

Chemistry 163B Winter 2014

Refrigerators and Generalization of Carnot Cycle

Chemistry 163B

Refrigerators and Generalization of Ideal Gas Carnot

(four steps to exactitude)
E&R pp 86-91, 109-111 Raff pp. 159-164

1

statements of the Second Law of Thermodynamics

1. Macroscopic properties of an isolated system eventually assume constant values (e.g. pressure in two bulbs of gas becomes constant; two block of metal reach same T) [Andrews, p37]
2. It is impossible to construct a device that operates in cycles and that converts heat into work without producing some other change in the surroundings. *Kelvin's Statement* [Raff p 157]; *Carnot Cycle*
3. It is impossible to have a natural process which produces no other effect than absorption of heat from a colder body and discharge of heat to a warmer body. *Clausius's Statement, refrigerator*
4. In the neighborhood of any prescribed initial state there are states which cannot be reached by any adiabatic process
~ *Caratheodory's statement* [Andrews p. 58]

2

roadmap for second law

- ✓ 1. Phenomenological statements (what is ALWAYS observed)
- ✓ 2. Ideal gas Carnot [reversible] cycle efficiency of heat → work (Carnot cycle transfers heat only at T_U and T_L)
3. Any cyclic engine operating between T_U and T_L must have an equal or lower efficiency than Carnot OR VIOLATE one of the phenomenological statements (observations)
4. Generalize Carnot to any reversible cycle (E&R fig 5.4)
5. Show that for this REVERSIBLE cycle
 $q_U + q_L \neq 0$ (dq inexact differential)
but
 $\frac{q_U}{T_U} + \frac{q_L}{T_L} = 0$ (something special about $\frac{dq_{rev}}{T}$)
6. S, entropy and spontaneous changes

3

goals for lecture[s]

- Carnot in reverse: refrigerators and heat pumps
- Show that $\epsilon_{ideal\ gas\ rev\ Carnot} \geq \epsilon_{any\ other\ machine}$ otherwise one of the phenomenological statements violated
- Not only for ideal gas but $\epsilon_{ideal\ gas\ rev\ Carnot} = \epsilon_{any\ other\ rev\ Carnot}$
- $dS = \frac{dq_{reversible}}{T}$ $\oint dS = \oint \frac{dq_{reversible}}{T} = 0$ and **S is STATE FUNCTION**

4

Carnot engine arithmetic (for below table see handout) ⇒

ENGINE	q	W_{net}	W_{gross}	
I. isothermal expansion	$+nRT_U \ln \frac{P_1}{P_2}$ 1.3	$-nRT_U \ln \frac{P_1}{P_2}$ 1.2	$+nRT_U \ln \frac{P_1}{P_2}$	heat in at T_U work out
II. adiabatic expansion	0	$nC_V(T_U - T_L)$ 2.4	$-nC_V(T_U - T_L)$	work out
III. isothermal compression	$nRT_L \ln \frac{P_1}{P_2} = -nRT_L \ln \frac{P_2}{P_1}$ 3.3&T.3	$-nRT_L \ln \frac{P_1}{P_2} = nRT_L \ln \frac{P_2}{P_1}$ 3.2&T.3	$-nRT_L \ln \frac{P_1}{P_2}$	heat lost at T_L work in
IV. adiabatic compression	0	$nC_V(T_U - T_L)$ 4.4	$-nC_V(T_U - T_L)$	work in
net gain/cost	$q_U \neq q_L$ $+nRT_U \ln \frac{P_1}{P_2}$		$W_{gross} = W_U + W_{II} + W_{III} + W_{IV} = 0$ $nR(T_U - T_L) \ln \frac{P_1}{P_2}$	$\epsilon = W_{net}/Q_U$ $\epsilon = (T_U - T_L)/T_U$

5

remember Carnot engine

- does net work on surroundings
- and
- net heat $q_{U(I)} + q_{L(III)} = -W_{total}$

