# Chemistry 163B Thermodynamics Winter 2020

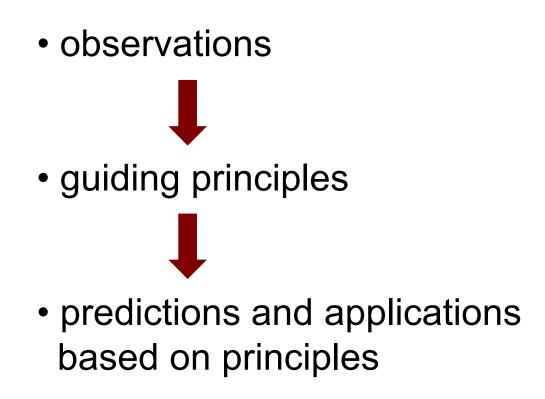


- Introduction and Class Resources, etc.
- Careful definition of thermodynamic variables (P, V, T, etc)
- Ideal gas ENERGY DEPENDS ONLY ON TEMPERATURE (derivation)
- Van der Waals equation (example of equation of state for 'real' gas)

## Thermodynamics is a

# really beautiful scientific

# story !!

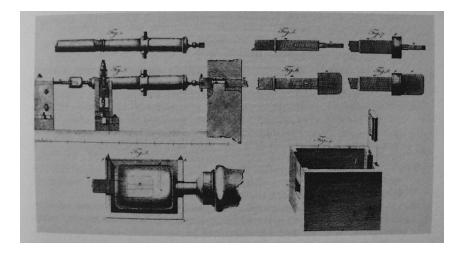


### Thermodynamics is very 'working class' in its origins:

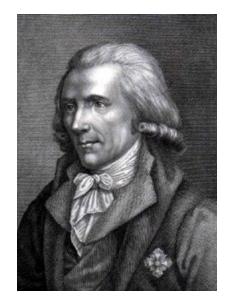


#### observations: thermo = heat

- Count Rumford, 1799
- observed water turning into steam when canon barrel was bored
- work ⇔ heat



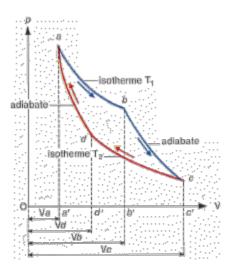
**FIGURE 11.** An illustration from Rumford's paper, "An Inquiry Concerning the Source of the Heat Which is Excited by Friction," showing the apparatus used by him in the cannon boring experiment. Figure 1, upper left, shows the cannon as received from the foundry, and Figure 2, below, shows it mounted in the machine used for boring. (Reproduced with the permission of Harvard University Press.)



- Sadi Carnot, 1824
- efficiency of engines





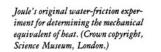


## the thermodynamic functions U, H, and S (1<sup>st</sup> and 2<sup>nd</sup> laws)

#### • Boltzmann, late 19<sup>th</sup> century, molecular picture of entropy

- Clausius, 1860 Entropy 2<sup>nd</sup> LAW OF THERMODYNAMICS
- **1st LAW OF THERMODYNAMICS**

• Conservation of heat and work (Joule, 1845)





Boltzmann



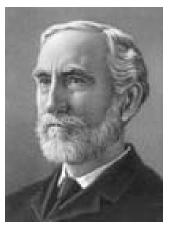
Clausius

#### guiding principles

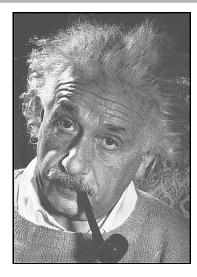


How does knowledge about efficiencies of steam engines, mechanical systems, etc, relate to processes in chemical, biological, and geological systems?

**ANSWERED BY:** 

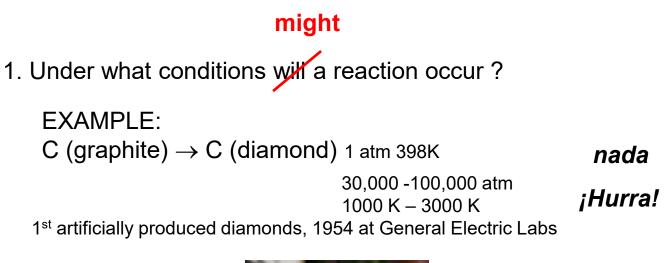


J. W. Gibbs- arguably the frist great American scientist who combined the concepts of heat and entropy and proposed "[Gibbs] Free Energy", **G**, a thermodynamic state function that leads to a whole spectrum of applications



A theory

is the more impressive the greater the simplicity of its premises, the more different kinds of things it relates, and the more extended its area of applicability. Hence the deep impression that classical thermodynamics made upon me. It is the only physical theory of universal content concerning which I am convinced that, within the framework of the applicability of its basic concepts, it will never be overthrown (for the special attention of those who are skeptics on principle). types of problems that thermodynamics addresses (reactions)





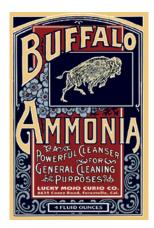
2. How far will a reaction proceed (given enough time)? How do the thermal and entropic properties determine EQUILIBRIUM ? How do the EQUILIBRIUM conditions depend on T,P ?

