Chemistry 163B Colligative Properties Challenged Penpersonship Notes



colligative

One entry found. Main Entry: col·li·ga·tive Pronunciation: kä-lə- gā-tiv, kə- li-gə-tiv Function: *adjective*

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: depending on the number of particles (as molecules) and not on the nature of the particles <pressure is a *colligative property*>

Handout #55

- A. Freezing point depression
- **B.** Boiling Point Elevation
- C. Osmotic Pressure

- I. The pure solvent (component B) is originally in equilibrium in the two phases.
- II. Addition of solute (component A) lowers the chemical potential of the solvent in the solution phase
- III. Temperature (freezing point depression, boiling point elevation) or pressure (osmotic pressure) must be altered to reestablish equilibrium between the solution and the pure solvent phase.
- IV. Obtain relationships between X_A or X_B and change in T or P.

I. pure solvent is originally in equilibrium in the two phases

pure solid[•]_B
$$\rightleftharpoons$$
 pure liquid[•]_B at T_{f}^{\bullet} the normal melting T_{fusion}
 $\mu_{B}^{s\bullet}(T_{f}^{\bullet}) = \mu_{B}^{\ell\bullet}(T_{f}^{\bullet})$
 $\Delta\mu_{B}(T_{f}^{\bullet}) = \mu_{B}^{\ell\bullet}(T_{f}^{\bullet}) - \mu_{B}^{s\bullet}(T_{f}^{\bullet}) = 0$
 $\Delta\overline{H}(T_{f}^{\bullet}) = \Delta\overline{H}_{B melting} > 0$ for solid \longrightarrow liquid

freezing point depression (solid *≠* solution)

II. Still at T_f^{\bullet} , add solute A to solvent with resulting mole fractions X_A and X_B

for solid phase of B there is no change :

$$\mu_B^{s\bullet}(T_f^{\bullet}) = \mu_B^{solid}(T_f^{\bullet})$$



for the solvent (B) in solution:

$$\mu_B^{\ell}(T_f^{\bullet}) \equiv \mu_B^{solvent} \equiv \mu_B^{\ell (in \ so \ln)}(T_f^{\bullet}) = \mu_B^{\ell \bullet}(T_f^{\bullet}) + RT_f^{\bullet} \ln\left(\gamma_B X_B\right)$$

so now $\Delta \mu_B(T_f^{\bullet}) = \mu_B^{\ell}(T_f^{\bullet}) - \mu_B^{s \bullet}(T_f^{\bullet}) = \Delta \mu_B^{\bullet}(T_f^{\bullet}) + RT_f^{\bullet} \ln\left(\gamma_B X_B\right)$
where $\Delta \mu_B^{\bullet}(T_f^{\bullet}) = \mu_B^{\ell \bullet}(T_f^{\bullet}) - \mu_B^{s \bullet}(T_f^{\bullet})$

and $\Delta \mu_{B}^{\bullet}(T_{f}^{\bullet}) = 0$ since pure liquid and solid are in equilibrium at T_{f}^{\bullet} thus $\Delta \mu_{B}(T_{f}^{\bullet}) = RT_{f}^{\bullet} \ln(\gamma_{B}X_{B}) < 0$

so the forward reacton (melting of the solid) would now occur spontaneously at T_{f}^{\bullet}

III. Alter temperature to restore equilibrium $T_f^{\bullet} \rightarrow T_f$

$$\left(\frac{\partial \frac{\Delta \mu}{T}}{\partial T}\right)_{P} = -\frac{\Delta \overline{H}}{T^{2}}$$

$$\int_{T_{f}}^{T_{f}} d\left(\frac{\Delta\mu_{B}}{T}\right)_{P} = -\int_{T_{f}}^{T_{f}} \frac{\Delta\overline{H}_{B \text{ melting}}}{T^{2}} dT \qquad \text{old stuff}$$

$$\left(\frac{\Delta\mu_{B}(T_{f})}{T_{f}}\right)_{P} - \left(\frac{\Delta\mu_{B}(T_{f}^{\bullet})}{T_{f}^{\bullet}}\right)_{P} = -\int_{T_{f}}^{T_{f}} \frac{\Delta\overline{H}_{B \text{ melting}}}{T^{2}} dT$$

