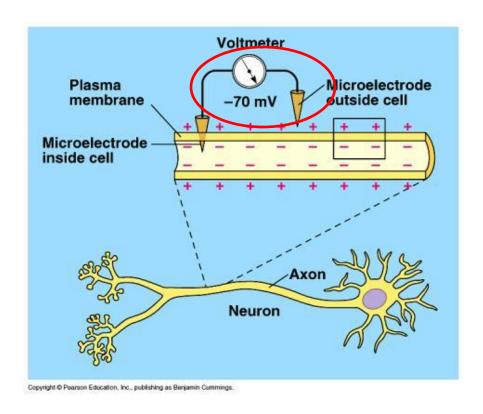
**Chemistry 163B** 

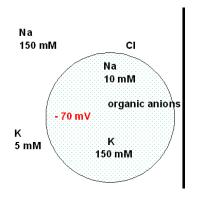
**Concluding Factoids** 

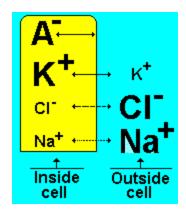
and

**Comments** 

# neuron, resting potential



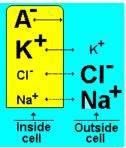




http://projects.gw.utwente.nl/pi/sim/Bovt/concep4.gif

#### resting potential and Nernst Equaiton

# major source of potential: $[K^+]_{outside}(C_{out}) \rightleftharpoons [K^+]_{inside}(C_{in})$



Typical Ion Concentrations Inside and Outside of Nerve Cells

Ion	Concentration Inside	Concentration Outside
Sodium (Na <sup>+</sup> )	12 mM	145 mM
Potassium (K <sup>+</sup> )	140 mM	5 mM
Calcium (Ca <sup>++</sup> )	0.1 μΜ	2 mM

$$\Phi = \Phi^{\circ} - \frac{RT}{n\mathcal{F}} \ln Q$$

$$\Phi^{\circ} = 0$$

$$Q = \frac{[K^+]_{inside}}{[K^+]_{outside}}$$

$$\Phi = -\frac{RT}{n\mathcal{F}} \ln Q = -.02569 \ln \frac{[K^+]_{inside}}{[K^+]_{outside}}$$
$$= -.02569 \ln \frac{140 \ mM}{5 \ mM} = -0.086 \ V$$

The computed number is a little higher than the quantity measured in experiments (-70 mV) but all the factors in this complex physical process

have been accounted for. http://www.medicalcomputing.net/action\_potentials.html

$$E_{rev} = \frac{R \cdot T}{z \cdot F} \cdot \left( \frac{P_K \cdot [K]_o + P_{Na} \cdot [Na]_o + P_{Cl} \cdot [Cl]_i}{P_K \cdot [K]_i + P_{Na} \cdot [Na]_i + P_{Cl} \cdot [Cl]_o} \right)$$

## **Gibbs-Duhem**

the partial molar quantities do not vary independently

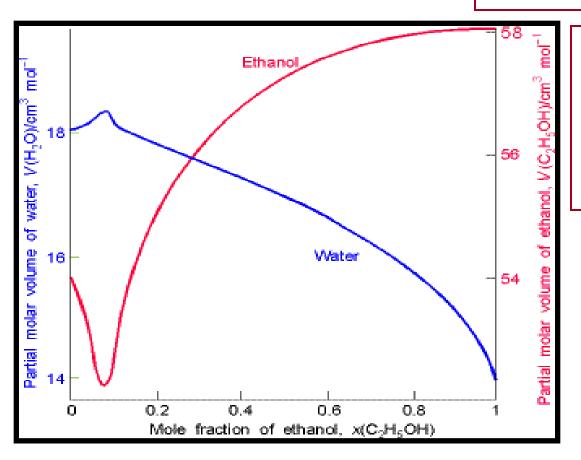
#### Gibbs-Duhem

$$X_{EtOH} \left( \frac{\partial \overline{V}_{EtOH}}{\partial n_{EtOH}} \right)_{T,P,n_{H_2O}} = -X_{H_2O} \left( \frac{\partial \overline{V}_{H_2O}}{\partial n_{EtOH}} \right)_{T,P,n_{H_2O}}$$

#### what are

$$\left(\frac{\partial \overline{V_a}}{\partial n_a}\right)_{T,P,n_b}$$
 and  $\left(\frac{\partial \overline{V_b}}{\partial n_a}\right)_{T,P,n_b}$ 

when a and b form an ideal solution?



do ideal solutions obey the Gibbs-Duhem relation?



