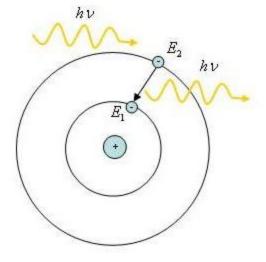
# Chemistry 163B Heuristic Tutorial Second Law, Statistics and Entropy

#### Systems naturally go to lower energy ????







#### falling apples

excited state  $\rightarrow$  ground state

#### chemistry 163B students

http://www.sciencemuseum.org.uk/onlinestuff/snot/ if\_the\_earths\_a\_big\_ball\_why\_dont\_we\_fall\_off\_the\_bottom\_of\_it.aspx http://www.thespectroscopynet.com/ images/PI\_AS\_EB\_StE.jpg http://www.moonbattery.com/ sleeping\_student.jpg

#### The energy lost has to go somewhere ???

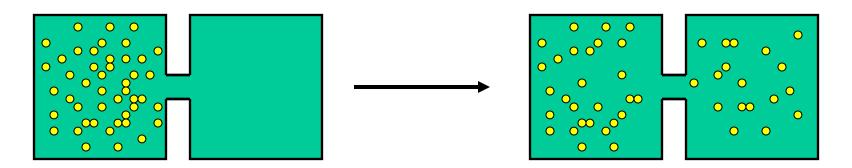
Energy lost by system means energy gained by surroundings.

First Law of Thermodynamics  

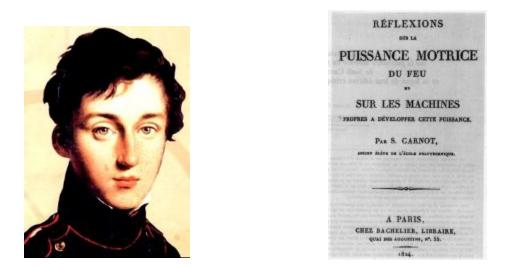
$$\Delta U_{sys} = -\Delta U_{surr}$$

$$\Delta U_{universe} = 0 \text{ (also consider E=mc^2)}$$

- Why do things happen?
- What are the limitations on things that do occur spontaneously?
- $\Delta H < 0$  was considered by Berthelot to be the driving principle for spontaneity
- But: some salts cool when dissolving and why do gasses diffuse if no energy difference

