

roadmap for second law

- 1. Phenomenological statements (what is ALWAYS observed)
- 2. Ideal gas Carnot <code>[reversible]</code> cycle efficiency of heat \to work (Carnot cycle transfers heat only at T $_{\rm U}$ and T $_{\rm L}$)
- Any cyclic engine operating between T_U and T_L must have an equal or lower efficiency than Carnot OR VIOLATE one of the phenomenological statements (observations)
- 4. Generalize Carnot to any reversible cycle (E&R fig 5.4)
- 5. Show that for this REVERSIBLE cycle

 $q_U + q_L \neq 0$ (dq inexact differential)

hut

 $\frac{q_U}{T_U} + \frac{q_L}{T_L} = 0 \quad (something special about \frac{dq_{rev}}{T})$

6. S, entropy and spontaneous changes

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from lecture on 2nd Law and probability (disorder)

(something special about $\frac{\overline{d}q_{rer}}{T}$)

- Disorder, $\mathbf{W},$ did not change during an adiabatic reversible expansion (q $_{\rm rev}$ =0)
- Disorder, $\boldsymbol{W},$ increased in isothermal reversible expansion $(q_{\text{rev}}\!>\!0)$
- Disorder, **W**, increased with T increase (q>0)
- Disorder, **W**, decreased with T decrease (q<0)
- As T → 0, **W** →1

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statements of the Second Law of Thermodynamics (roadmap #1)

- Macroscopic properties of an <u>isolated system</u> eventually assume constant values (e.g. pressure in two bulbs of gas becomes constant; two block of metal reach same T) [Andrews. p37]
- It is impossible to construct a device that operates in cycles and that converts heat into work without producing some other change in the surroundings. Kelvin's Statement [Raff p 157]; Carnot Cycle
- It is impossible to have a natural process which produces no other effect than absorption of heat from a colder body and discharge of heat to a warmer body. Clausius's Statement, refrigerator
- In the neighborhood of any prescribed initial state there are states which cannot be reached by any adiabatic process ~ Caratheodory's statement [Andrews p. 58]

goals of Carnot arithmetic (step 2 of roadmap)



- 1. Carnot cycle is "engine" that produces work from heat
- Define efficiency:
 efficiency=(net work done by machine)/(heat energy input to machine)
- Today, arithmetic manipulations of 1st Law results from ideal gas Carnot cycle (HW2 #10) to show that this efficiency depends only on the two temperatures at which heat is transferred to and from surroundings (the T_U of step 1 and T_L of step 3; the non-adiabatic paths)
- 4. Although for [reversible] Carnot cycle $\oint d \!\!\!\!/ q_{\scriptscriptstyle rev} \neq 0$

$$\oint \frac{dq_{rev}}{r} = 0$$

from Carnot cycle

for system in complete cycle: ΔU =0; q >0; w <0 (work DONE on surr) (Prob #10e)

q > 0 (q_{in}) at higher T_H ; q < 0 (q_{out}) at lower T_L

efficiency= -w/ $q_{1\rightarrow2}$ (how much net work out (-sign) for heat in $1\rightarrow2$)

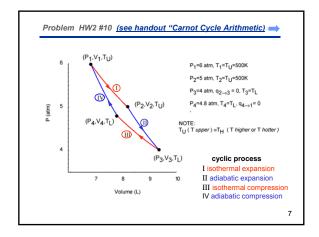
efficiency will depend on $T_{\text{\scriptsize U}}$ and $T_{\text{\scriptsize L}}$

HW5 prob #22 ε is ε fficiency

$$\varepsilon = \frac{T_H - T_C}{T}$$
 or $\varepsilon = \frac{T_U - T_C}{T}$

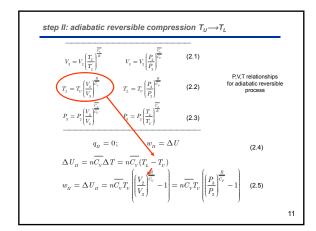
H=HOT C=COLD or U=UPPER L=LOWER

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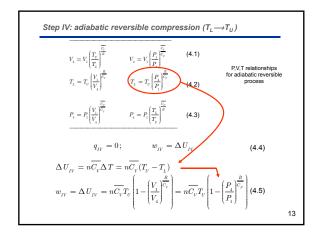


