## Chemistry 163B Thermodynamics Winter 2020

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#### Menu: for TODAY



- · Introduction and Class Resources, etc.
- Careful definition of thermodynamic variables (P, V, T, etc)
- Ideal gas Energy Depends Only On Temperature (derivation)
- Van der Waals equation (example of equation of state for 'real' gas)

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Thermodynamics is a really beautiful scientific story!!

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"rules" of science

observations

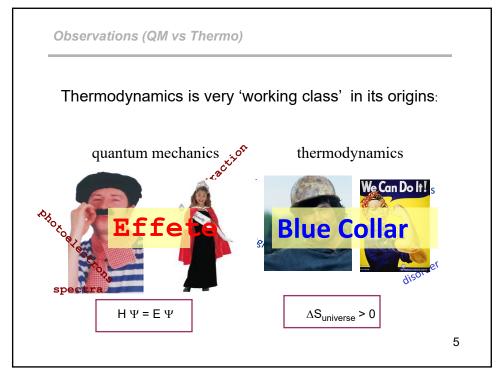


• guiding principles



 predictions and applications based on principles

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#### observations: thermo ≡ heat

- Count Rumford, 1799
- observed water turning into steam when canon barrel was bored
- work ⇔ heat

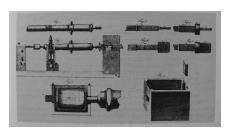
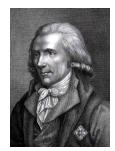


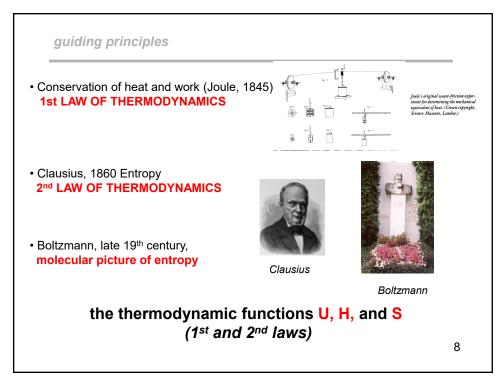
FIGURE 11. An illustration from Rumford's paper, "An Inquiry Concerning the Source of the Heat Which is Excited by Firction," showing the apparatus used by him in the cannon boring experiment. Figure 1, upper left, shows the cannon as received from the foundry, and Figure 2, below, shows it mounted in the machine used for boring. (Reproduced with the permission of Harvard University Press.)



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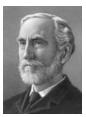


"Applications"

U,H,S,G

How does knowledge about efficiencies of steam engines, mechanical systems, etc, relate to processes in chemical, biological, and geological systems?

#### **ANSWERED BY:**

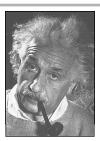


J. W. Gibbs- arguably the frist great American scientist who combined the concepts of heat and entropy and proposed "[Gibbs] Free Energy", **G**, a thermodynamic state function that leads to a whole spectrum of applications

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from: Einstein's "Autobiographical Notes"



A theory

is the more impressive the greater the simplicity of its premises, the more different kinds of things it relates, and the more extended its area of applicability. Hence the deep impression that classical thermodynamics made upon me. It is the only physical theory of universal content concerning which I am convinced that, within the framework of the applicability of its basic concepts, it will never be overthrown (for the special attention of those who are skeptics on principle).

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types of problems that thermodynamics addresses (reactions)

#### might

1. Under what conditions will a reaction occur?

**EXAMPLE:** 

C (graphite) → C (diamond) 1 atm 398K

nada

30,000 -100,000 atm 1000 K - 3000 K

¡Hurra!

1st artificially produced diamonds, 1954 at General Electric Labs



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types of problems that thermodynamics addresses (equilibria)

2. How far will a reaction proceed (given enough time)? How do the thermal and entropic properties determine EQUILIBRIUM? How do the EQUILIBRIUM conditions depend on T,P?