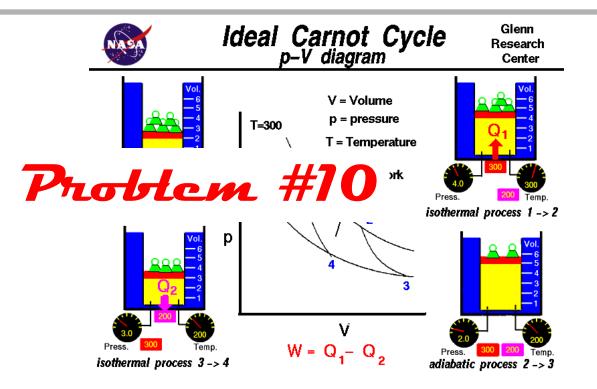


#### SADI CARNOT



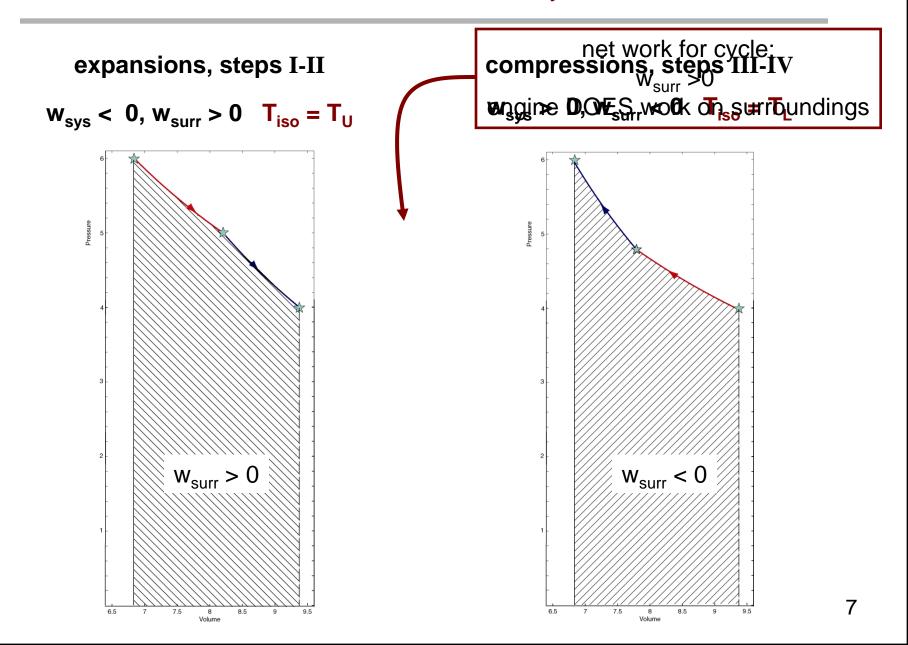
- born 1796, son of Lazare Carnot and antimonarchist
- named Sadi after Persian poet and mystic
- went to Polytechnique Ecole whose faculty included Lagrange, Fourier, Laplace, Berthelot, Ampere, duLong and had as classmates Cauchy, Coriolis, Poisson, Petit, Fresnel
- 1814 went into Corps of Engineers and when monarchy reestablished was sent to boondocks outpost
- 1824 wrote "Reflections on the Motive Power of Heat and Machines Adapted for Developing this Power"

#### Carnot cycle (E&R. pp. 86-90 and HW2 prob #10)

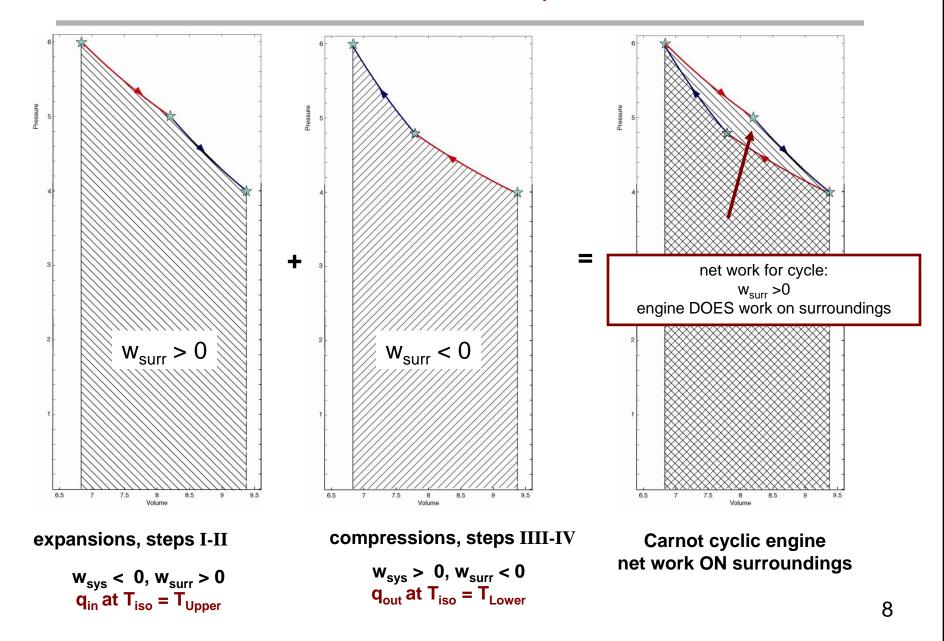


1→2 isothermal reversible expansion at T<sub>1</sub> (300K) 2→3 adiabatic reversible expansion T<sub>1</sub> → T<sub>2</sub> (200K) 3→4 isothermal compression at T<sub>2</sub> (200K) 4→1 adiabatic compression T<sub>2</sub> → T<sub>1</sub> (300K)