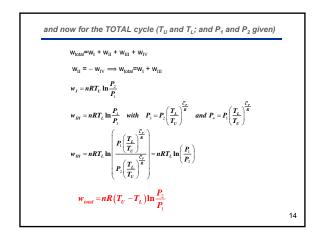
• get $w_I + w_{II} + w_{IV} = w_{total}$ • get $q_I = q_{input}$

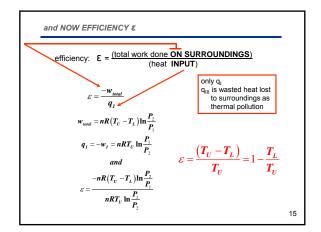
Summary (see handout "Summary of Heat and Work for the Carnot Cycle $+nRT_v \ln \frac{P_1}{P_2}$ 1.3 $-nRT_v \ln \frac{P_1}{P}$ $+ \, nR \, T_{\scriptscriptstyle U} \, \ln \frac{P_{\scriptscriptstyle 1}}{P_{\scriptscriptstyle 2}}$ $-n\overline{C_v}(T_L-T_v)$ expansion heat lost at T_L
$$\begin{split} &nR \ T_L \ \ln \frac{P_q}{P_4} = \\ &-nR \ T_L \ \ln \frac{P_1}{P_2} \end{split}$$
$$\begin{split} &-nR \; T_L \; \ln \frac{P_4}{P_4} \\ &= \; nR \; T_L \; \ln \frac{P_1}{P_2} \end{split} \quad \textbf{3.28T.3}$$
 $-nRT_L \ln \frac{P_1}{P_s}$ work in IV. adiabatio $-n\overline{C_v}(T_v-T_{\scriptscriptstyle L})$ $+ nR T_v \ln \frac{P_1}{P}$ $\varepsilon = (T_U - T_L)/T_U$ $nR(T_v - T_L) \ln \frac{P_1}{P}$

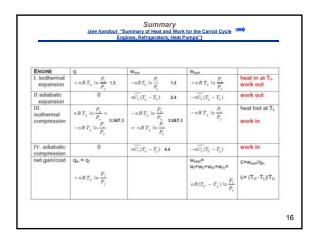


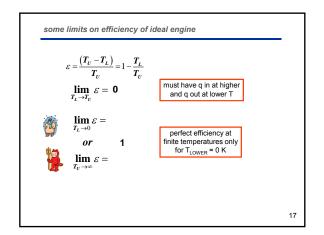
Step III: isothermal reversible compression at T_L $\Delta U_{III} = 0 \qquad (3.1)$ $w_{III} = -nRT_L \ln \frac{V_4}{V_3} = nRT_L \ln \frac{P_4}{P_3} \qquad (3.2)$ $q_{III} = -w_{III} = nRT_L \ln \frac{V_4}{V_3} = nRT_L \ln \frac{P_3}{P_4} \qquad (3.3)$

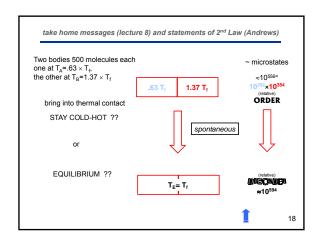


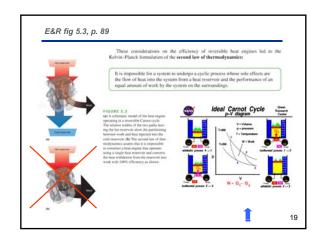


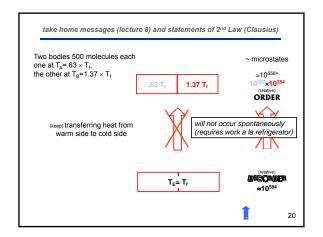












End of Lecture 9

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