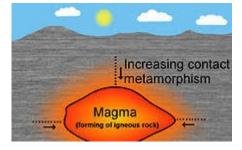


 $N_2(g) + 3H_2(g) \leftrightarrows 2NH_3(g)$ 

what are best T,P for NH<sub>3</sub> products?

**The Haber Process** 





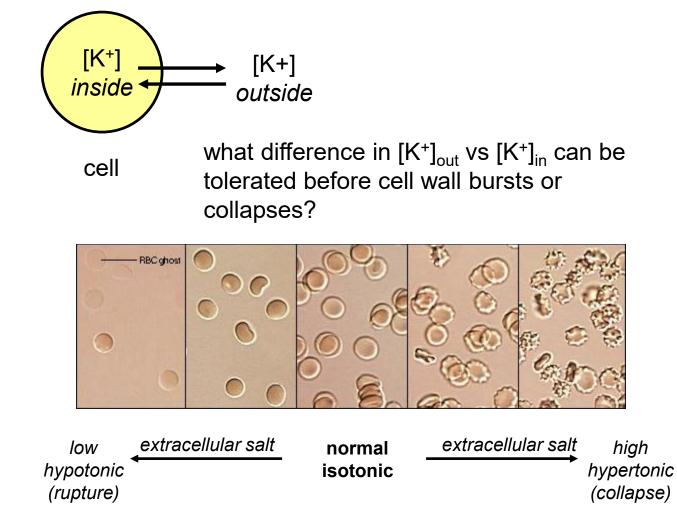
 $SiO_2 + CaCO_3 \leftrightarrows CaO \bullet SiO_2 + CO_2 (g)$ quartz calcite wollastonite

geologic thermometer:

The fraction of wollastonite in a rock sample can be used to estimate the temperature at which the rock metamorphosis occurred [the T at which the equilibrium was rapidly frozen]

#### **Geologic Thermometer**

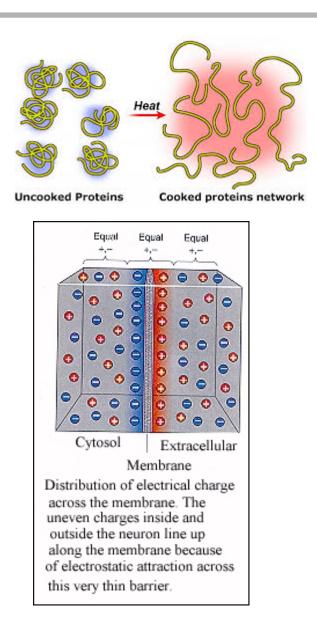
3. Chemical and physical changes in biological systems



http://www.vivo.colostate.edu/hbooks/cmb/cells/pmemb/osmosis.html

4. Why does an egg hard boil? (protein conformation)

5. Membrane potentials and ion concentrations in neurons.(electrochemistry and thermodynamics)



6. Thermodynamic feasibility of SO<sub>2</sub> removal

 $SO_2(g) \leftrightarrows S(s) + O_2(g)$ 



- 1. How fast a reaction proceeds (kinetics, catalysts, enzymes; in chem 103, BMB 100, chem 163C)
- 2. Macroscopic thermodynamics does not prove or require hypotheses about molecular structure; however we will use our knowledge of molecular structure to get an atomic "picture" of thermodynamic processes. The quantitative connection is made by statistical thermodynamics:

chem 163A ⇔ chem 163B chem 163C

3. Although in chemistry 163B we will study how thermodynamics put limits on processes at equilibrium, there exists a whole other field of *non-equilibrium thermodynamics*.

- 1. Clear conceptual picture of thermodynamics
- 2. Ability to relate and apply thermodynamics to chemical and biological systems

#### 3. **PROBLEM SOLVING: Chemistry + Logic + Mathematics**

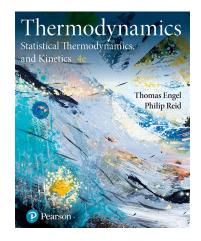
- 4. How to do independent and advanced reading/research in areas that utilize thermodynamics.
- 5. THE GRAND PICTURE of how thermodynamics and quantum mechanics fit into our picture of 'nature'.
- 6. Advanced mathematical techniques

www.chemistry.ucsc.edu  $\Rightarrow$  course pages  $\Rightarrow$  Chemistry 163B

http://switkes.chemistry.ucsc.edu/teaching/CHEM163B/

• lectures: A MUST

• homework: A MUST



- <u>sections:</u> required (A MUST)
- <u>tutorial EVENT & Office Hours & LSS (for YOU!)</u>
- midterms: 31<sup>st</sup> January 28<sup>th</sup> February
   final: 19<sup>th</sup> March, 4:00-7:00 PM (*last class 13<sup>th</sup> March*)

# Learn Thermodynamics

- <u>Lectures</u>
- Sections (start Monday, Jan 13; HW#1 Probs 1-8)
- **Tutorial Event** (starts **TOMORROW** Tues, Jan 7, HW#1 Probs1-2)
- Office hours (start TODAY Mon, Jan 6)
- LSS Tutor