6

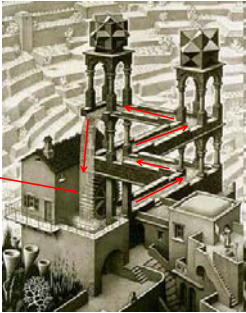
Chemistry 163B Winter 2014 Refrigerators and Generalization of Carnot Cycle

perpetual motion of the first kind (produce work with no heat input)
Escher "Waterfall"

cyclic machine
(water 'flows downhill'
to pillar on left;
'round and 'round')
no energy input

work on surroundings

VIOLATES 1st LAW



7

remember Carnot engine

- does net work on surroundings

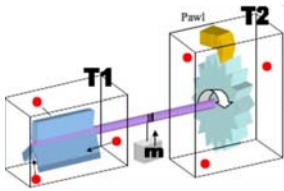
but

- extracts heat from surroundings at T_U
 $q_{U(I)} < 0$
- gives off heat to surroundings at T_L
 $q_{L(III)} > 0$

8

perpetual motion of the second kind (produce work extracting heat from cooler source to run machine at warmer temperature)

Brownian Ratchet



get work only if $T_1 > T_2$

http://wapedia.mobi/en/Brownian_ratchet#1

9

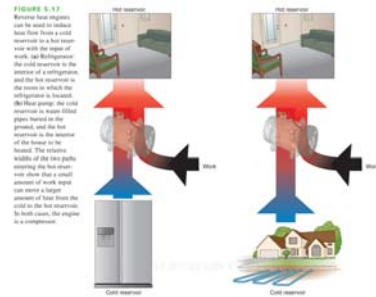
refrigerators and heat pumps: running the Carnot cycle in REVERSE

- it only makes 'sense' to talk about running a process in **REVERSE** for **reversible** processes (on a PV diagram there is no 'reverse' process for irreversible expansion against constant P_{ext})
- however the Carnot cycle is a combination of reversible processes

10

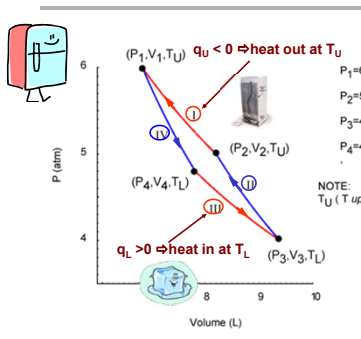
heat pumps and refrigerators (fig. 5.17 E&R) 3rd

FIGURE 5.17
Reversible heat engines can be used to induce heat flow from a cold reservoir to a hot reservoir with the application of work. In Refrigeration, the cold reservoir is the interior of a refrigerator, and the hot reservoir is the interior of a house. The heat pump, the cold reservoir is a heat-filled pipe buried in the ground, and the hot reservoir is the interior of the house to be heated. The interior walls of the house provide the heat sink. The arrows show that a small amount of work input can move a larger amount of heat from the cold to the hot reservoir. In a compressor, the arrows show that a larger amount of heat from the cold to the hot reservoir is a compressor.



11

reverse Carnot cycle: a refrigerator



$w_{sys} = -w_{surr} > 0$
work done ON system

$P_1 = 6 \text{ atm}, T_1 = T_U = 500\text{K}$
 $P_2 = 5 \text{ atm}, T_2 = T_U = 500\text{K}$
 $P_3 = 4 \text{ atm}, q_{2 \rightarrow 3} = 0, T_3 = T_L$
 $P_4 = 4.8 \text{ atm}, T_4 = T_L, q_{4 \rightarrow 1} = 0$

NOTE:
 T_U (T upper) = T_H (T higher or T hotter)

cyclic process
IV adiabatic expansion
III isothermal expansion
II adiabatic compression
I isothermal compression

12

Chemistry 163B Winter 2014 Refrigerators and Generalization of Carnot Cycle

Carnot refrigerator arithmetic (just negatives of Carnot engine)
for below table see handout