#### Carnot cycle (graphical interpretation; $w_{sys} = -\int P_{ext} dV$ ; review)



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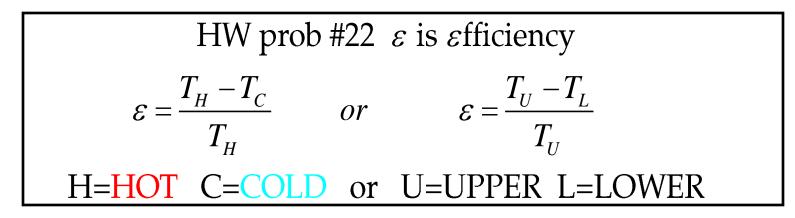


for system in complete cycle:  $\Delta U=0$ ; q >0; w <0 (work DONE on surr) (#10E)

q > 0 ( $q_{in}$ ) at higher  $T_1$ ; q < 0 ( $q_{out}$ ) at lower  $T_2$ 

efficiency=  $-w/q_{1\rightarrow 2}$ (how much net **work out** for **heat in**  $1\rightarrow 2$ )

efficiency will depend on  $T_1$  and  $T_2$ 



- Macroscopic properties of an <u>isolated system</u> eventually assume constant values (e.g. pressure in two bulbs of gas\_becomes constant; two block of metal reach same T) [*Andrews.* p37]
- 2. It is impossible to construct a device that operates in cycles and that converts heat into work without producing some other change in the surroundings. *Kelvin's Statement [Raff p 157]; Carnot Cycle*
- 3. It is impossible to have a natural process which produces no other effect than absorption of heat from a colder body and discharge of heat to a warmer body. *Clausius's Statement, refrigerator*
- 4. In the neighborhood of any prescribed initial state there are states which cannot be reached by any adiabatic process
  - ~ Caratheodory's statement [Andrews p. 58]

#### Tolman's perpetual motion machine

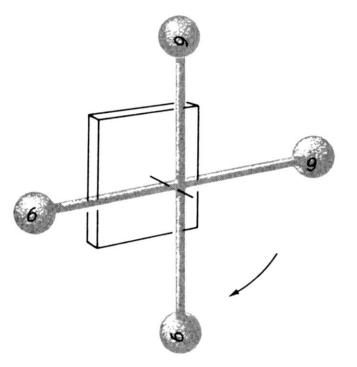
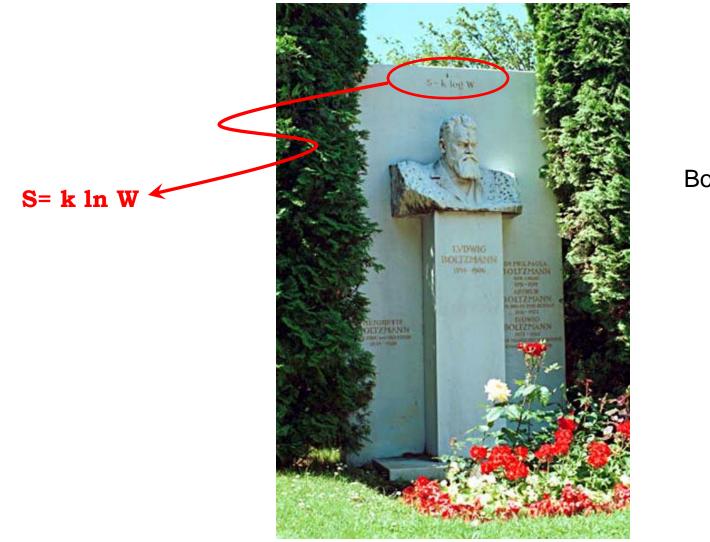
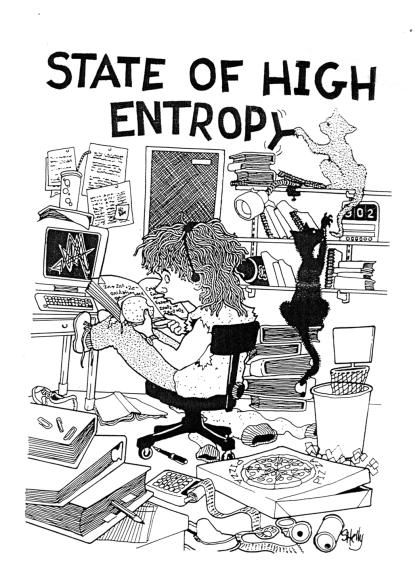