#### first Tutorial Tuesday 7th January, NS Annex 102, 5:25PM-6:30PM

Chemistry 163B

Winter 2020

**Chemistry 16** 

#### **Comments on Mathematical Techniques for Chemistry 163B**

Our text (*E&R: ME2, pp* 17-28; *ME3, pp*.63-68) (*Appendix B.2.1-B.2.3*)<sub>3re</sub> contains detailed information on the aspects of differential and integral calculus relevant to our study of thermodynamics. We will review these techniques in the context of class derivations and homework problems, rather than just as abstract mathematical exercises. However it is useful to categorize them below. In your first discussion section the TAs will also comment on the techniques.

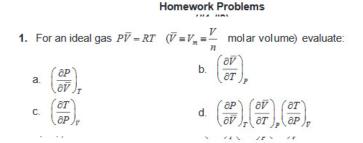
- 1. Partial derivatives:
  - a. Know physical meaning of partial derivatives
  - b. Know how to evaluate them mechanically
  - c. Know chain rule
- 2. You should have "at hand" the derivatives and integrals of functions like:  $x^n$ ,  $x^n$ ,  $\ln(x)$ ,  $e^{ax}$ , sin ax, cos ax ["at hand" = in your accessible neurons]
- 3. Differential expressions (E&R 2.8; pp 39-41, 63 )[ pp 28, 45-49]3rd
  - a.  $\vec{a}\psi$  is inexact differential if  $\int_{initial}^{final} \vec{a}\psi$  depends on the path

from initial  $\rightarrow$  final This implies there is no "underlying" well behaved, function  $\psi$ that changes like  $d\psi$ 

- b.  $d \psi$  is exact differential if  $\int_{initial}^{final} d \psi$  does not depend on the path from initial  $\rightarrow$  final
- Implications that arise from d ψ being an exact differential:
  - a. There is a well behaved function  $\psi$  whose change is described by  $d\psi$

b. 
$$d\psi(V,T) = \left(\frac{\partial\psi}{\partial V}\right)_T dV + \left(\frac{\partial\psi}{\partial T}\right)_V dT$$
  
or in more general notation  
 $d\psi(x, y, z) = \left(\frac{\partial\psi}{\partial x}\right)_{yz} dx + \left(\frac{\partial\psi}{\partial y}\right)_{zz} dy + \left(\frac{\partial\psi}{\partial z}\right)_{zy} dz$ 

- c.  $\oint d\psi = 0$  (integral for any cyclic path; i.e. the initial and final states are identical)
- d.  $\int_{initial}^{jinal} d\psi = \psi(final) \psi(initial)$



- e. One can often get, via the chain rule for differentiation, rigorous results by "canceling  $\partial$ 's". However the correct result for part d is **NOT** what one would obtain by just "canceling  $\partial$ 's" in the numerators and denominators in each of the three terms. Why for part d can one NOT apply the chain rule to get  $\left(\frac{\partial P}{\partial P}\right) = 1$ ? [NOTE: you may evaluate part d and e using the specific results from a, b, c for an ideal gas. However the correct result is a more general relationship for any well behaved function z(x,y)]
- 2. For a Van der Waals gas:  $\left(P + \frac{a}{\overline{p}^2}\right)(\overline{p} b) = RT$  evaluate: a.  $\left(\frac{\partial P}{\partial \overline{p}}\right)_T$  b.  $\left(\frac{\partial^2 P}{\partial \overline{p}^2}\right)_T$ c.  $\left(\frac{\partial P}{\partial T}\right)_{\overline{p}}$  d.  $\left[\frac{\partial}{\partial T}\left(\frac{\partial P}{\partial \overline{p}}\right)_T\right]_T$ e.  $\left[\frac{\partial}{\partial \overline{p}}\left(\frac{\partial P}{\partial T}\right)_p\right]_T$

f. How do the results of parts d and e compare? Why is this?

#### Tutorial Tuesday 7<sup>th</sup> January

Homework Problems (#1-#8)

**1.** For an ideal gas  $P\overline{V} = RT$  ( $\overline{V} \equiv V_m \equiv \frac{V}{n}$  molar volume) evaluate:

a. 
$$\left(\frac{\partial P}{\partial \overline{V}}\right)_T$$
  
b.  $\left(\frac{\partial \overline{V}}{\partial T}\right)_P$   
c.  $\left(\frac{\partial T}{\partial P}\right)_{\overline{V}}$   
d.  $\left(\frac{\partial P}{\partial \overline{V}}\right)_T \left(\frac{\partial \overline{V}}{\partial T}\right)_P \left(\frac{\partial T}{\partial P}\right)_{\overline{V}}$ 