REFRIGERATOR	q	-W _{sys}	Q _{surr}	
IV. adiabatic expansion T ₄ → T ₃	0	-nC _v (T ₃ - T ₄)	0	work done by system
III. isothermal expansion at T ₃ P ₄ → P ₃	-nRT ₃ ln $\frac{P_4}{P_3}$	+nRT ₃ ln $\frac{P_4}{P_3}$	-nRT ₃ ln $\frac{P_4}{P_3}$	work done by sys heat withdrawn from T ₃ (ice box)
II. adiabatic compression T ₃ → T ₂	0	-nC _v (T ₂ - T ₃)	0	work on system
I. isothermal compression at T ₂ P ₂ → P ₁	-nRT ₂ ln $\frac{P_2}{P_1}$	+nRT ₂ ln $\frac{P_2}{P_1}$	+nRT ₂ ln $\frac{P_2}{P_1}$	heat out at T ₂ refrig "coils" work on system
net gain/cost		W _{total} = W ₁ + W ₂ + W ₃ + W ₄ = +nR(T ₂ - T ₁) ln $\frac{P_2}{P_1}$	Q _{surr, net} = Q _{surr, III} + +nRT ₃ ln $\frac{P_4}{P_3}$	η _r = C _R = $\frac{-Q_{surr, net}}{W_{total}} = \frac{q_{III}}{w_{total}} = \frac{T_L}{T_U - T_L}$ E&R eqn 5.45

Coefficient of performance of refrigerator: $\eta_r \equiv C_R = \frac{-q_{surr, net}}{w_{total}} = \frac{q_{III}}{w_{total}} = \frac{T_L}{T_U - T_L}$ 13

reverse Carnot cycle: a heat pump

$q_U < 0 \Rightarrow$ heat out at T_U
 $q_L > 0 \Rightarrow$ heat in at T_L

$W_{sys} = -W_{surr} > 0$
work done ON system

P₁ = 6 atm, T₁ = T_U = 500K
P₂ = 5 atm, T₂ = T_U = 500K
P₃ = 4 atm, q_{2→3} = 0, T₃ = T_L
P₄ = 4.8 atm, T₄ = T_L, q_{4→1} = 0

NOTE: T_U (T upper) = T_H (T higher or T hotter)

cyclic process
IV adiabatic expansion
III isothermal expansion
II adiabatic compression
I isothermal compression

14

"goodness of performance"

Since refrigerators and heat pumps are just Carnot machines in reverse, the relationship for $\epsilon = -W_{total}/q_H = (T_U - T_L)/T_U$ holds for these cycles. However only for "engines" does it represent the efficiency or "goodness of performance" (work_{total out}/heat in).

For a refrigerator performance is (heat_{in} at T_L/work_{total})

$$\eta_r \equiv C_R = \frac{-q_{from freezer}}{w_{total}} = \frac{q_{III}}{w_{total}} = \frac{T_L}{T_U - T_L} \quad \text{E\&R eqn 5.45}$$

HW#6 P28 (E&RP5.33)

For a heat pump performance is (heat_{out} at T_U/work_{total})

$$\eta_{hp} \equiv C_{HP} = \frac{q_{given off to room}}{w_{total}} = \frac{-q_I}{w_{total}} = \frac{T_U}{T_U - T_L} \quad \text{E\&R eqn 5.44}$$

(> 1) 15

one more important FACTOID about Carnot machine

for complete reversible Carnot cycle:

$$\oint dU = \Delta U = 0$$

$$\oint dH = \Delta H = 0$$

$$\oint \delta q_{rev} = q = \neq 0$$

$$\oint \delta w_{rev} = w = \neq 0$$

BUT ALSO LET'S LOOK AT:

$$\oint_{cycle} \frac{\delta q_{rev}}{T}$$

16

one more important FACTOID about Carnot machine

$$\int_I \frac{\delta q_{rev}}{T} = \frac{nRT_U \ln \frac{P_1}{P_2}}{T_U}$$

$$\int_{II} \frac{\delta q_{rev}}{T} = 0 \text{ (adiabatic)}$$

$$\int_{III} \frac{\delta q_{rev}}{T} = \frac{-nRT_L \ln \frac{P_1}{P_2}}{T_L}$$

$$\int_{IV} \frac{\delta q_{rev}}{T} = 0 \text{ (adiabatic)}$$

$$\oint_{cycle} \frac{\delta q_{rev}}{T} = 0$$

have we uncovered a new state function entropy (S) ??