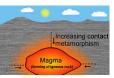
 $N_2(g) + 3H_2(g) \leftrightarrows 2NH_3(g)$ 

what are best T,P for NH<sub>3</sub> products?









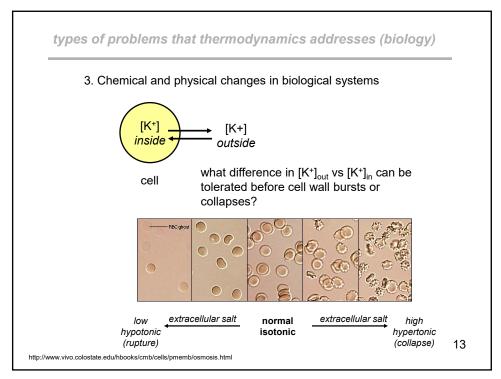
 $SiO_2 + CaCO_3 \leftrightarrows CaO \cdot SiO_2 + CO_2 (g)$ quartz calcite wollastonite

geologic thermometer:

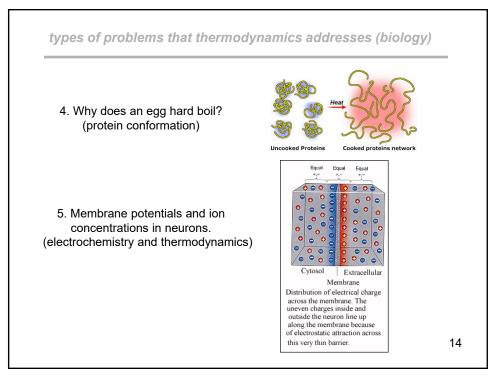
The fraction of wollastonite in a rock sample can be used to estimate the temperature at which the rock metamorphosis occurred [the T at which the equilibrium was rapidly frozen]

**Geologic Thermometer** 

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types of problems that thermodynamics addresses (ecology)

6. Thermodynamic feasibility of SO<sub>2</sub> removal

 $SO_2(g) \leftrightarrows S(s) + O_2(g)$ 



http://healthandenergy.com/images/magnitka%20smoke%20stacks.jpg

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#### what thermodynamics can't answer

- 1. How fast a reaction proceeds (kinetics, catalysts, enzymes; in chem 103, BMB 100, chem 163C)
- 2. Macroscopic thermodynamics does not prove or require hypotheses about molecular structure; however we will use our knowledge of molecular structure to get an atomic "picture" of thermodynamic processes. The quantitative connection is made by statistical thermodynamics:

chem 163A ⇔ chem 163B chem 163C

3. Although in chemistry 163B we will study how thermodynamics put limits on processes at equilibrium, there exists a whole other field of *non-equilibrium thermodynamics*.

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#### aims of class

- 1. Clear conceptual picture of thermodynamics
- 2. Ability to relate and apply thermodynamics to chemical and biological systems
- 3. PROBLEM SOLVING: Chemistry + Logic + Mathematics
- 4. How to do independent and advanced reading/research in areas that utilize thermodynamics.
- 5. THE GRAND PICTURE of how thermodynamics and quantum mechanics fit into our picture of 'nature'.
- 6. Advanced mathematical techniques

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#### class administration

www.chemistry.ucsc.edu  $\Rightarrow$  course pages  $\Rightarrow$  Chemistry 163B

http://switkes.chemistry.ucsc.edu/teaching/CHEM163B/

- lectures: A MUST
- homework: A MUST
- sections: required (A MUST)



• midterms: 31st January

28th February

• final: 19<sup>th</sup> March, 4:00-7:00 PM

(last class 13th March)

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Thermodynamic

#### **Learn Thermodynamics**

- Lectures
- Sections (start Monday, Jan 13; HW#1 Probs 1-8)
- Tutorial Event (starts TOMORROW Tues, Jan 7, HW#1 Probs1-2)
- Office hours (start TODAY Mon, Jan 6)
- LSS Tutor