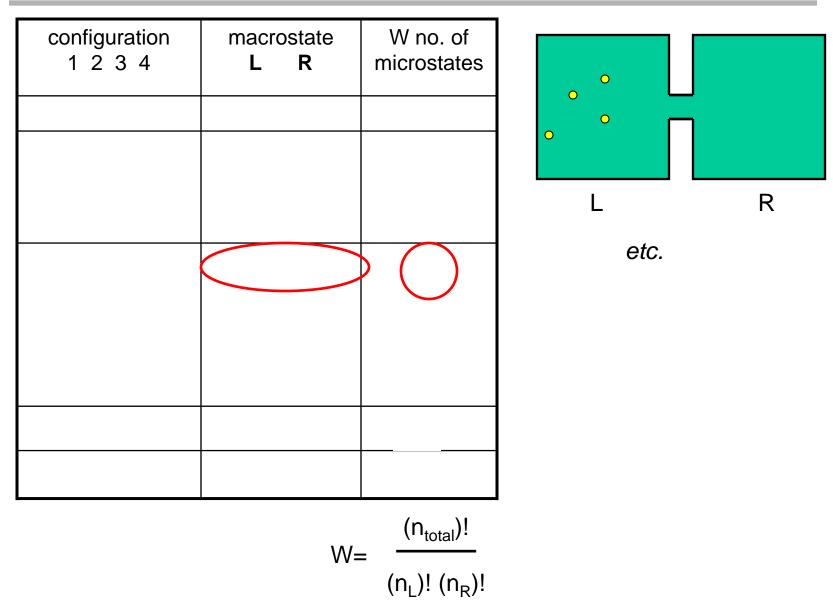
Figure 2-1 Tolman's perpetual motion machine. In his lectures on thermodynamics Professor R. C. Tolman used to delight in presenting this tongue-in-cheek example of a perpetuum mobile of the first kind. The numbers indicate weights, in arbitrary units.



#### Boltzmann

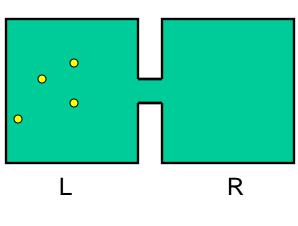


#### microstates and macrostates



#### microstates and macrostates

configuration 1 2 3 4	macr L	ostate R	W no. of microstates
LLLL	4	0	1
LLLR LLRL LRLL RLLL	3	1	4
LLRR LRLR RLLR LRRL RLRL RRLL	2	2	6
~	1	3	4
~	0	4	1

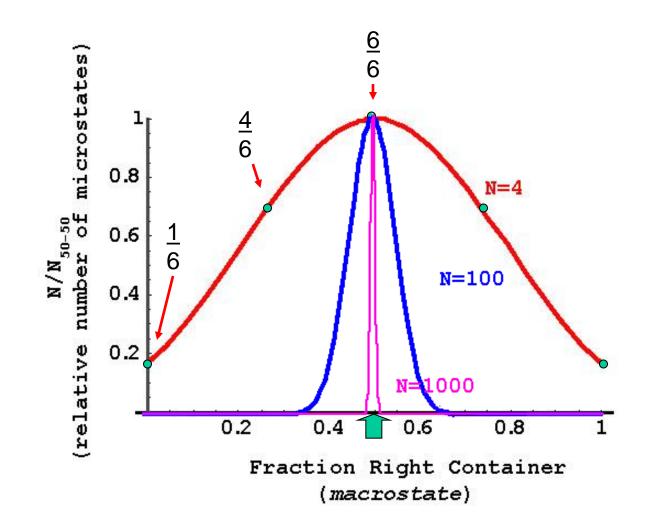


etc.