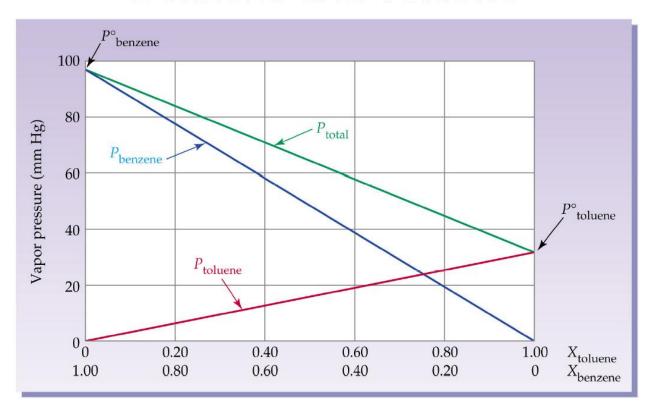
# non-ideal solutions

## benzene-toluene, quite ideal (similar to Fig 9.2 E&R) !!

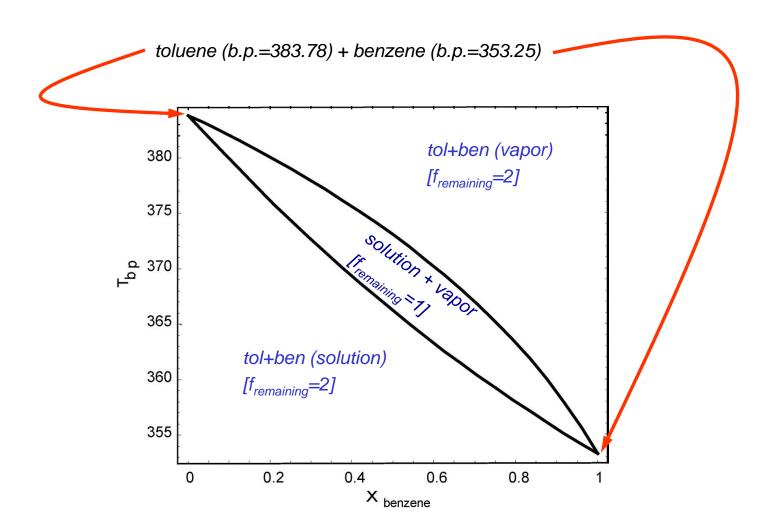
#### Raoult's Law of Ideal Solutions

$$egin{aligned} oldsymbol{P}_A &= oldsymbol{X}_A^{(\ell)} oldsymbol{P}_A^{ullet} & oldsymbol{P}_B &= oldsymbol{X}_B^{(\ell)} oldsymbol{P}_B^{ullet} \ oldsymbol{P}_{total} &= oldsymbol{X}_A^{(\ell)} & oldsymbol{P}_A^{ullet} - oldsymbol{P}_B^{ullet} &+ oldsymbol{P}_B^{ullet} \end{aligned}$$

# Benzene and Toluene



# ideal solution: T vs X (P=1 atm) for solution-vapor equilibrium



#### non-ideal solutions: azeotrope

#### Definition[s]:

- constant boiling liquid
- solution where the mole fraction of each component is the same in the liquid (solution) as the vapor

$$X_i^{(\ell)} = X_i^{(v)}$$

 boiling point of azeotrope may be higher or lower than of pure liquids

#### non-ideal solutions: positive deviations from ideal solution (E&R pp 214-218)

$$CS_2(\ell) + (CH_3)_2CO(\ell)$$

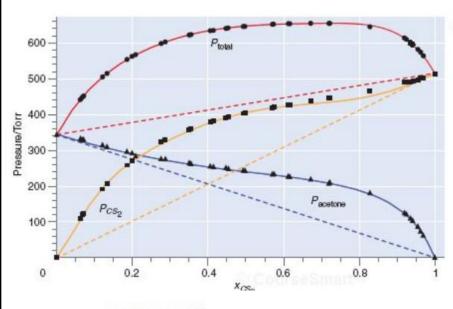
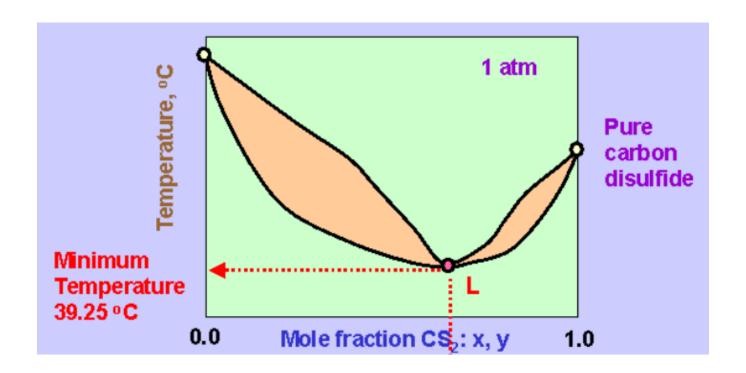