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#### first Tutorial Tuesday 7th January, NS Annex 102, 5:25PM-6:30PM Chemistry 16. Comments on Mathematical Techniques for Chemistry 163B Homework Problems Our text (EAR: ME2, pp 17-28, ME3, pp 63-68) [Appendix 8 2 + 8 2,3]s, contains testilated information on the aspects of differential and integral calculus relevant to our study of thermodynamics. We will review these techniques in the context of class derivations and homework problems, rather than just as abstract mathematical exercises. However it is useful to categorize them below. In your first discussion section the TAs will also comment on the techniques. 1. For an ideal gas $P\overline{V} = RT$ $(\overline{V} = V_R = \frac{V}{n})$ molar volume) evaluate: d. $\left(\frac{\partial P}{\partial \overline{V}}\right)_T \left(\frac{\partial \overline{V}}{\partial T}\right)_P \left(\frac{\partial T}{\partial P}\right)_P$ You should have "at hand" the derivatives and integrals of functions like: x<sup>n</sup>, x<sup>n</sup>, ln (x), e<sup>ax</sup>, sin ax, cos ax ["at hand" = in your accessible neurons] e. One can often get, via the chain rule for differentiation, rigorous results by "canceling $\partial's$ " . However the correct result for part d is $\mbox{\bf NOT}$ what Differential expressions (E&R 2.8; pp 39-41, 63 )/ pp 28, 45-49/2m one would obtain by just "canceling $\partial 's$ " in the numerators and denominators in each of the three terms. Why for part d can one NOT a. $d\psi$ is inexact differential if $\int\limits_{-\infty}^{\infty} d\psi$ depends on the path apply the chain rule to get $\left(\frac{\partial P}{\partial P}\right)$ = 1? [NOTE: you may evaluate part d from initial $\to$ final This implies there is no "underlying" well behaved, function $\psi$ that changes like $d\!\!/\psi$ and e using the specific results from a, b, c for an ideal gas. However the correct result is a more general relationship for any well behaved function z(x,y)] b. $d\psi$ is exact differential if $\int\limits_{-\infty}^{\delta nd} d\psi$ does not depend on the path from initial → final 2. For a Van der Waals gas: $\left(P + \frac{a}{\overline{V}^2}\right) (\overline{V} - b) = RT$ evaluate: Implications that arise from $\mathit{d}\,\psi$ being an exact differential: a. $\left(\frac{\partial P}{\partial \overline{V}}\right)_T$ b. $\left(\frac{\partial^2 P}{\partial \overline{V}^2}\right)_T$ a. There is a well behaved function $\psi$ whose change is described by $d\psi$ b. $d\psi$ $(V, \mathcal{I}) = \left(\frac{\partial \psi}{\partial V}\right)_{\mathcal{I}} dV + \left(\frac{\partial \psi}{\partial T}\right)_{\mathcal{F}} dT$ C. $\left(\frac{\partial P}{\partial T}\right)_{p}$ or in more general notation $d \psi (x, y, z) = \begin{pmatrix} \frac{\partial \psi}{\partial x} \end{pmatrix}_{y, z} dx + \begin{pmatrix} \frac{\partial \psi}{\partial y} \end{pmatrix}_{x, y} dy + \begin{pmatrix} \frac{\partial \psi}{\partial z} \end{pmatrix}_{x, y} dz$ e. $\left[\frac{\partial}{\partial \overline{V}} \left(\frac{\partial P}{\partial T}\right)_{p}\right]_{p}$ c. ∮dψ = 0 (integral for any cyclic path; i.e. the initial and final states are identical) f. How do the results of parts d and e compare? Why is this? d. $\int_{0}^{fond} d\psi = \psi(final) - \psi(initial)$

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Chemistry 163B

#### Tutorial Tuesday 7th January

**Homework Problems** (#1-#8)

**1.** For an ideal gas  $P\overline{V} = RT$   $(\overline{V} \equiv V_m \equiv \frac{V}{n}$  molar volume) evaluate:

- $\mathrm{d.} \quad \left(\frac{\partial P}{\partial \, \overline{\mathcal{V}}}\right)_{\!T} \! \left(\frac{\partial \, \overline{\mathcal{V}}}{\partial \, T}\right)_{\!p} \! \left(\frac{\partial \, T}{\partial P}\right)_{\!p}$