$$W = \frac{(n_{total})!}{(n_L)! (n_R)!}$$

## microstate: one of the **EQUALLY PROBABLE** configurations of molecules (e.g. LLLL vs LRLR)

macrostate: state with specific macroscopic properties e.g. L=2 R=2



although each allowed microstate (e.g. LLRR or LLLL) is equally probable

the overwhelming number of microstates correspond to macrostates with almost identical macroscopic properties (e.g. ~ 50-50 RvsL)

W, the number of microstates corresponding to the macrostate, is a measure of the DISORDER of the system in that macrostate

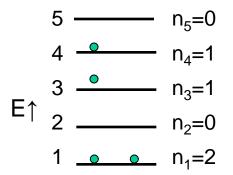
a system "meanders" through all available microstates; but you are only likely to observe it in one of the overwhelming number that correspond to the equilibrium macrostate



famous quote

# " discided happens"

19



 $n_i = number of molecules in energy state \epsilon_i$ 

$$\sum_{i} n_{i} = n_{total}$$

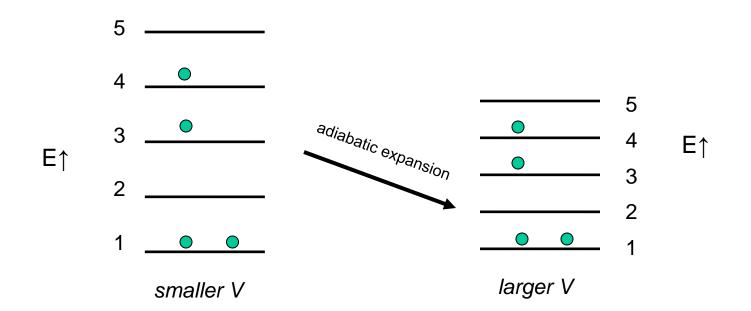
$$W = \frac{n_{total}!}{n_{1}!n_{2}!n_{3}!\cdots}$$
 number of ways of arranging with  $n_{1}, n_{2}, \dots$ 

NOTE: W depends only on then<sub>i</sub>'s, i.e. the distribution of molecules among quantum states

$$\begin{split} U &= E_{total} = \sum_{i} n_{i} \epsilon_{i} \\ dE &= \sum_{i} n_{i} d\epsilon_{i} + \sum_{i} \epsilon_{i} dn_{i} \\ \hline \\ change in energy \\ due to change in \\ energy levels, \\ e.g. 3D quantum \\ p.i.b. change in \\ energy levels as \\ box changes size \end{split}$$

work

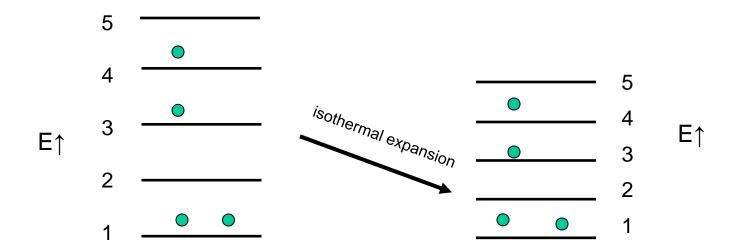
reversible adiabatic expansion ( $\Delta U_{sys} < 0$ ;  $q_{rev} = 0$ )



quantum: expansion, bigger box, energy levels more closely spaced

- Total energy of system decreases ( $\Delta U_{sys} < 0$  for adiabatic expansion)
- NO CHANGE IN LEVEL POPULATIONS if expansion done slowly, reversibly
- $q_{rev} = 0$ ; NO CHANGE IN DISORDER (**W**)