FIGURE 9.13

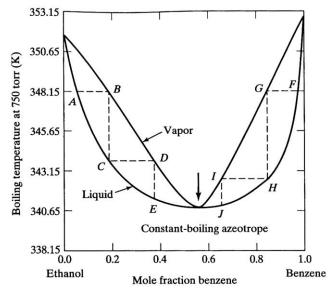
The data in Table 9.3 are plotted versus  $x_{CS_2}$ . The dashed lines show the expected behavior if Raoult's law were obeyed.

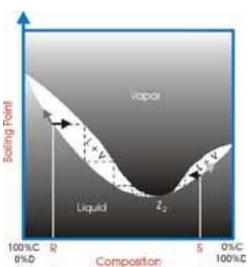
- positive deviations from Raoult's Law: smaller forces between components than 'within' components
- total pressure greater than ideal solution



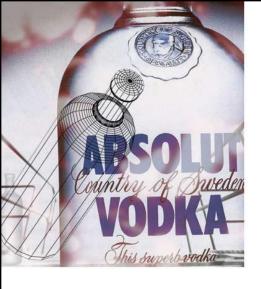
http://www.separationprocesses.com/Distillation/Fig011b.htm

#### low boiling azeotrope

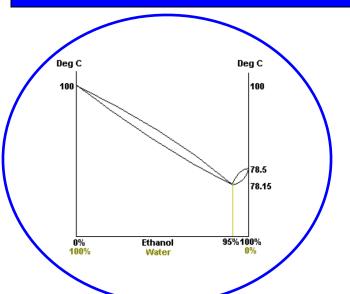




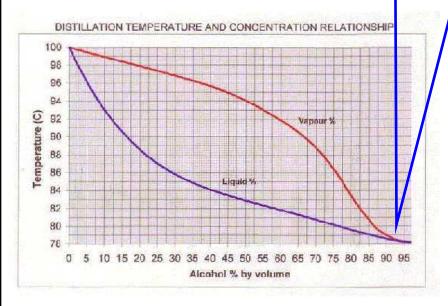
- weaker between component forces
   (A↔B) (than A ↔A, B ↔B)
- fractional distillation leads to constant boiling azeotrope in vapor
- and (in **pot** after azeotrope boils off)
  - $(X_A)_{initial} > (X_A)_{azeotrope}$  pure A
  - $(X_A)_{initial} < (X_A)_{azeotrope}$  pure B



#### Water-Ethanol Mixture



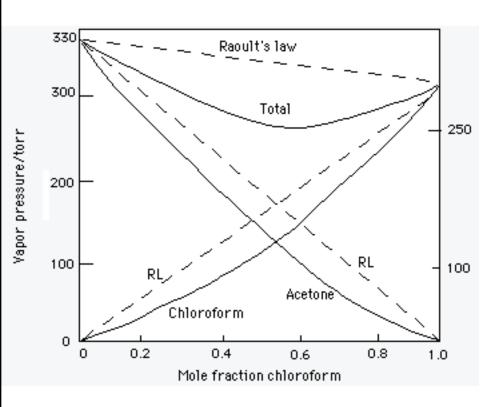




For the water-ethanol mixture, the azeotrope concentration corresponds to ~95% of ethanol in the mixture. This is the limit that can be reached by distillation of a less-alcohol-rich mixture.