**2.** For a Van der Waals gas:  $\left(P + \frac{a}{\overline{V}^2}\right) \left(\overline{V} - b\right) = RT$  evaluate:

- $\begin{array}{lll} \text{a.} & \left(\frac{\partial P}{\partial \overline{V}}\right)_{\!\!T} & & \text{b.} & \left(\frac{\partial^2 P}{\partial \overline{V}^2}\right)_{\!\!T} \\ \text{c.} & \left(\frac{\partial P}{\partial T}\right)_{\!\!F} & & \text{d.} & \left[\frac{\partial}{\partial T}\left(\frac{\partial P}{\partial \overline{V}}\right)_{\!\!T}\right]_{\!\!F} \end{array}$
- e.  $\left[\frac{\partial}{\partial \bar{V}} \left(\frac{\partial P}{\partial T}\right)_{\bar{V}}\right]_{\bar{V}}$

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Winter 2020

Chemistry 163B

3. Engel & Reid problem P1.38 (4th edition)

#### to HW#1 listing on CANVAS

Van der Waals gas

★4. (optional) The Van der Waals and virial expressions are two commonly used equations of state as approximations to real gas behavior:

$$P = \frac{RT}{(\overline{V} - b)} - \frac{a}{\overline{V}^2} \quad \textit{Van der Waals}$$

$$P = RT \left[ \frac{C_1(T)}{\overline{V}} + \frac{C_2(T)}{\overline{V}^2} + \frac{C_3(T)}{\overline{V}^3} \dots + \frac{C_n(T)}{\overline{V}^n} \dots \right] \quad virial$$

a. Show that the first three virial coefficients are related to the Van der Waals parameters a and b in the following way:

 $C_1(T)=1$ 

 $C_2(T)=b-a/RT$ 

 $C_3(T)=b^2$ 

note that the virial expansion is just a Taylor (Maclaurin) series in  $z^k = \left(\frac{1}{\overline{p}}\right)^k$ 

$$\frac{P}{RT} = \sum_{k=0}^{\infty} C_k \left(T\right) \left(\frac{1}{\overline{V}}\right)^k = \sum_{k=0}^{\infty} C_k \left(T\right) z^k = f(z;T)$$

with coefficient  $C_k(T) = \frac{1}{k!} \left( \frac{d^k f}{dz^k} \right)$ 

b. Why does the Van der Waals "a" only appear in  $C_2(T)$ ?

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#### enough hellos ....

#### and NOW TO BEGIN!!

#### our thermodynamics trek







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system and surroundings (careful definitions) E&R<sub>4th</sub> sec 1.3



A thermodynamic **system** consists of all the materials involved in the process under study. This material could be the contents of an open beaker containing reagents, the electrolyte solution within an electrochemical cell, or the contents of a cylinder and movable piston assembly in an engine.

In thermodynamics, the rest of the universe is referred to as the surroundings.

system + surroundings = the UNIVERSE

If a system can exchange matter with the surroundings, it is called an open system; if not, it is a **closed system**.



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Variables of state: V, T, P (careful definitions)



#### STATE VARIABLES:

properties whose values are required to specify the STATE of a system

•VOLUME: MEASURED WITH A RULER



•PRESSURE: FORCE/AREA (physics 5-6A)

•TEMPERATURE: SEE IDEAL GAS THERMOMETER HANDOUT

• EQUATION of

STATE: RELATES P, V, T

(more later)



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Pressure, Kinetic Energy, and Temperature

