Chemistry 163B Winter 2014 Clausius Inequality and ΔS for an Ideal Gas

Chemistry 163B

q_{rev} , Clausius Inequality and calculating ΔS for ideal gas P,V,T changes (HW#6)

> Challenged Penmanship Notes

statements of the Second Law of Thermodynamics

- 1. Macroscopic properties of an isolated system eventually assume constant values (e.g. pressure in two bulbs of gas become constant; two block of metal reach same T) [Andrews. p37]
- 2. It is impossible to construct a device that operates in cycles and that converts heat into work without producing some other change in the surroundings. Kelvin's Statement [Raff p 157]; Carnot Cycle
- 3. It is impossible to have a natural process which produces no other effect than absorption of heat from a colder body and discharge of heat to a warmer body. Clausius's Statement, refrigerator
- In the neighborhood of any prescribed initial state there are states which cannot be reached by any adiabatic process

~ Caratheodory's statement [Andrews p. 58]

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four steps to exactitude

$$I. \quad \varepsilon_{\textit{CARNOT[ideal gas]}} = \frac{-w_{\textit{total}}}{q_{tt}} = 1 - \frac{T_L}{T_{tt}} = 1 + \frac{q_L}{q_{tt}}$$

 $II. \quad \varepsilon_{\mathit{ANY REVERSIBLE 'TWO TEMPERATURE' MACHINE}} = \varepsilon_{\mathit{CARNOT[ideal gas]}}$ or else violation of 2nd Law

III. $\oint_{\text{cycle}} \frac{dq_{\text{rev}}}{T} = 0 \quad \text{eqn 5.11 E \& R; demonstrated for ideal gas Carnot;}$

general proof for two temperature reversible cycle; see "a REALLY BIG RESULT" last lecture (Dickerson p. 155; Raff p. 162 - 163)

 $IV. \quad \oint\limits_{\rm cycle} \frac{dq_{\rm rev}}{T} = 0 \quad \text{ for any reversible cyclic process}$

figure 5.4 E & R (Dickerson pp.156 - 159, Raff pp.163 - 164) Entropy

is an exact differential

S is a state function

goals of lecture

- Relate ΔS and q_{irrev}
- 2. Calculate ΔS for P,V, T changes of ideal gas (HW#6) a. using REVERSIBLE path (q_{rev}) [even for irreversible processes] b. using partial derivatives of S with respect to P, V, T [a look ahead]

entropy and heat for actual (irreversible processes): $\mathbf{q}_{\text{irrev}}$

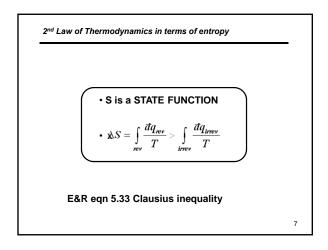
an irreversible (actual) cyclic engine ϵ_{irrev} coupled with a Carnot heat pump of ϵ_{C} **will not** violate 2nd Law if $\epsilon_{\text{irrev}} < \epsilon_{C}$ (viz section, H0#25 SL 29;H0 #28)

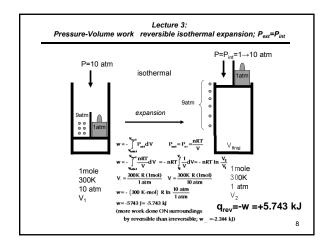
BUT what about q_{irrev} with $\varepsilon_{irrev} < \varepsilon_C$?? $\left(\frac{-\boldsymbol{w}_{total}}{q_{U}} \right)_{irrev} = \left(\frac{q_{U} + q_{L}}{q_{U}} \right)_{irrev} = 1 + \frac{\left(q_{L} \right)_{irrev}}{\left(q_{U} \right)_{irrev}} < 1 - \frac{T_{L}}{T_{U}} = \varepsilon_{reversible}$

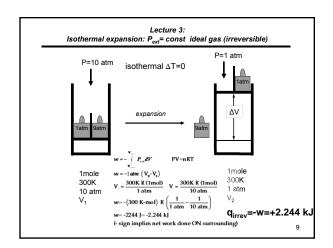
 $\frac{(q_L)_{\rm irrev}}{\pi} + \frac{(q_U)_{\rm irrev}}{\pi} < 0 = \Delta S_{\rm cyclic} \ {\it engine} \ ({\it reversible} \ {\it or irreversible})$

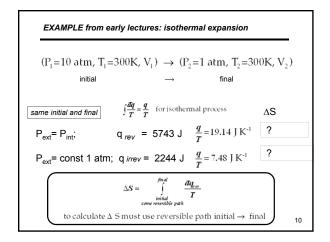
 $\frac{dq}{T} \le dS$ T

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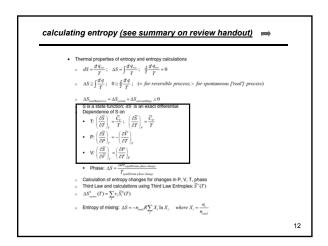


$$\Delta S_{universe} \geq 0$$

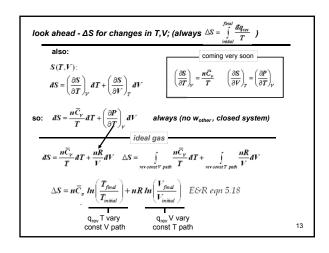
$$SOON:$$

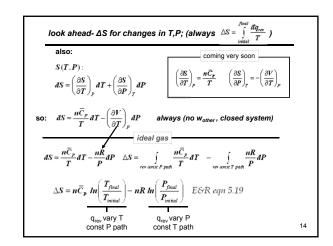
$$\Delta S_{system} + \Delta S_{surroundings} = \Delta S_{universe} \geq 0$$

$$disorder \ increases$$



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End of Lecture

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