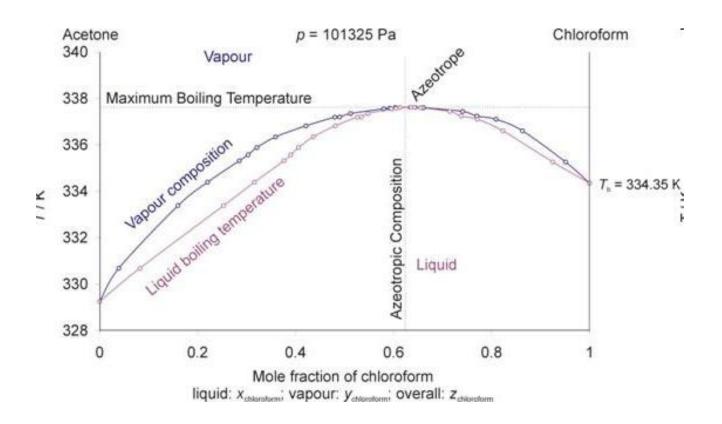
#### non-ideal solutions : negative deviations from ideal solution

$$CHCl_3(\ell) + (CH_3)_2CO(\ell)$$



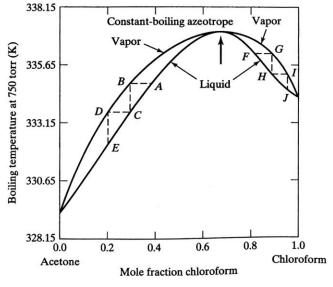
- negative deviations from Raoult's Law: greater forces between components than 'within' components
- total pressure lower than ideal solution

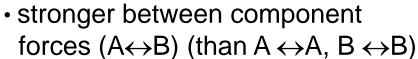
#### acetone-chloroform: negative deviation ⇒ high boiling azeotrope



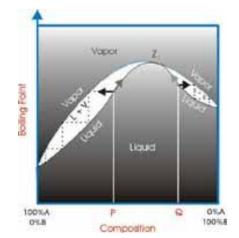
http://www.chm.bris.ac.uk/~chdms/Teaching/Chemical\_Interactions/images/pic192.jpg

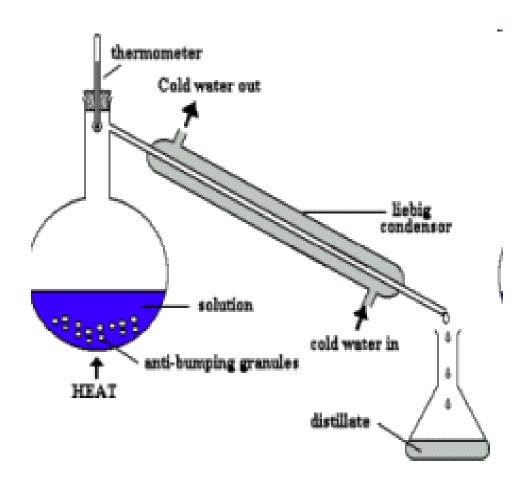
# high boiling azeotrope



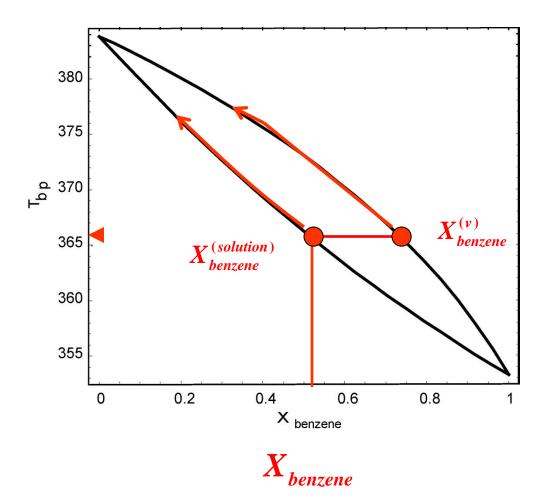


- fractional distillation leads to pure component in vapor until solution (pot) reaches azeotrope composition
  - $(X_A)_{initial} > (X_A)_{azeotrope}$  pure A
  - $(X_A)_{initial} < (X_A)_{azeotrope}$  pure B





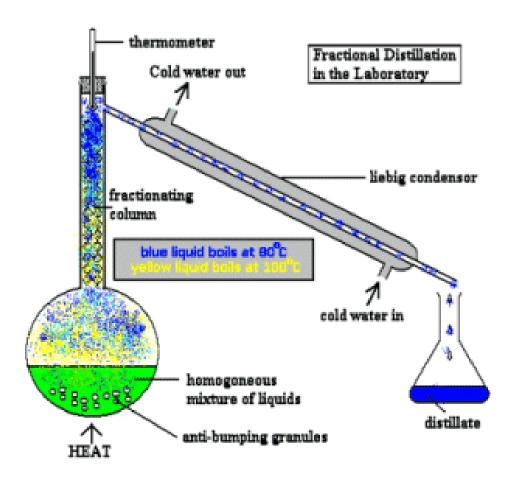
# simple distillation (one evaporation; $T_{bp}$ varies as X changes)