**SEE HANDOUT** 

PV=nRT n=moles, R= gas constant

$$PV = (nN) \frac{R}{N} T$$
  $N = Avogadro's number \left[ \frac{molecules}{mol} \right]$ 

$$PV=n*kT$$
  $nN=n*=$  number of molecules

$$k = \frac{R}{N}$$
 Boltzmann's constant

Fundamental and Defined Constants

Engel & Reid  $\,$  [front cover, Table 1.1 (p13 $_{4th}$  [8] $_{3nd}$ ), Table 1.2 (p13 $_{4th}$ [9] $_{3nd}$ )]

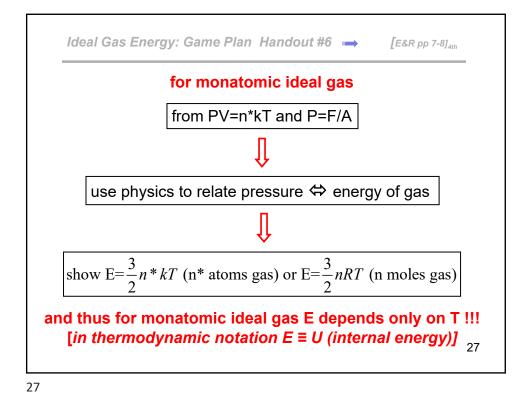
 $R = 8.3145 \text{ J mol}^{-1} \text{ K}^{-1}$ 

 $= .083145 \text{ L bar mol}^{-1} \text{ K}^{-1}$ 

= .082058 L atm mol  $^{\text{-1}}$  K  $^{\text{-1}}$ 

 $0.986923 \text{ atm} = 1 \text{ bar} = 10^5 \text{ kg m}^{-1}\text{s}^2 = 10^5 \text{ Pa}$  (pascal)  $1L=1 \text{ dm}^3=10^{-3}\text{m}^3$ 

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RESULT: for ('monatomic') ideal gas [new persult]

Result: for ('monatomic') ideal gas (how) energy depends only on temperature

#### heuristic derivation

- 1. molecules all with same  $|v_x|$  (all same  $v_x$  is 'heuristic')
- 2. elastic collision with wall velocity of mass goes  $v_x \rightarrow v_x$
- 3. from physics  $P = \frac{F}{A}$  P = pressure
- 4. from physics  $F = \frac{dp}{dt}$  p = mv, momentum; t = time
- 5.  $dp \approx \Delta p = 2m v_x$  per collision (m is mass of particle)





6. total  $\Delta p$  in given time  $\Delta t$ ,  $\left(\frac{\Delta p}{\Delta t}\right) \approx \left(\frac{dp}{dt}\right)$ 

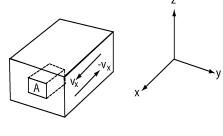
would depend on number of collisions in that interval

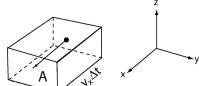
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#### heuristic derivation

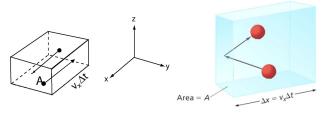
7.





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#### heuristic derivation



- 8.  $\frac{n^*}{V}$  is density of molecules,  $Av_x \Delta t = V$  is volume of rectangular box,
- 9.  $\sqrt{\frac{1}{2}} \frac{n^*}{V} A_{V_x} \Delta t$  is total number of molecules colliding with area A in  $\Delta t$

10. total 
$$\Delta p = (2mv_x) \left(\frac{1}{2}\right) \left(\frac{n^*}{V}\right) (Av_x \Delta t) = (mv_x^2) \left(\frac{n^*}{V}\right) (A\Delta t)$$

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ES2

#### heuristic derivation

11. after some algebra and equating

$$\begin{split} P &= \frac{F}{A} = \frac{\Delta p}{A\Delta t} = \left(mv_x^2\right) \left(\frac{n^*}{V}\right) = \frac{n^*kT}{V} \\ P &= \left(\frac{mv_x^2}{2}\right) \left(\frac{n^*}{V}\right) = \left(\frac{p^*}{V}\right) \frac{kT}{2} \\ \left(\frac{mv_x^2}{2}\right) = \frac{kT}{2} \quad \text{for each molecule of 1-D ideal gas} \end{split}$$

