{C}_{V}$$

to get relationship between C_P and C_V one needs to have relationship involving both H and U; soooo

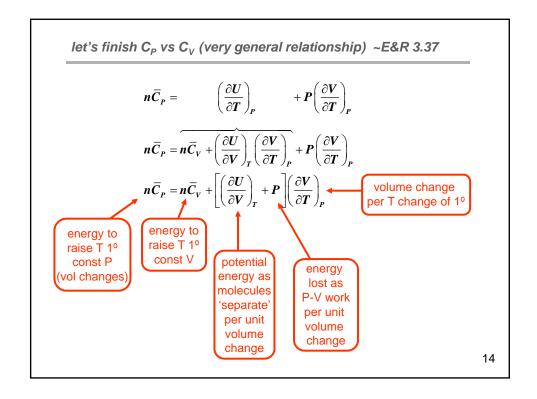
$$H = U + PV$$
$$dH = dU + PdV + VdP$$

12

continuing with relating C_P and C_V

H = U + PV

$$\begin{split} dH &= dU + PdV + VdP \\ \text{divide by } dT, \text{ P constant} \\ \left(\frac{\partial H}{\partial T}\right)_P &= \left(\frac{\partial U}{\partial T}\right)_P + P\left(\frac{\partial V}{\partial T}\right)_P + V\left(\frac{\partial P}{\partial T}\right)_P \\ n\overline{C}_P &= \left(\frac{\partial U}{\partial T}\right)_P + P\left(\frac{\partial V}{\partial T}\right)_P \\ \text{now to get} \quad \left(\frac{\partial U}{\partial T}\right)_P \\ dU &= n\overline{C}_V dT + \left(\frac{\partial U}{\partial V}\right)_T dV \\ \left(\frac{\partial U}{\partial T}\right)_P &= n\overline{C}_V + \left(\frac{\partial U}{\partial V}\right)_T \left(\frac{\partial V}{\partial T}\right)_P \end{split}$$



$$n\overline{C}_{P} \text{ vs } C_{V} \text{ for ideal gas}$$

$$n\overline{C}_{P} = n\overline{C}_{V} + \left[\left(\frac{\partial U}{\partial V}\right)_{T} + P\right] \left(\frac{\partial V}{\partial T}\right)_{P}$$
for ideal gas
$$V = \frac{nRT}{P}$$
Energy, U is function of ONLY T, U(T)
$$\left(\frac{\partial V}{\partial T}\right)_{P} = \frac{nR}{P}$$

$$\left(\frac{\partial U}{\partial V}\right)_{T} = \mathbf{0}$$

$$n\overline{C}_{P} = n\overline{C}_{V} + \left[0 + P\right] \frac{nR}{P}$$

$$n\overline{C}_{P} = n\overline{C}_{V} + nR$$

$$\overline{C}_{P} = \overline{C}_{V} + R \quad \text{for ideal gas}$$

Nature of	Gas	C _v (J mol ⁻¹ K ⁻¹)	C, (J mol ⁻¹ K ⁻¹)	C _p - C _q (J mol ⁻¹ K ⁻²)		γ	
Monatomic	Не	12.5	20.8		8.30		1.66
Monatomic	Ne	12.7	20.8		8.12		1.64
Monatomic	Ar	12.5	20.8		8.30		1.67
Diatomic	H_2	20.4	28.8		8.45		1.41
Diatomic	O ₂	21.0	29.3		8.32		1.40
Diatomic	N_2	20.8	29.1		8.32		1.40
Triatomic	H ₂ O	27.0	35.4		8.35		1.31
Polyatomic	CH ₄	27.1	35.4		8.36		1.31

R=8.31 J mol ⁻¹ K ⁻¹
ideal gas
$\overline{C}_P - \overline{C}_V = R$
monatomic $\overline{C}_V = \frac{3}{2}R$
diatomic $\overline{C}_{v} \cong \frac{5}{2}R$
$\boldsymbol{J} \; \boldsymbol{mol}^{-1} \; \boldsymbol{K}^{-1}$
$\frac{3}{2}$ R = 12.47
$\frac{5}{2}\mathbf{R} = 20.78$
$\frac{7}{3}$ R = 29.10

Table from: http://www.scribd.com/doc/33638936/NCERT-Book-Physics-Class-XI-2

16

in section derive equation following equation

$$n\overline{C}_{V} = n\overline{C}_{P} + \left[\left(\frac{\partial H}{\partial P} \right)_{T} - V \right] \left(\frac{\partial P}{\partial T} \right)_{V}$$

start with dU = dH - PdV - VdP divide by dT with V constant and then boogie along as we just did!!