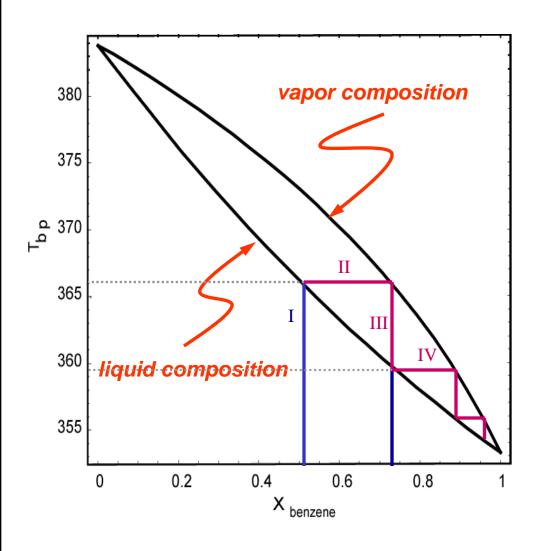
#### add heat

 $X_{benzene}^{(solution)}$  decreases

 $T_{bp}$  increases gradually

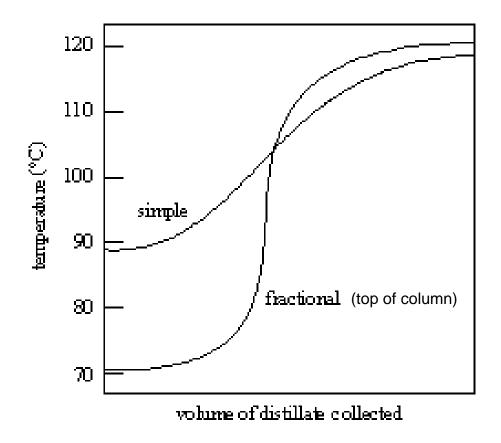


#### Fractional Distilation



- I. start with 50-50 mixture
  - $T_{bp}$  ≈ 366
- II. vapor X<sup>v</sup><sub>benzene</sub> ≈.72
- III. condense  $X_{\text{benzene}}^{\ell} \approx .72$   $T_{\text{bp}} \approx 359.5$
- IV. evaporate
  - vapor X<sup>v</sup><sub>benzene</sub> ≈.88
  - V. etc, ...
  - VI. apporaches  $X_{benzene}=1$  20

# T vs progress for a distillation



http://www.uwlax.edu/faculty/koster/Image119.gif

# **Electrolytes and Debye-Huckel Theory**

## activity coefficients for ions (HW9 #58)

$$BaCl_{2}(s) \rightleftharpoons Ba^{2+}(aq) + 2Cl^{-}(aq)$$

$$K_{sp} = \frac{a_{Ba^{2+}(aq)} a_{Cl^{-}(aq)}}{a_{BaCl_{2}(s)}}$$

$$a_{BaCl_{2}(s)} = 1$$

$$a_{Ba^{2+}(aq)} = \gamma_{Ba^{2+}} \left[ Ba^{2+} \right]$$

$$a_{Cl^{-}(aq)} = \gamma_{Cl^{-}} \left[ Cl^{-} \right]$$

cannot determine  $\gamma_{Ba^{2+}}$  and  $\gamma_{CI^{-}}$  independently

but only 
$$\gamma_{Ba^{2+}} = \gamma_{Cl^{-}} = \gamma_{\pm}$$
  $\gamma_{+} = \gamma_{-} \equiv \gamma_{\pm}$ 

$$K_{sp} = \frac{\gamma \pm \frac{3}{1}}{1} \frac{\left[Ba^{2+}\right]/1M \left[Cl^{-}\right]/1M}{(1)}$$

$$K_{sp} = \gamma \pm \frac{3}{1} \left[Ba^{2+}\right] \left[Cl^{-}\right]^{2}$$

#### Debye-Hückel Theory

- 'a priori' calculation of activity coefficients,  $\gamma$  , for ions
- expect γ < 1 since ions not independent [effective concentration reduced; a < c ]</li>
- $\mu$  is calculated as work done to bring other charges to region surrounding ion in question
- the result is

$$\ln \gamma \pm = -\Omega |z_+ z_-| T^{-\frac{3}{2}} I^{\frac{1}{2}}$$

where  $\Omega$  depends on the solvent's dieelectric constant and other physical constants  $z_+$  and  $z_-$  are the (interger) charges on the cation and anion

and  $I = \frac{1}{2} \sum_{i} m_{i} z_{i}^{2}$  is the ionic strength of the solution,  $m_{i}$  is molal concentration of *ion* 