$$\Delta S = \int dS = \int \frac{\delta q_{rev}}{T}$$

does it just apply to ideal gas Carnot cycle ??? 17

Generalization of Ideal Gas Carnot Cycle

- Our work on the (reversible) Carnot Cycle using an ideal gas as the "working substance" lead to the relationship

$$\epsilon = \frac{-W_{total}}{q_U} = \frac{T_U - T_L}{T_U}$$

However, the second law applies to machines with any 'working substance' and general cycles.
- The following presentation shows that a (reversible) Carnot machine with 'any working substance' cannot have $\epsilon_{rev any ws} > \epsilon_{Carnot ideal gas}$.
- REVERSING the directions of the ideal gas and 'any rev Carnot' (e.g. Raff, pp 160-162) shows that $\epsilon_{rev any ws} = \epsilon_{Carnot ideal gas}$
- One can also show (E&R Fig 5.4, Raff 162-164) that any Carnot machine has $\oint \delta q_{rev}/T = 0$ and that any reversible machine cycle can be expressed as a sum of Carnot cycles.

18

Chemistry 163B Winter 2014

Refrigerators and Generalization of Carnot Cycle

Carnot machine

Carnot machine: **cyclic, reversible**, machine exchanging heat with environment at only two temperatures T_U, T_L

Carnot engine: 'forward' Carnot cycle

Carnot heat pump: 'reverse' Carnot cycle

$$\epsilon = 1 - \frac{T_L}{T_U} = \frac{-W_{total}}{q_U} \text{ applies to both forward and reverse Carnot cycles}$$

19

can $\epsilon_x > \epsilon_c$ for any Carnot machine X vs ideal gas Carnot machine C ???
(generalizing $\epsilon_{rev} = 1 - T_L/T_U$ that was derived for reversible ideal gas Carnot cycle)

machine X: any 'working substance' (not necessarily ideal gas) exchanges heat at only two temperatures T_U and T_L

the machine X operates as a Carnot engine doing work, while the machine C operates as a reverse Carnot ideal gas engine acting as a heat pump.
In this example the work **done** by X, $(w_t)_x$ is totally used by C: $(w_t)_c = -(w_t)_x$

20

CAN $\epsilon_x > \epsilon_{Carnot}$: worksheet for **numerical example** (all w_x goes into w_{Carnot})

TRY: $\epsilon_x = 0.6 > \epsilon_{Carnot} = 0.5$; specify heat into x $(q_U)_x = 100$ J and all $(w_{out})_x = (w_{in})_{Carnot}$

violation of 2nd Law = 0.5

$\epsilon = \frac{-W_t}{q_U} \quad q_U = \frac{-W_t}{\epsilon} \quad \Delta U = q_U + q_L + w_t = 0$
 $q_U = \frac{-W_t}{\epsilon} \quad w_t = -q_U \epsilon$

$w_{total} = 0$
 $(q_U)_{total} = -20J \text{ (into } T_U)$
 $(q_L)_{total} = +20J \text{ (out of } T_L)$

21

CAN $\epsilon_x > \epsilon_{Carnot}$: worksheet for **numerical example** (all w_x goes into w_{Carnot})

TRY: $\epsilon_x = 0.6 > \epsilon_{Carnot} = 0.5$; specify heat into x $(q_U)_x = 100$ J and all $(w_{out})_x = (w_{in})_{Carnot}$

violation of 2nd Law

$\epsilon = \frac{-W_t}{q_U} \quad q_U = \frac{-W_t}{\epsilon} \quad \Delta U = q_U + q_L + w_t = 0$
 $q_U = \frac{-W_t}{\epsilon} \quad w_t = -q_U \epsilon$

$w_{total} = 0$
 $(q_U)_{total} = -20J \text{ (into } T_U)$
 $(q_L)_{total} = +20J \text{ (out of } T_L)$

22

Clausius Statement of Second Law (numerical example)

we assumed an $\epsilon_x > \epsilon_c$ for ideal gas Carnot and calculated

$w_{total} = 0$

$(q_L)_{total} = +20J$ (into 'combo engine' out of cold reservoir at T_{lower})

$(q_U)_{total} = -20J$ (out of 'combo engine' into heat reservoir at T_{upper})

BUT: It is impossible to have a natural process which produces no other effect than absorption of heat from a colder body and discharge of heat to a warmer body. **Clausius's Statement**

if second law holds $\epsilon_x > \epsilon_c$ cannot be true

23

general proof: can $\epsilon_x > \epsilon_c$ for Carnot machine X vs ideal gas Carnot machine C ???