**2.** For a Van der Waals gas:  $\left(P + \frac{a}{\overline{V}^2}\right)(\overline{V} - b) = RT$  evaluate:

a. 
$$\left(\frac{\partial P}{\partial \overline{V}}\right)_T$$
  
b.  $\left(\frac{\partial^2 P}{\partial \overline{V}^2}\right)_T$   
c.  $\left(\frac{\partial P}{\partial T}\right)_{\overline{V}}$   
d.  $\left[\frac{\partial}{\partial T}\left(\frac{\partial P}{\partial \overline{V}}\right)_T\right]_T$ 

e. 
$$\left[\frac{\partial}{\partial \overline{V}} \left(\frac{\partial P}{\partial T}\right)_{\overline{V}}\right]_{T}$$

Winter 2020

3. Engel & Reid problem P1.38 (4th edition)

#### to HW#1 listing on CANVAS

★4. (optional) The Van der Waals and virial expressions are two commonly used equations of state as approximations to real gas behavior:

$$P = \frac{RT}{(\overline{V} - b)} - \frac{a}{\overline{V}^2} \quad Van \ der \ Waals$$

 $P = RT\left[\frac{C_1(T)}{\overline{V}} + \frac{C_2(T)}{\overline{V}^2} + \frac{C_3(T)}{\overline{V}^3} \dots + \frac{C_n(T)}{\overline{V}^n} \dots\right] \quad virial$ 

## a. Show that the first three virial coefficients are related to the Van der Waals

parameters a and b in the following way:

 $C_1(T)=1$ 

C<sub>2</sub>(T)=b-a/RT

C<sub>3</sub>(T)=b<sup>2</sup>

HINT:

note that the virial expansion is just a Taylor (Maclaurin) series in  $z^{k} = \left(\frac{1}{\overline{\nu}}\right)^{k}$ 

$$\frac{P}{RT} = \sum_{k=0}^{\infty} C_k(T) \left(\frac{1}{\overline{V}}\right)^k = \sum_{k=0}^{\infty} C_k(T) z^k = f(z;T)$$
with coefficient  $C_k(T) = \frac{1}{k!} \left(\frac{d^k f}{dz^k}\right)_{z=0}$ 

b. Why does the Van der Waals "a" only appear in C2(T)?

#### Van der Waals gas

	01 > Modules	
2020 Winter Quarter		
Home		
Discussions	<ul> <li>Homework Problems</li> </ul>	
Grades	@ HW1 Probs 1-8 W20-1.pdf	
People		
Files		
Syllabus	<ul> <li>Homework Solutions</li> </ul>	
Modules		
Conferences	<ul> <li>Sample Exams</li> </ul>	
Collaborations		

enough hellos ....

# and NOW TO BEGIN !!

# our thermodynamics trek







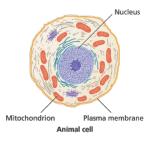


A thermodynamic **System** consists of all the materials involved in the process under study. This material could be the contents of an open beaker containing reagents, the electrolyte solution within an electrochemical cell, or the contents of a cylinder and movable piston assembly in an engine.

In thermodynamics, the rest of the universe is referred to as the **surroundings**.

system + surroundings = the **UNIVERSE** 

If a system can exchange matter with the surroundings, it is called an **open system**; if not, it is a **closed system**.





#### STATE VARIABLES:

properties whose values are required to specify the STATE of a system

•VOLUME: MEASURED WITH A RULER

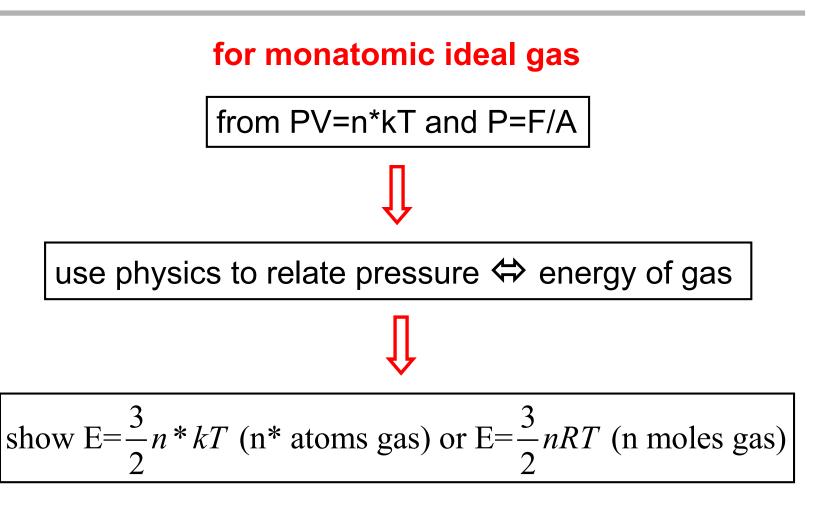


- •PRESSURE: FORCE/AREA (physics 5-6A)
- •TEMPERATURE: SEE IDEAL GAS THERMOMETER HANDOUT
- EQUATION of STATE: RELATES P, V, T *(more later)*

PV=nRTn=moles, R= gas constant
$$PV=(nN)\frac{R}{N}T$$
N=Avogadro's number  $\left[\frac{molecules}{mol}\right]$  $PV=n*kT$  $nN=n*=$  number of molecules $k=\frac{R}{N}$  Boltzmann's constant