12. in 3D with  $|v_X| = |v_Y| = |v_Z|$ 

total KE=
$$\left(\frac{1}{2}mv_x^2 + \frac{1}{2}mv_y^2 + \frac{1}{2}mv_z^2\right)n^* = \frac{3}{2}n^*kT = \frac{3}{2}nRT$$

$$\frac{1}{2}RT \text{ for each deg ree }(x,y,z) \text{ of 'classical freedom'}$$

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**ES2** Eugene Switkes, 1/6/2020

TAKE HOME MESSAGES

- · Good warm up of physics and equation derivation
- For a molecule with only kinetic energy (e.g. monatomic species), and ideal gas (no intermolecular forces)

$$E = \frac{3}{2}kT$$
 per molecule or  $E = \frac{3}{2}RT$  per mole

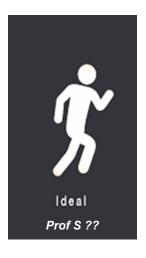
- For monatomic ideal gas, E is function of  $\boldsymbol{only}\;\boldsymbol{T};$ 

T constant ⇔ E constant

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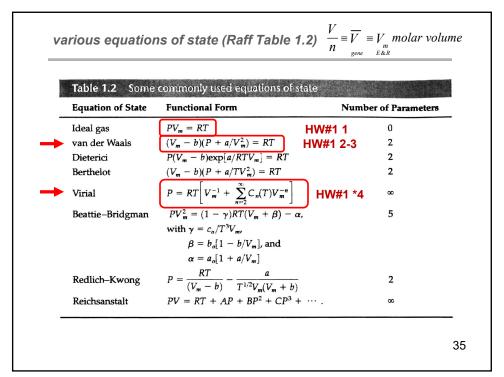
beyond PV=nRT: 'real' gases and equations of state (E&R sec 1.5)



v



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Some comments on the

Van der Waals equation of state

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#### van der Waals equation the parameter b

interpretation of parameters:

b is correction for actual volume of atoms/molecules

- volume available to molecules  $\left(\overline{V}-b\right)$  smaller than  $\ \overline{V}$
- b is associated with repulsive forces

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#### van der Waals equation the parameter a

$$P_{ideal} \qquad \overline{V}_{ideal} = RT$$

$$\left(P + \frac{a}{\overline{V}^2}\right)(\overline{V} - b) = RT$$

$$\frac{100}{100}$$

interpretation of parameters:

- a is correction for attractive forces of atoms/molecules
  - · a is associated with attractive forces
  - $P_{bulk} \equiv P_{ideal}$  is greater than  $P \equiv P_{meas}$  measured at surface

$$\bullet \quad \mathsf{P}_{\mathsf{bulk}} \! = \! \left( P_{\mathit{meas}} + \frac{a}{\overline{V}^{\, 2}} \right) \quad P_{\mathit{meas}} \to P_{\mathit{bulk}} \quad \overline{V} \to \infty$$

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# • asymmetric attractive forces for molecule at surface • molecule at surface has less momentum less than molecule in bulk • $P \equiv P_{meas} < P_{bulk}$ • $P_{bulk} = \left(P + \frac{a}{\overline{V}^2}\right)$ • $P_{meas}$

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#### van der Waals equation

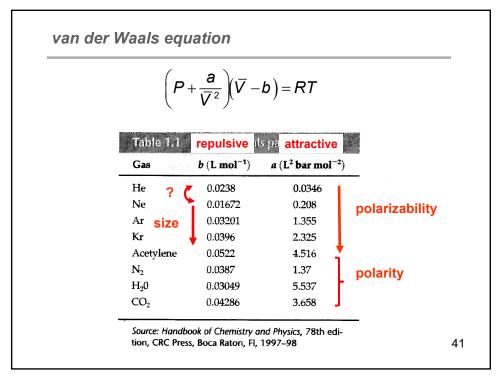
$$\left(P + \frac{a}{\overline{V}^2}\right)(\overline{V} - b) = RT$$