III. Alter temperature to restore equilibrium (continued)

$$\left(\frac{\Delta\mu_B(T_f)}{T_f}\right)_P - \left(\frac{\Delta\mu_B(T_f^{\bullet})}{T_f^{\bullet}}\right)_P = -\int_{T_f^{\bullet}}^{T_f} \frac{\Delta\overline{H}_{B \text{ melting}}}{T^2} dT$$

$$\left(\frac{\Delta\mu_B(T_f)}{T_f}\right)_P = 0 \text{ since at 'new' equilibrium } T_f , \Delta\mu_B(T_f) = 0$$
and
$$\left(\frac{\Delta\mu_B(T_f^{\bullet})}{T_f^{\bullet}}\right)_P = R\ln(\gamma_B X_B) \quad from \text{ eqn in } II.$$

$$-R\ln(\gamma_B X_B) = -\int_{T_f^{\bullet}}^{T_f} \frac{\Delta\overline{H}_{B \text{ melting}}}{T^2} dT$$

$$R\ln(\gamma_B X_B) + \left[-\int_{T_f^{\bullet}}^{T_f} \frac{\Delta\overline{H}_{B \text{ melting}}}{T^2} dT\right] = 0$$

change in $\Delta \mu_{\rm B}$ due to adding solute

change in $\Delta \mu_B$ due to temperature change

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IV. Obtain relationships between X_B and change in T

$$R \ln \left(\gamma_B X_B \right) = \int_{T_f}^{T_f} \frac{\Delta \overline{H}_{B \text{ melting}}}{T^2} dT$$

$$\Delta \overline{H}_{B \text{ melting}} \sim \text{independent of T}$$

$$R \ln \left(\gamma_B X_B \right) = -\Delta \overline{H}_{B \text{ melting}} \left[\frac{1}{T_f} - \frac{1}{T_f^*} \right]$$

since $lhs < 0 \Rightarrow T_f < T_f^*$ (freezing point **depression**)

$$\gamma_B X_B = \exp \left[-\frac{\Delta \overline{H}_{B \text{ melting}}}{R} \left[\frac{1}{T_f} - \frac{1}{T_f^*} \right] \right] \text{ (integration of eqn 9.31 E\&R)}$$

IV. Obtain relationships between X_B and change in T (cont)

$$\gamma_B X_B = \exp\left[-\frac{\Delta \overline{H}_{B \text{ melting}}}{R} \left[\frac{1}{T_f} - \frac{1}{T_f^{\bullet}}\right]\right]$$

$$-\frac{R}{\Delta \overline{H}_{B melting}} \ln(\gamma_B X_B) + \frac{1}{T_f^{\bullet}} = \frac{1}{T_f}$$
$$T_f = \frac{T_f^{\bullet} \Delta \overline{H}_{B melting}}{\Delta \overline{H}_{B melting} - RT_f^{\bullet} \ln(\gamma_B X_B)} \quad (\sim \text{ eqn } 9.32 \text{ E\&R})$$



I. pure solvent at P_{left} is originally in equilibrium with pure solvent at P_{right} ; i.e. $P_{left}=P_{right}=P_0$

pure $\ell iquid_{B}^{\bullet}(P_{0}, left) \rightleftharpoons pure \ell iquid_{B}^{\bullet}(P_{0}, right)$ at *T* 'left' and 'right' refer to compartments separated by solute impermeable membrane $\mu_{B}^{\bullet}(P_{0}, left) = \mu_{B}^{\bullet}(P_{0}, right)$

II. in left hand compartment add solute A to solvent with resulting mole fractions X_A and X_B

add X_A solute to liquid in 'left' compatient resulting in X_B for solvent $\mu_B^{\ell}(P_0, left) = \mu_B^{\ell}(P_0, left) + RT \ln(\gamma_B X_B) < \mu_B^{\ell}(P_0, right)$

 $\mu_B^{\ell}(P_0, left) < \mu_B^{\ell \bullet}(P_0, right)$

so the solvent B moves spontaneously left \leftarrow right (i.e. diluting solution on left)