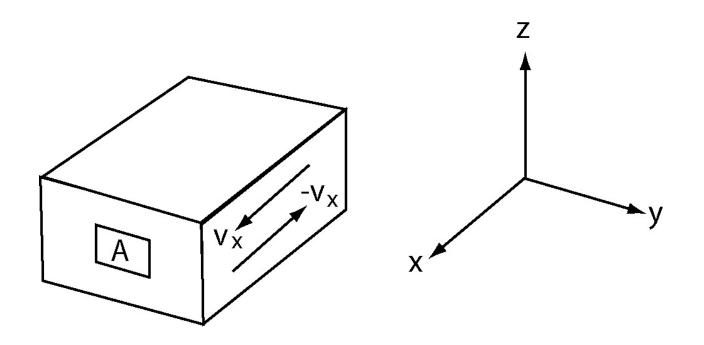
Fundamental and Defined Constants

Engel & Reid [front cover, Table 1.1 (p13<sub>4th</sub> [8]<sub>3rd</sub>), Table 1.2 (p13<sub>4th</sub>[9]<sub>3rd</sub>)] R= 8.3145 J mol<sup>-1</sup> K<sup>-1</sup> = .083145 L bar mol<sup>-1</sup> K<sup>-1</sup> = .082058 L atm mol<sup>-1</sup> K<sup>-1</sup> 0.986923 atm = 1 bar = 10<sup>5</sup> kg m<sup>-1</sup>s<sup>-2</sup> = 10<sup>5</sup> Pa (pascal) 1L=1 dm<sup>3</sup>=10<sup>-3</sup>m<sup>3</sup>



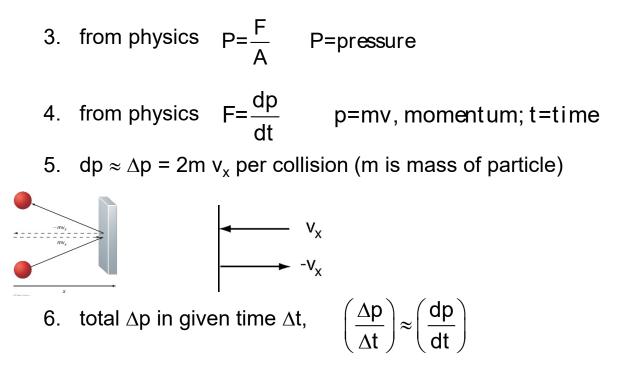
and thus for monatomic ideal gas E depends only on T !!! [in thermodynamic notation E ≡ U (internal energy)]





### RESULT: for ('monatomic') ideal gas (how) energy depends only on temperature

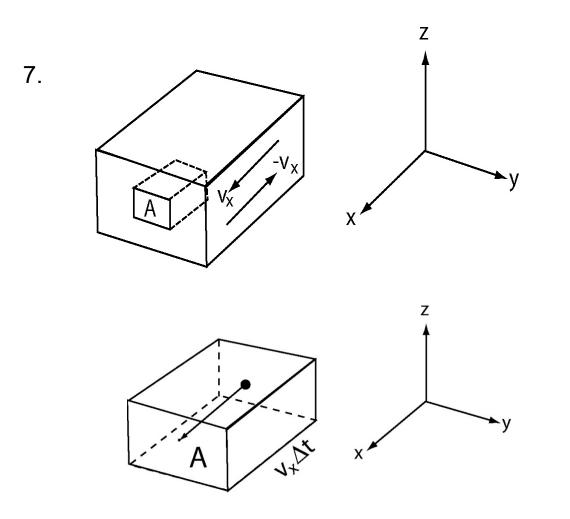
- 1. molecules all with same  $|v_x|$  (all same  $v_x$  is 'heuristic')
- 2. elastic collision with wall velocity of mass goes  $v_x \rightarrow v_x$



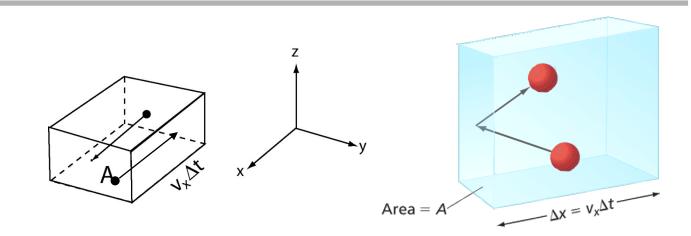
,.

would depend on number of collisions in that interval

#### heuristic derivation



#### heuristic derivation



8.  $\frac{n^*}{V}$  is density of molecules,  $Av_x \Delta t = V$  is volume of rectangular box, 9.  $\left(\frac{1}{2}\frac{n^*}{V}Av_x\Delta t\right)$  is total number of molecules colliding with area A in  $\Delta t$ 

10. total 
$$\Delta p = (2mv_x) \left(\frac{1}{2}\right) \left(\frac{n^*}{V}\right) (Av_x \Delta t) = (mv_x^2) \left(\frac{n^*}{V}\right) (A\Delta t)$$