Gas	b (L mol <sup>-1</sup> )	a (L² bar mol <sup>-2</sup>
U48	v(L moi )	u (L. Dar moi -)
He	0.0238	0.0346
Ne	0.01672	0.208
Ar	0.03201	1.355
Kr	0.0396	2.325
Acetylene	0.0522	4.516
$N_2$	0.0387	1.37
$H_20$	0.03049	5.537
$CO_2$	0.04286	3.658

Source: Handbook of Chemistry and Physics, 78th edition, CRC Press, Boca Raton, Fl, 1997–98

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some trash talk on VDW eqn: inaccurate but instructive !!! (from other texts)

#### **Validity**

However, the Van der Waals model is not appropriate for rigorous quantitative calculations, remaining useful only for **teaching** and qualitative purposes.<sup>[1]</sup>

Nowadays, Eq. 2.9 belongs to "pedagogical physics:" it is the simplest equation that illustrates several important concepts, but its accuracy is not satisfactory.

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Menu: for TODAY



- ✓ Introduction and Class Resources, etc.
- ✓ Careful definition of thermodynamic variables (P, V, T, etc)
- ✓ Ideal gas Energy Depends Only On Temperature (T)
- ✓ Van der Waals equation (example of equation of state for 'real' gas)

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## End of Lecture 1

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Table 1.2 Some	commonly used equations of state	
Equation of State	Functional Form	Number of Parameters
Ideal gas	$PV_m = RT$	0
van der Waals	$(V_m - b)(P + a/V_m^2) = RT$	2
Dieterici	$P(V_m - b)\exp[a/RTV_m] = RT$	2
Berthelot	$(V_m - b)(P + a/TV_m^2) = RT$	2
Virial	$P = RT \left[ V_m^{-1} + \sum_{n=2}^{\infty} C_n(T) V_m^{-n} \right]$	<b>∞</b>
Beattie-Bridgman	$PV_m^2 = (1 - \gamma)RT(V_m + \beta) - \alpha,$	5
	with $\gamma = c_o/T^3 V_m$ , $\beta = b_o[1 - b/V_m]$ , and $\alpha = a_o[1 + a/V_m]$	
Redlich-Kwong	$P = \frac{RT}{(V_m - b)} - \frac{a}{T^{1/2}V_m(V_m + b)}$	2
Reichsanstalt	$PV = RT + AP + BP^2 + CP^3 + \cdots$	œ

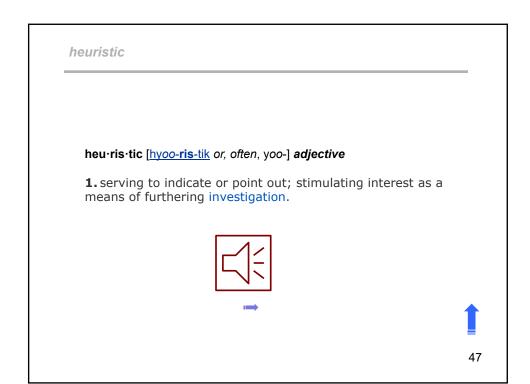
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#### The Haber Process (thermodynamics and kinetics)

Previously the problem had been that N<sub>2</sub> is a very stable molecule, and so most attempts to convert it to less stable molecules, such as NH<sub>3</sub>, failed because of thermodynamic or entropy problems. The secret to the Haber-Bosch process proved to be a catalyst of iron with a small amount of aluminium added (aluminium was at the time an exotic and expensive metal that probably attracted Haber's attention as a novelty). The Haber-Bosch process operates at high pressure so as to shift the equilibrium to the right, and high temperature to increase the rates of the reaction. Of course, operating at high temperature actually shifted the reaction to the left, but the trade-off for faster rates was accepted. By removing the ammonia as liquid ammonia, the equilibrium is continuously shifted to the right.



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