$(q_U)_x > 0 \quad (q_U)_c < 0$

$\epsilon_x = \frac{-(w_t)_x}{(q_U)_x} \quad \epsilon_c = \frac{-(w_t)_c}{(q_U)_c} = \frac{(w_t)_x}{(q_U)_c}$

$(w_t)_x = -(q_U)_x \epsilon_x \quad (w_t)_c = (q_U)_c \epsilon_c$

$(q_L)_x + (q_U)_x + (w_t)_x = 0 \quad (q_L)_c + (q_U)_c + (w_t)_c = 0$

to give $-(w_t)_x = (w_t)_c$, $-\frac{(q_U)_x}{\epsilon_x} = \frac{(q_U)_c}{\epsilon_c}$, and $(q_U)_c = -\frac{\epsilon_x}{\epsilon_c} (q_U)_x$

$(q_U)_{total} = (q_U)_x + (q_U)_c = (q_U)_x \left(1 - \frac{\epsilon_x}{\epsilon_c}\right)$ (which will be < 0 , for $\epsilon_x > \epsilon_c$)

$(q_L)_{total} = (q_L)_x + (q_L)_c = -(q_U)_x - (w_t)_x + (q_U)_c + (w_t)_c = -(q_U)_{total}$

24

Chemistry 163B Winter 2014 Refrigerators and Generalization of Carnot Cycle

general proof: can $\epsilon_x > \epsilon_c$ for Carnot machine X vs ideal gas Carnot machine C ???

So $(q_U)_{total} < 0$
and
 $(q_L)_{total} = - (q_U)_{total} > 0$
with $w_{total} = (w)_X + (w)_C = 0$
so what's the problem ???
q transferred $T_L \rightarrow T_U$ with no net work
violates Clausius statement of second law
so what's the solution ???
 $\epsilon_x > \epsilon_c$ is not a condition consistent with the Second Law

25

HW#4 Prob. 23

23. The diagram below, where Carnot engine X and Carnot heat pump C are coupled, is similar to that used in lecture to illustrate that the efficiency of any Carnot engine, ϵ_c , has to be the same as that of an ideal gas Carnot engine, ϵ_c , when the engines operate between the same two temperatures. The diagram below differs in that now 33% (-20 J) of the total work done by engine X is done on the surroundings, while 67% (+40 J) is input into the Carnot refrigerator C.

Assume that as indicated $\epsilon_x = 0.6$ and $\epsilon_c = 0.5$
For $(q_U)_X = 100J$, $(w_{surr})_X = -20J$, $(w)_X = +40J$, and $(q_U)_C = 80J$
Calculate:
a. $(q_L)_X$
b. $(q_L)_C$
c. $(q_U)_{heat} = (q_U)_X + (q_U)_C$
d. $(q_L)_{heat} = (q_L)_X + (q_L)_C$
e. $w_{heat} = (w_{surr})_X + (w)_X + (w)_C$
f. Considering the [correct] results for parts c, d, and e, how does the process with coupled Carnot engines X and C having $\epsilon_x = 0.6$ and $\epsilon_c = 0.5$ violate one of the statements of the Second Law of Thermodynamics

26

setup for (HW prob #23) ϵ_x efficiency greater than Carnot
TRY: $\epsilon_x = 0.6 > \epsilon_{carnot} = 0.5$; specify heat into x $(q_U)_X = 100J$ and all (2/3) $(w_{out})_X = (w)_C$

$\epsilon_x = 0.6$ $(q_U)_X = 100J \Rightarrow (w_{total})_X = -60J$
 $\epsilon_c = 0.5$ $(w_{total})_C = +40J \Rightarrow (q_U)_C = 80J$
calc: $(q_L)_X$, $(q_L)_C$
 $(q_L)_{total}$, $(q_U)_{total}$, $(w)_{total}$

ANOTHER CONSEQUENCE OF ASSUMING $\epsilon_x > \epsilon_c$ (2nd Law Statement)