[E & R: Eqn 10.32 with  $\kappa$  from Eqn. 10.29]

#### Debye-Hückel Theory

$$\ln \gamma \pm = -\Omega |z_{+}z_{-}| T^{-\frac{3}{2}} I^{\frac{1}{2}}$$

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[E & R: Eqn 10.32 with  $\kappa$  from Eqn. 10.29]

$$\begin{split} \log \gamma_{\pm} &= -0.5092 \big| z_{+} z_{-} \big| I^{\frac{1}{2}} \text{ for water solvent at 298.15K} \\ \ln \gamma_{\pm} &= -1.173 \big| z_{+} z_{-} \big| I^{\frac{1}{2}} \quad \text{(E\&R eqn 10.33)} \\ & I = \frac{1}{2} \sum_{i} \ m_{i+} z_{i+}^{2} + m_{i-} z_{i-}^{2} \quad \text{ionic strength} \end{split}$$

#### observations: thermo ≡ heat

- Count Rumford, 1799
- observed water turning into steam when canon barrel was bored
- work ⇔ heat

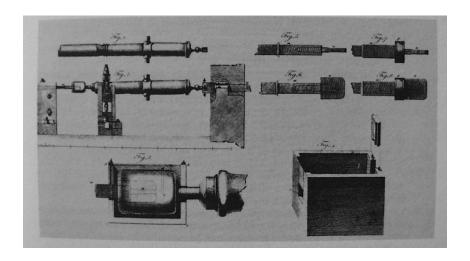
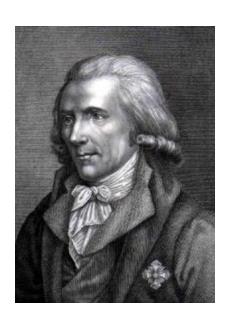


FIGURE 11. An illustration from Rumford's paper, "An Inquiry Concerning the Source of the Heat Which is Excited by Friction," showing the apparatus used by him in the cannon boring experiment. Figure 1, upper left, shows the cannon as received from the foundry, and Figure 2, below, shows it mounted in the machine used for boring. (Reproduced with the permission of Harvard University Press.)





$$dU = d\bar{q} - PdV + dw_{other}$$

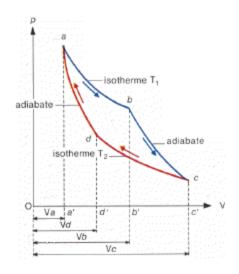
$$dU = 0$$

$$dH = d\bar{q} + VdP + dw_{other}$$

# observations: mechanical efficiency of steam engine

- Sadi Carnot, 1824
- efficiency of engines







# microstates and disorder

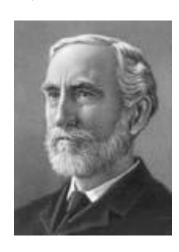
$$\begin{split} \varepsilon_{\textit{fficiency}} &\leq 1 - \frac{T_L}{T_H} \\ dS &\geq \frac{dq}{T} \\ dS &= \frac{dq_{\textit{rev}}}{T} \\ \Delta S_{\textit{UNIVERSE}} &\geq 0 \\ \oint dS &= 0 \\ dU &= TdS - PdV + dw_{\textit{other}} \\ dH &= TdS + VdP + dw_{\textit{other}} \end{split}$$



## "Applications"

How does knowledge about efficiencies of steam engines, mechanical systems, etc, relate to processes in chemical, biological, and geological systems?