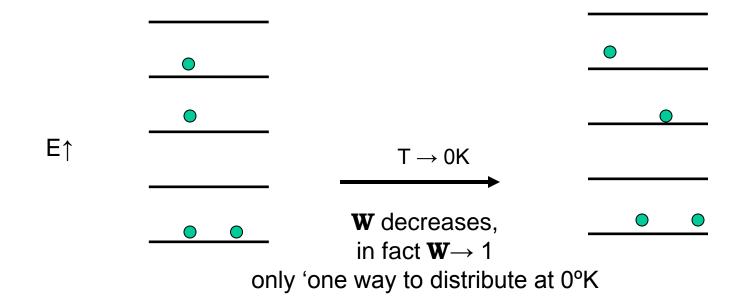
reversible isothermal expansion ideal gas ( $\Delta U_{sys} = 0$ ;  $q_{rev} > 0$ ; w = -q)



to maintain  $\Delta U = 0$  need to put in heat

- Levels get closer due to  $\Delta V > 0$ ; w < 0
- To maintain  $\Delta U = 0$ , q>0 and the level populations have to change and thus W changes
- $q_{rev} > 0$ ; INCREASE IN **W**, INCREASE IN DISORDER

			•
	•	T increases,	
E↑	••	W (disorder) increases	

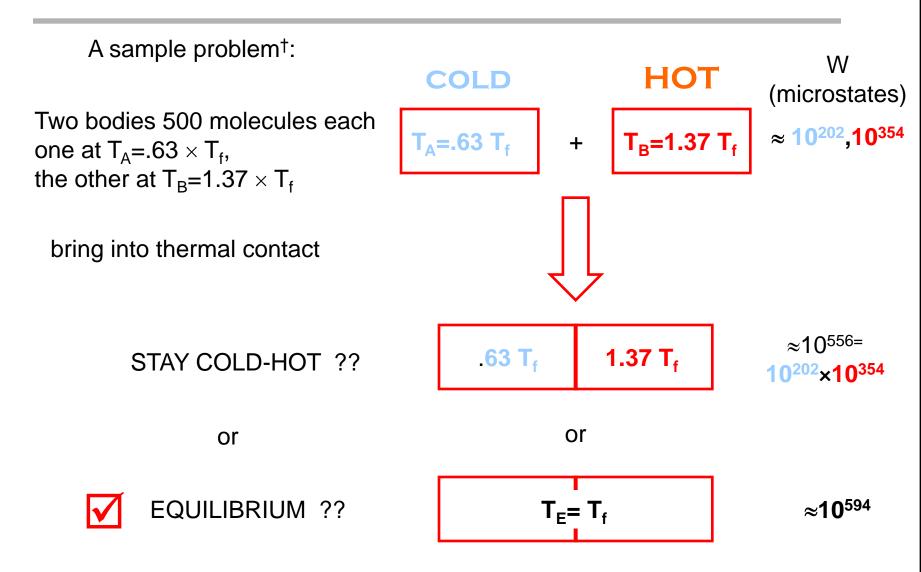


## $S = k \ln W$

## S is entropy k=Boltzmann's constant= 1.3807 $\times$ 10<sup>-23</sup> J K<sup>-1</sup>

disorder increases  $\Leftrightarrow$  entropy increases

- Disorder,  $\boldsymbol{W},$  did not change during an adiabatic reversible expansion (q\_{rev} =0)
- Disorder, **W**, increased in isothermal reversible expansion  $(q_{rev} > 0)$
- Disorder, **W**, increased with T increase (q>0)
- Disorder, **W**, decreased with T decrease (q<0)
- As  $T \rightarrow 0$ ,  $W \rightarrow 1$



*† adapted from Nash, <u>ChemThermo</u>, Addison Wesley, pp 175-176* 

The equilibrium macrostate is  $\frac{10^{594}}{10^{556}} = 10^{38}$  time more likely than the hot-cold state, even though every (microstate)<sub>hot-cold</sub> has the same likelihood as a (microstate)<sub>equilibrium</sub>.