27

$\epsilon_x > \epsilon_c$ (no way !!; slides #20-#24); **but can $\epsilon_x < \epsilon_c$ ($\epsilon_x = 0.5 < \epsilon_c = 0.6$) ??**

derivation a la slide #21 with input of $(q_U)_X = 100J$
gives $(q_U)_{total} = +16\%$ (out of T_U)
 $(q_L)_{total} = -16\%$ (into T_L) $>$ heat from hotter to cooler
 $\epsilon_x = 0.5 < \epsilon_c = 0.6$ is OK (no violation)
if X is machine and C is heat pump
(real machine can be less efficient than reversible Carnot heat pump)

28

CAN $\epsilon_x = 0.5 < \epsilon_c = 0.6$ if X is a some cyclic REVERSIBLE machine

NO: for reversible X and reversible Carnot, WHY: can now run X as heat pump $\epsilon_x = 0.5$ and Carnot as machine $\epsilon_c = 0.6$

same calc as slides 21-22 same violation as $\epsilon_x > \epsilon_c$
 $\epsilon_{Machine}$ must be less than or equal to $\epsilon_{HeatPump}$

29

moral of the story for machines exchanging heat at T_U and T_L

- $\epsilon_{reversible Carnot ideal gas} = (1 - T_L/T_U)$
- $\epsilon_{reversible any working substance}$ cannot be $>$ $\epsilon_{reversible Carnot ideal gas}$ (slides 21-22)
- $\epsilon_{reversible any working substance}$ cannot be $<$ $\epsilon_{reversible Carnot ideal gas}$ (slide 29)
- $\epsilon_{reversible IN GENERAL} = \epsilon_{reversible Carnot ideal gas} = (1 - T_L/T_U)$
- $(\epsilon_{irreversible})_{engine} < \epsilon_{maximum} = (1 - T_L/T_U)$ (slide 28)

$\epsilon_{maximum} = \epsilon_{reversible} = (1 - T_L/T_U)$
general

30

Chemistry 163B Winter 2014 Refrigerators and Generalization of Carnot Cycle

generalization to arbitrary cycle (E&R Fig. 5.4, Raff Fig. 4.11)

WHAT about reversible cycle in general (maybe not only two T's) ?

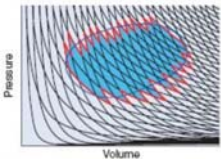
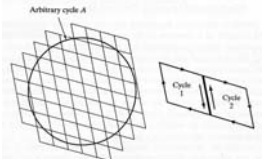


FIGURE 5.4
An arbitrary reversible cycle, indicated by the ellipse, can be approximated to any desired accuracy by a sequence of alternating adiabatic and isothermal segments.



sum of Carnot cycles

31

a REALLY BIG RESULT: connecting ϵ and entropy

have shown generally for any reversible CYCLIC engine operating between T_U and T_L :

$$\epsilon = \frac{-w_{total}}{q_U} = 1 - \frac{T_L}{T_U}$$

now

$$\epsilon = \frac{q_U + q_L}{q_U} = 1 + \frac{q_L}{q_U}$$

thus

$$1 + \frac{q_L}{q_U} = 1 - \frac{T_L}{T_U}$$

$$\frac{q_L}{T_L} + \frac{q_U}{T_U} = 0$$

FOR THE CYCLE
(ANY reversible cyclic process operating between T_U and T_L)