#### **ANSWERED BY:**



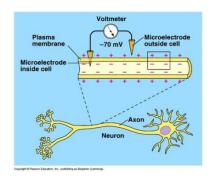
J. W. Gibbs- arguably the frist great American scientist who combined the concepts of heat and entropy and proposed "[Gibbs] Free Energy", **G**, a thermodynamic state function that leads to a whole spectrum of applications

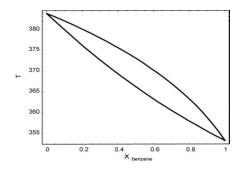
## Free Energy and Equilibrium

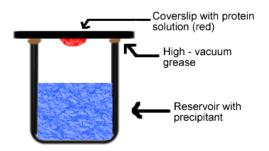
$$\begin{split} \Delta G_{T,P} &= \Delta H_{T,P} - T \Delta S_{T,P} \\ \frac{\Delta G_{T,P}}{T} &= \underbrace{\frac{\Delta H_{T,P}}{T}}_{-\Delta S_{surroundings}} \underbrace{-\Delta S_{T,P}}_{-\Delta S_{system}} \\ dG &= -SdT + VdP + dw_{other} \\ dA &= -SdT - PdV + dw_{other} \end{split}$$

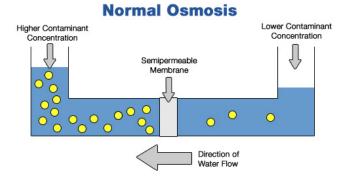


# **Applications**









#### quantitative-deductive mathematical abilities

$$dH = TdS + VdP + \sum_{i} \left(\frac{\partial H}{\partial n_{i}}\right)_{T,P,n_{j} \neq n_{i}} dn_{i}$$

Maxwell-Euler 
$$\left(\frac{\partial V}{\partial S}\right)_{P,n_{all}} = \left(\frac{\partial T}{\partial P}\right)_{S,n_{all}}$$

$$\left(\frac{\partial \mu/T}{\partial T}\right)_{P} = -\frac{\overline{H}}{T^{2}}$$

$$\left(\frac{\partial \Delta\mu_{reac}/T}{\partial T}\right)_{P} = -\frac{\Delta H_{reac}}{T^{2}}$$

$$\left(\frac{\partial \ln K_{eq}}{\partial T}\right)_{P} = \frac{\Delta H_{reac}^{o}}{RT^{2}}$$

#### Final Exam

- Conceptual and 'analytical math' from throughout term
- Problems concentrate on material since last exam.
  - Ideal Solutions and corrections for non-ideality

  - Colligative properties (HW9)
  - Electrochemistry (HW9)
    - Φ and ΔG, Δ*μ*
    - Three cells
  - Vocabulary from concluding factoids
- BRAIN POWER

#### Finals Prep Help Schedule Chemistry 1638

#### Week of March 17-20

Friday, 14 March	9:00-10:00 AM	1567/157 PSB	Regular Office Hours Switkes
	11:00-12:30 AM	CL1	Regular Lecture ELECTROCHEMISTRY II
	2:00-3:00 PM	E&MS B214	Regular Discussion <i>M</i> ednick
	Sample Final on eCommmons     HW#9 Solutions on eCommons     Review Weeks 8-10 on WWW		
Sunday, 16 March	Sample Final Key on eCommons		
Monday, 17 March	11:00-12:30 AM	CL1	LAST Class Switkes CONCLUDING FACTOIDS
	2:00-3:00 PM	1567/157 PS	Regular Office Hours Switkes
	5:00-6:30 PM Thimann 1 Review Session Switkes		
Tuesday, 18 March	4:00-5:00 PM	145 PSB	Last Chance Review Office Hours Liu
Wednesday, 19 March	10:00-12:00 AM	341 PSB	Last Chance Review Office Hours Mednick
Thursday, 20 March	FINAL EXAM 12:00-3:00 PM Classroom 1		

Chemistry 163B Winter 2014 help sessions Finals Prep



#### the warranty

From: Gene Switkes <gene@chemistry.ucsc.edu>

To: switkes@chemistry.ucsc.edu; XXXXXXXXXXX

Sent: Mon, February 15, 2010 10:51:17 AM

Subject: Re: Question from former student

Hi David,

Good to hear from you. 1983-- don't know if the chem 101 warranty is still valid [just joking].

[answered question about disorder]

>Eugene Switkes,

#### chem 163B warranty

Date: Mon, 15 Feb 2010 11:48:07 -0800 (PST)

From: David XXXX XXXXXXXXXX

Subject: Re: Question from former student

Very helpful, thanks.

By the way, I had 163 with you, not 101... and I distinctly recall that you said that the 163 warranty **NEVER** expires...

Cheers, David



# (except)