No more than one time in 10<sup>38</sup> a measurement will find the blocks in a half-hot and half-cold configuration.

If you had observed the microstate of the system 10<sup>6</sup> times a second constantly (without a msec of rest!) from the beginning of the universe until your midterm Friday (10<sup>10</sup> years) **the odds against ever seeing a (microstate)**<sub>hot-cold</sub> **are** 1:10<sup>15</sup> !!!

† adapted from Nash, ChemThermo, Addison Wesley, pp 175-176

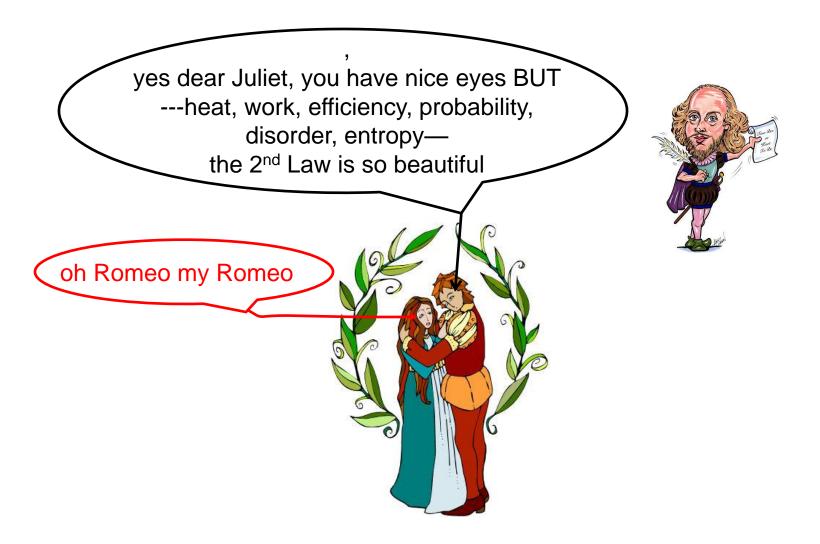
#### take home message continued<sup>†</sup>

....... a progressive increase in "disorder" necessarily accompanies an approach to equilibrium characterized by the assumption of macrostates with ever-increasing values of W. And what may at first appear to be a purposeful "drive" towards states of maximal disorder, can now be seen to arise from the operation of blind chance in an assembly where all microstates remain equally probable, but where the overwhelming proportion of microstates is associated with the maximally disordered (nearly identical) macrostates corresponding to equilibrium macroscopic properties.

*†* adapted from Nash, <u>ChemThermo</u>, Addison Wesley, p 26.

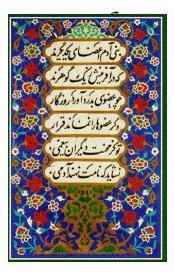
## much more molecules, probability, statistical mechanics

### CHEMISTRY 163C



End Of Introductory Lecture on Second Law and Dísorder





بنی آ دم اعضاء یک پیکرند که در آ فرینش زیک کوهرند چو عضوی بدرد آ ورد روزگارد دکر عضوه را غاند قرار

literal translation (Farzaneh): Of one Essence is the human race thus has Creation put the base One Limb impacted is sufficient For all Others to feel the Mace

-Saadi (1184-1283)

interpretative translation on UN building: Human beings are members of a whole, In creation of one essence and soul. If one member is afflicted with pain, Other members uneasy will remain. If you have no sympathy for human pain, The name of human you cannot retain.

Persían Poet 13th Century



Nicolas Léonard Sadi Carnot (1796-1832) in the dress uniform of a student of the <u>École Polytechnique</u>  $\mathcal{E} = 1 - \frac{T_L}{T_U}$ French Thermodyamicist Namesake 19<sup>th</sup> century

Sadi

Saadi

and

#### heu-ris-tic [hyoo-ris-tik or, often, yoo-] adjective

1. serving to indicate or point out; stimulating interest as a means of furthering investigation.