11. after some algebra and equating

$$P = \frac{F}{A} = \frac{\Delta p}{A\Delta t} = \left(mv_x^2\right) \left(\frac{n^*}{V}\right) = \frac{n^*kT}{V}$$

$$P = \left(mv_x^2\right) \left(\frac{n^*}{V}\right) = \left(\frac{p^*}{V}\right) \frac{kT}{2}$$

$$\left(\frac{mv_x^2}{2}\right) = \frac{kT}{2}$$
 for each molecule of 1-D ideal gas

12. in **3D** with  $|v_x| = |v_y| = |v_z|$ 

total KE=
$$\left(\frac{1}{2}mv_x^2 + \frac{1}{2}mv_y^2 + \frac{1}{2}mv_z^2\right)n^* = \frac{3}{2}n^*kT = \frac{3}{2}nRT$$
  
$$\int \frac{1}{2}RT \text{ for each degree } (x, y, z) \text{ of 'classical freedom'}$$

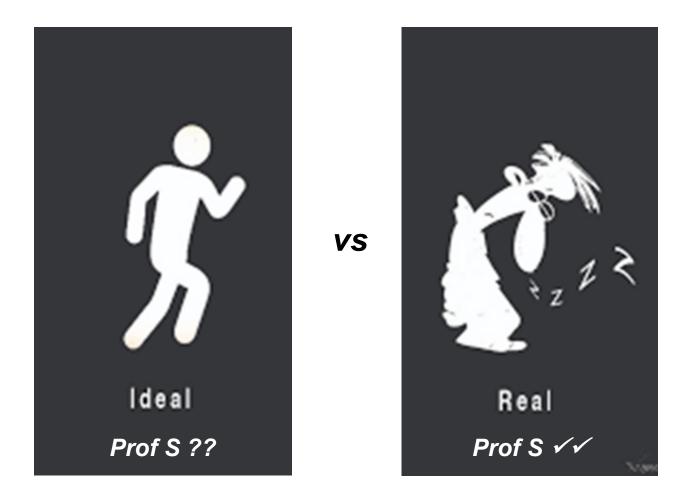
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- Good warm up of physics and equation derivation
- For a molecule with only kinetic energy (e.g. monatomic species), and ideal gas (no intermolecular forces)

$$E = \frac{3}{2}kT$$
 per molecule or  $E = \frac{3}{2}RT$  per mole

• For monatomic ideal gas, E is function of **Only T**;

T constant ⇔ E constant



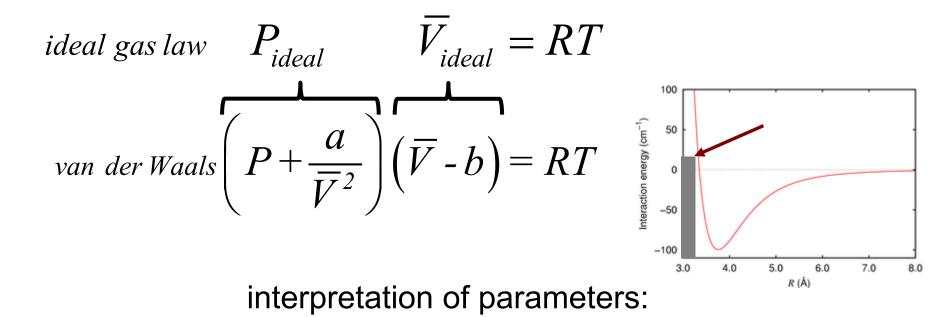
#### Table 1.2 Some commonly used equations of state

	Equation of State	Functional Form	Number of Parameters	
	Ideal gas	$PV_m = RT$ HW	#1 1	0
$\rightarrow$	van der Waals	$(V_m - b)(P + a/V_m^2) = RT$	<b>#1 2-3</b>	2
	Dieterici	$P(V_m - b)\exp[a/RTV_m] = RT$		2
	Berthelot	$(V_m - b)(P + a/TV_m^2) = RT$		2
-	Virial	$P = RT \left[ V_m^{-1} + \sum_{n=2}^{\infty} C_n(T) V_m^{-n} \right] \qquad \mathbf{H}$	W#1 *4	œ
	Beattie-Bridgman	$PV_m^2 = (1 - \gamma)RT(V_m + \beta) - \alpha,$		5
		with $\gamma = c_o/T^3 V_m$		
		$\beta = b_o[1 - b/V_m]$ , and		
		$\alpha = a_o[1 + a/V_m]$		
	Redlich-Kwong	$P = \frac{RT}{(V_m - b)} - \frac{a}{T^{1/2}V_m(V_m + b)}$		2
	Reichsanstalt	$PV = RT + AP + BP^2 + CP^3 + \cdots$		œ