32

the BOTTOM LINE

so generally for this reversible cycle

DEFINE:
$$dS \equiv \frac{\bar{d}q_{reversible}}{T}$$

$$\oint dS = \oint \frac{\bar{d}q_{reversible}}{T} = 0$$

and S is **STATE FUNCTION**

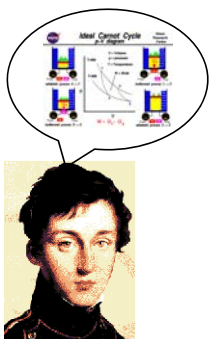
33

roadmap for second law

- ✓ 1. Phenomenological statements (what is ALWAYS observed)
- ✓ 2. Ideal gas Carnot (reversible) cycle efficiency of heat \rightarrow work (Carnot cycle transfers heat only at T_U and T_L)
- ✓ 3. Any cyclic engine operating between T_U and T_L must have an equal or lower efficiency than Carnot OR VIOLATE one of the phenomenological statements (observations)
- ✓ 4. Generalize Carnot to any reversible cycle (E&R fig 5.4)
- ✓ 5. Show that for this REVERSIBLE cycle $q_U + q_L \neq 0$ (dq inexact differential)
but
 $\frac{q_U}{T_U} + \frac{q_L}{T_L} = 0$ (something special about $\frac{\bar{d}q_{rev}}{T}$)
- ✓ 6. **STATE FUNCTION S**, entropy and spontaneous changes (more to come)

34

did Sadi imagine his ideal gas Carnot Cycle?



35

4th IASME/WSEAS International Conference on ENERGY, ENVIRONMENT, ECOSYSTEMS and SUSTAINABLE DEVELOPMENT (EEESD04)
Algarve, Portugal, June 11-13, 2008

**Sadi Carnot's Ingenious Reasoning
of Ideal Heat Engine Reversible Cycles**

MILIVOJE M. KOSTIC
Department of Mechanical Engineering
Northern Illinois University
DeKalb, IL 60115
U.S.A.
kostic@niu.edu; <http://www.kostic.niu.edu>

36

Chemistry 163B Winter 2014

Refrigerators and Generalization of Carnot Cycle

1. Introduction: Sadi Carnot's Far-Reaching Treatise of Heat Engines Was Not Noticed at His Time and Even Not Fully Recognized Nowadays

Sadi Carnot laid ingenious foundations for the Second Law of Thermodynamics before the First Law of energy conservation was known and long before Thermodynamic concepts were established. Sadi Carnot may have not been aware of ingenuity of his reasoning, and we may have never known since he died at age 36 from cholera epidemic.

37

2. Sadi Carnot's Ingenious Reasoning of Ideal Heat Engine Reversible Cycles

54 MOTIVE POWER OF HEAT.

The operations which we have just described might have been performed in an inverse direction and order. There is nothing to prevent forming vapor with the calorio of the body B, and at the temperature of that body, compressing it in such a way as to make it acquire the temperature of the body A, finally condensing it by contact with this latter body, and continuing the compression to complete liquefaction.

The most importantly, Carnot introduced the reversible processes and cycles and, with ingenious reasoning, proved that maximum heat engine efficiency is achieved by any reversible cycle (thus all must have the same efficiency), i.e.:


The motive power of heat is independent of the agents employed to realize it; its quantity is fixed solely by the temperatures of the bodies between which is effected, finally, the transfer of the caloric. [1], i.e.:

$$W = W_{\text{netout}} = Q_{\text{in}} \cdot f_c(T_H, T_L)$$

$$\eta_c = \frac{W_{\text{netout}}}{Q_{\text{in}}} \Bigg|_{\text{Max}} = \frac{f_c(T_H, T_L)}{Q_{\text{in}}} \Bigg|_{\text{Qualitative Junction}} \Bigg|_{\text{Rev.}} \quad (1)$$

38

Carnot vs Einstein ??? (Milivoje Kostic)



$$\{Q_H, Q_L, W_C\} \xrightarrow[\text{REVERSED}]{\text{or}} \{-Q_H, -Q_L, -W_C\}$$

Carnot

$$\eta_c = \frac{W}{Q_{\text{in}}} = \frac{f_c(T_H, T_L)}{Q_{\text{in}}} \Bigg|_{\text{Qualitative Junction}} \Bigg|_{\text{Rev.}}$$

$$\frac{Q(T)}{Q(T_c)} = \frac{f(T)}{f(T_c)} \Bigg|_{f(T), T} = \frac{T}{T_c} = \frac{Q}{Q_c}$$

Carnot Ratio Equality
(By Carnot's Inference)

versus

< ? >

Einstein

$$E = mc^2$$




Fig. 8: Significance of the Carnot's reasoning of reversible cycles is in many ways comparable with the Einstein's relativity theory in modern times. The Carnot Ratio Equality is much more important than what it appears at first. It is probably the most important equation in Thermodynamics and among the most important equations in natural sciences.

39