III. alter Pressure: $P_{left} \rightarrow P_0 + \pi$ to restore equilibrium solution $(X_B, P_0 + \pi, left) \rightleftharpoons pure \ solvent(P_0, right)$ $\left(\frac{\partial \mu_B^{left}}{\partial P}\right)_T = \overline{V}_B$

$$\int_{P_0}^{P_0+\pi} d\mu_B^{left}\left(X_B\right) = \int_{P_0}^{P_0+\pi} \overline{V}_B dP$$

assuming solvent is incompressible $(\overline{V}_B \text{ doesn't change with pressure at constant T})$ $\mu_B^{left} (X_B, P_0 + \pi) = \mu_B^{left} (X_B, P_0) + [P_0 + \pi - P_0] \overline{V}_B$ $\mu_B^{left} (X_B, P_0 + \pi) = \mu_B^{left} (X_B, P_0) + \pi \overline{V}_B$ osmotic pressure (III, alter pressure, continued)

$$\mu_{B}^{left}\left(X_{B},P_{0}+\pi\right) = \mu_{B}^{left}\left(X_{B},P_{0}\right) + \pi \overline{V}_{B}$$
$$\mu_{B}^{left}\left(X_{B},P_{0}+\pi\right) = \mu_{B}^{\bullet}\left(P_{0}\right) + RT\ln\left(\gamma_{B}X_{B}\right) + \pi \overline{V}_{B}$$

want π to restore equilibrium such that $\mu_{B}^{left}(X_{B}, P_{0} + \pi) = \mu_{B}^{\bullet \ right}(P_{0})$

$$\underbrace{\frac{\mu_{B}^{\bullet}(P_{0}) + RT\ln(\gamma_{B}X_{B}) + \pi\overline{V_{B}}}_{left}}_{\pi} = \underbrace{\frac{\mu_{B}^{\bullet}(P_{0})}{right}}_{right}$$

$$\pi = -\frac{RT\ln(\gamma_{B}X_{B})}{\overline{V_{B}}}$$

$$\pi = -\frac{RT \ln(\gamma_B X_B)}{\overline{V_B}}$$
for $\gamma_B \approx 1$ and $X_B = 1 - X_A$

$$\pi = -\frac{RT \ln(1 - X_A)}{\overline{V_B}}$$

$$\ln(1 + x) \approx x \quad \text{for small } x \quad (i.e. \text{ dilute solution, } X_A \text{ small})$$

$$\pi = \frac{X_A RT}{\overline{V_B}}$$

$$X_A = \frac{n_A}{n_A + n_B} \quad \text{and } n_A + n_B \approx n_B \quad \text{for dilute solution}$$

$$\pi \approx \frac{n_A RT}{n_B \overline{V_B}}$$

$$\pi V_B = n_A RT$$

$$\pi V_{\text{solution}} = n_{\text{solute}} RT$$

Handout #55 Colligative Properties

from relationships for Chem 163B final:

Colligative properties:

• freezing point lowering:
$$\gamma_B X_B = \exp\left[-\frac{\Delta \overline{H}_{fusion}}{R}\left[\frac{1}{T_f} - \frac{1}{T_f^{\bullet}}\right]\right]$$

• boiling point elevation:
$$\gamma_B X_B = \exp\left[\frac{\Delta \overline{H}_{vaporization}}{R}\left[\frac{1}{T_{bp}} - \frac{1}{T_{bp}^{\bullet}}\right]\right]$$

$$\pi = \frac{-RT\ln(\gamma_B X_B)}{\overline{V}_B}$$

• osmotic pressure:

$$\pi \approx \frac{n_A RT}{V_B} = \frac{n_{solute} RT}{V_{solvent}} \quad for \ dilute \ solution$$

reverse osmosis



FROM TAP WATER TO PURE WATER





 Low production cost - gives you water of a guaranteed quality for pennies per gallon





Reverse Osmosis





http://www.zenon.com/image/resources/glossary/reverse_osmosis/normal_osmosis.jpg

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effect of osmosis on blood cells



Woman dies after water-drinking contest

Water intoxication eyed in 'Hold Your Wee for a Wii' contest death

AP Associated Press updated 7:24 p.m. PT, Sat., Jan. 13, 2007

SACRAMENTO, Calif. - A woman who competed in a radio station's contest to see how much water she could drink without going to the bathroom died of water intoxication, the coroner's office said Saturday.

Jennifer Strange, 28, was found dead Friday in her suburban Rancho Cordova home hours after taking part in the "Hold Your Wee for a Wii" contest in which KDND 107.9 promised a Nintendo Wii video game system for the winner.

"She said to one of our supervisors that she was on her way home and her head was hurting her real bad," said Laura Rios, one of Strange's co-workers at Radiological Associates of Sacramento. "She was crying and that was the last that anyone had heard from her."

B NBC VIDEO



Launch

Woman in water drinking contest dies Jan. 15: Sacramento Bee reporter Christina Jewett talks to MCNRC TV/a Castagea Braver about the docth of a

to MSNBC-TV's Contessa Brewer about the death of a woman who had competed in a radio station contest. MSNBC

End of lecture