## Some comments on the

# Van der Waals equation of state

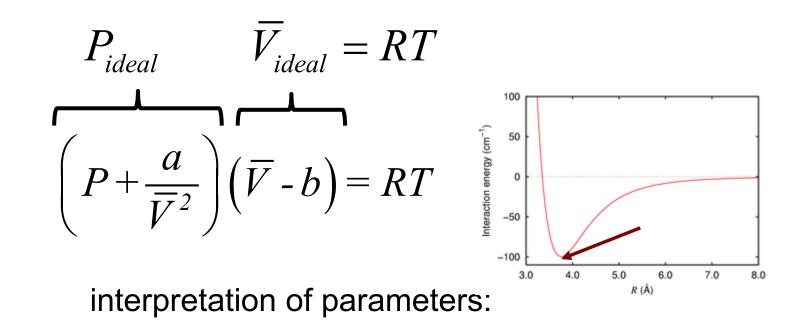
# van der Waals equation the parameter b



b is correction for actual volume of atoms/molecules

- volume available to molecules  $\left(\overline{V}-b
  ight)$  smaller than  $\ \overline{V}$
- b is associated with repulsive forces

## van der Waals equation the parameter a

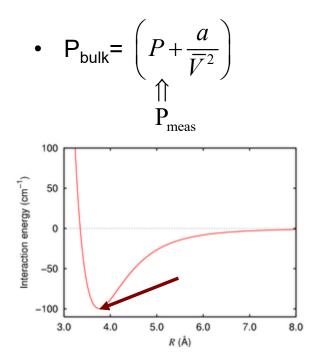


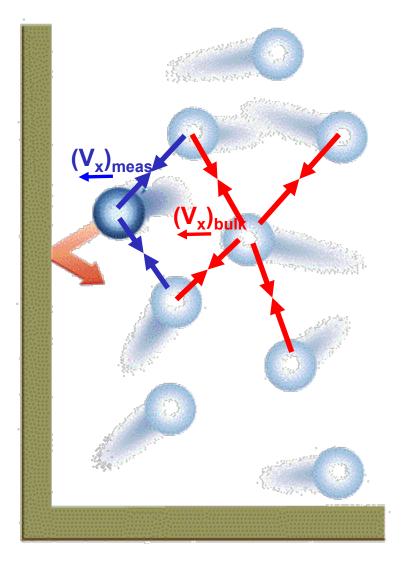
a is correction for attractive forces of atoms/molecules

- a is associated with attractive forces
- $P_{\text{bulk}} \equiv P_{\text{ideal}}$  is greater than  $P \equiv P_{\text{meas}}$  measured at surface •  $P_{\text{bulk}} = \left( P_{\text{meas}} + \frac{a}{\overline{V}^2} \right) \quad P_{\text{meas}} \to P_{\text{bulk}} \quad \overline{V} \to \infty$

#### heuristic justification for attractive constant a

- asymmetric attractive forces for molecule at surface
- molecule at surface has less momentum less than molecule in bulk
- P=Pmeas < Pbulk





#### van der Waals equation

$$\left(P+\frac{a}{\overline{V}^{2}}\right)\left(\overline{V}-b\right)=RT$$

Table 1.1 van der Waals parameters					
Gas	<b>b</b> (L mol <sup>-1</sup> )	$a (L^2 bar mol^{-2})$			
He	0.0238	0.0346			
Ne	0.01672	0.208			
Ar	0.03201	1.355			
Kr	0.0396	2.325			
Acetylene	0.0522	4.516			
$N_2$	0.0387	1.37			
H <sub>2</sub> 0	0.03049	5.537			
$CO_2$	0.04286	3.658			

Source: Handbook of Chemistry and Physics, 78th edition, CRC Press, Boca Raton, Fl, 1997–98

### van der Waals equation

$$\left(P+\frac{a}{\overline{V}^{2}}\right)\left(\overline{V}-b\right)=RT$$

Table 1.1	repulsive	pa attractive	
Gas	<b>b</b> ( <b>L mol</b> <sup>-1</sup> )	$a (L^2 bar mol^{-2})$	
He ?	0.0238	0.0346	
Ne	0.01672	0.208	polarizability
Ar size	0.03201	1.355	
Kr	0.0396	2.325	
Acetylene	0.0522	4.516	
$N_2$	0.0387	1.37	polarity
H <sub>2</sub> 0	0.03049	5.537	
$CO_2$	0.04286	3.658	

Source: Handbook of Chemistry and Physics, 78th edition, CRC Press, Boca Raton, Fl, 1997–98

# Validity

However, the Van der Waals model is not appropriate for rigorous quantitative calculations, remaining useful only for **teaching** and qualitative purposes.<sup>[1]</sup>

Nowadays, Eq. 2.9 belongs to **"pedagogical physics:"** it is the simplest equation that illustrates several important concepts, but its accuracy is not satisfactory.



- ✓ Introduction and Class Resources, etc.
- ✓ Careful definition of thermodynamic variables (*P*, *V*, *T*, etc)
- ✓ Ideal gas Energy Depends Only On Temperature (T)
- Van der Waals equation (example of equation of state for 'real' gas)

# End of Lecture 1

#### Table 1.2 Some commonly used equations of state

	Equation of State	Functional Form	Number of Parameters
$\rightarrow$	Ideal gas	$PV_m = RT$	0
	van der Waals	$(V_m - b)(P + a/V_m^2) = RT$	2
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	Berthelot	$(V_m - b)(P + a/TV_m^2) = RT$	2
	Virial	$P = RT \left[ V_m^{-1} + \sum_{n=2}^{\infty} C_n(T) V_m^{-n} \right]$	œ
	Beattie-Bridgman	$PV_m^2 = (1 - \gamma)RT(V_m + \beta) - \alpha,$	5
		with $\gamma = c_o/T^3 V_m$	
		$\beta = b_o[1 - b/V_m]$ , and	
		$\alpha = a_o[1 + a/V_m]$	
	Redlich-Kwong	$P = \frac{RT}{(V_m - b)} - \frac{a}{T^{1/2}V_m(V_m + b)}$	2
	Reichsanstalt	$PV = RT + AP + BP^2 + CP^3 + \cdots$	œ

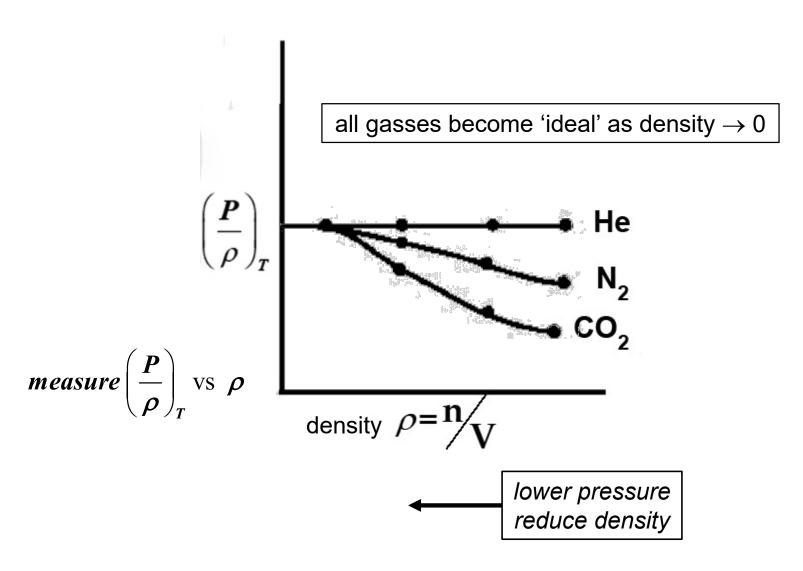
Previously the problem had been that  $N_2$  is a very stable molecule, and so most attempts to convert it to less stable molecules, such as  $NH_3$ , failed because of thermodynamic or entropy problems. The secret to the Haber-Bosch process proved to be a catalyst of iron with a small amount of aluminium added (aluminium was at the time an exotic and expensive metal that probably attracted Haber's attention as a novelty). The Haber-Bosch process operates at high pressure so as to shift the equilibrium to the right, and high temperature to increase the rates of the reaction. Of course, operating at high temperature actually shifted the reaction to the left, but the trade-off for faster rates was accepted. By removing the ammonia as liquid ammonia, the equilibrium is continuously shifted to the right.

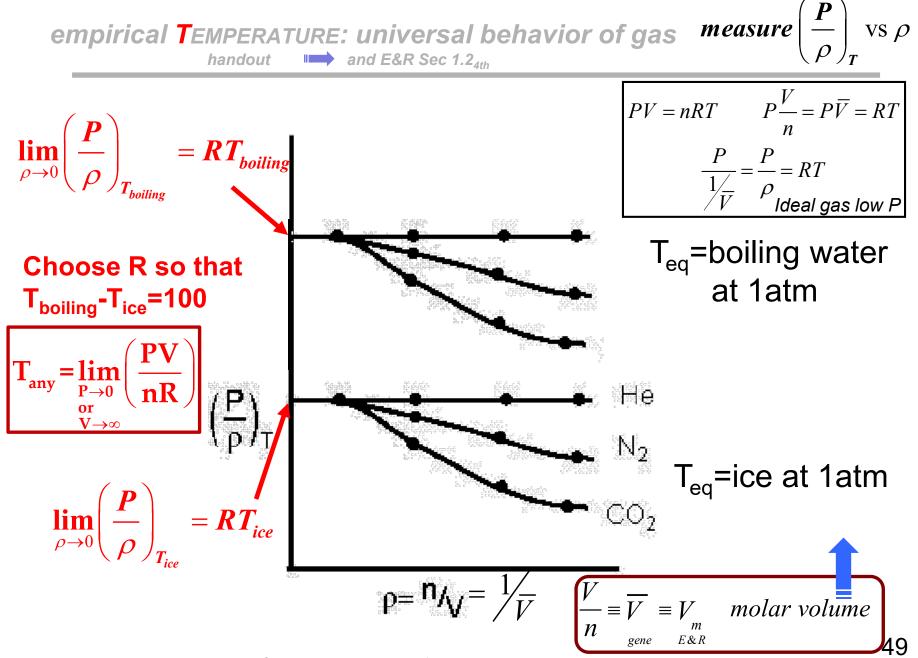
#### heu·ris·tic [hyoo-ris-tik or, often, yoo-] adjective

**1.** serving to indicate or point out; stimulating interest as a means of furthering investigation.









[n.b. curves for various gasses are 'cartoons' but actual data would converge to limit]