## Chemistry 163B Winter 2020

## Lectures 2-3

Heat and Work



- Heat (q), Work (w) and the First Law of Thermodynamics ∆U≡q+w
- Example calculations of q, w, U for reversible and irreversible expansions of ideal gas (comparisons and 'take home messages')
- Molecular picture of heat and work energy transfers

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7 Results

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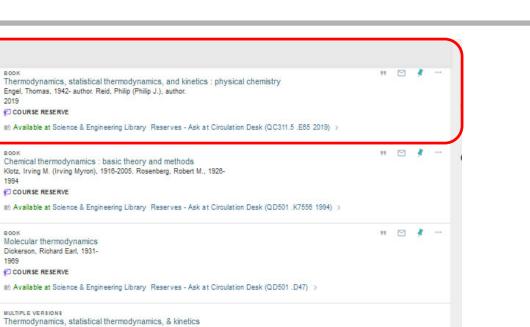
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• df is 'differential' representing an infinitesimal change

• **to calculate** 
$$\Delta f$$
 a finite change  $\Delta f = \int_{initial}^{final} df$ 

 if *f* is a state function, the integral around a closed (cyclic) path (finish=start) is

$$\oint df = \mathbf{0}$$



• if the 'system' goes from one state to another by differing paths





• the change in some aspect of the system can either be

independent of the path taken
 (depends only on the initial and final values of the state variables)
 Or
 depend on the path taken

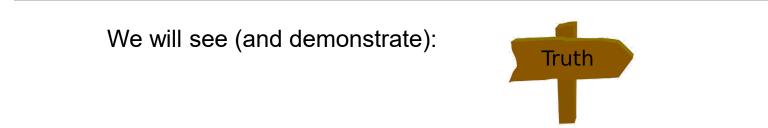
• if change is path **independent**  $\Rightarrow$  exact differential,

there is underlying **STATE FUNCTION** 

 if change is path dependent ⇒ inexact differential, no underlying property of the state of system

more in Lecture #5 (math !!)

all transfers of energy can be classified as heat (q) or work (w)



- heat (q) and work (w) are NOT PROPERTIES of a system but correspond to TRANSFERS of energy into (+)<sub>sys</sub> or out of (-)<sub>sys</sub> the system [e.g. there is no underlying property "heat" of a system"]
- when a system goes from an initial to a final state,
   e.g. (P<sub>i</sub>, V<sub>i</sub>, T<sub>i</sub>) ⇒ (P<sub>f</sub>, V<sub>f</sub>, T<sub>f</sub>) the values of **q** and **w** will **DEPEND ON THE PATH** taken between the states
- a small changes in a **path-dependent** quantities are **INEXACT DIFFERENTIALS** indicated by e.g.dq and dw

the FIRST LAW of thermodynamics

- U is symbol for INTERNAL ENERGY of a system
- $\Delta U = q + w + \chi$ ;  $dU = dq + dw + \sum_{i=1}^{n} dn_i$
- dn<sub>i</sub>=0 closed system, *ignore for now*
- $\Delta U_{sys} = -\Delta U_{surr}$  (conservation of energy)
- U is state function
- **∆U does not depend on path** (only on initial and final states)
- dU is an exact differential

equivalent statements



heat capacity (E&R section 2.11)<sub>[4th]</sub>

• 
$$\frac{d^{-}q}{dT} = C$$
 heat capacity  $\begin{bmatrix} J \ K^{-1} \end{bmatrix}$  extensive

the amount (transfer) of heat required to raise substance 1K

• 
$$\frac{d^{-1}q}{dT} = n\overline{C}$$
 molar heat capacity  $[J \mod^{-1} K^{-1}]$  intensive

the amount (transfer) of heat requires to raise 1 mol substance 1K

*C̄ generally depends on T and conditions* for example ideal monatomic gas

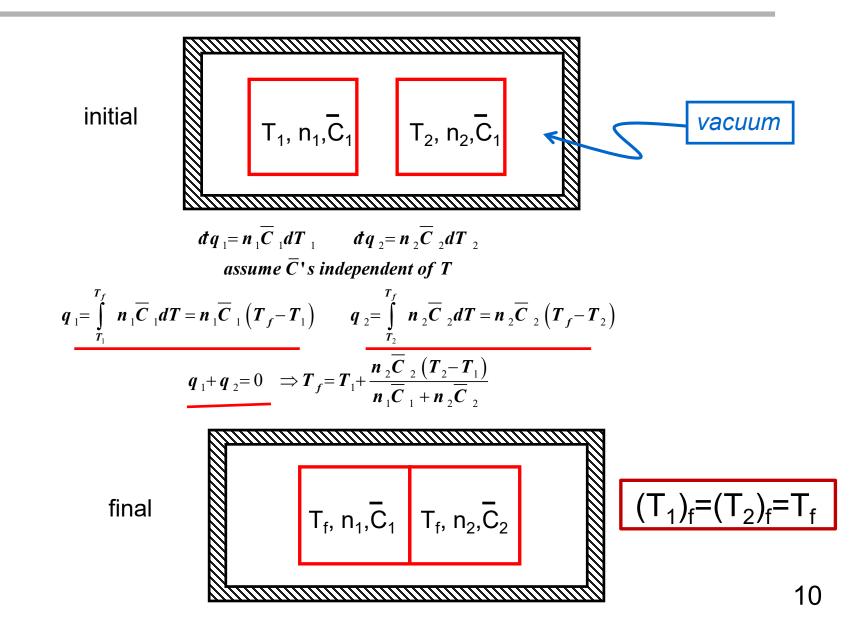
molar heat capacity at constant volume  $\overline{C}_V = \frac{3}{2}R$ molar heat capacity at constant pressure  $\overline{C}_P = \frac{5}{2}R$ 

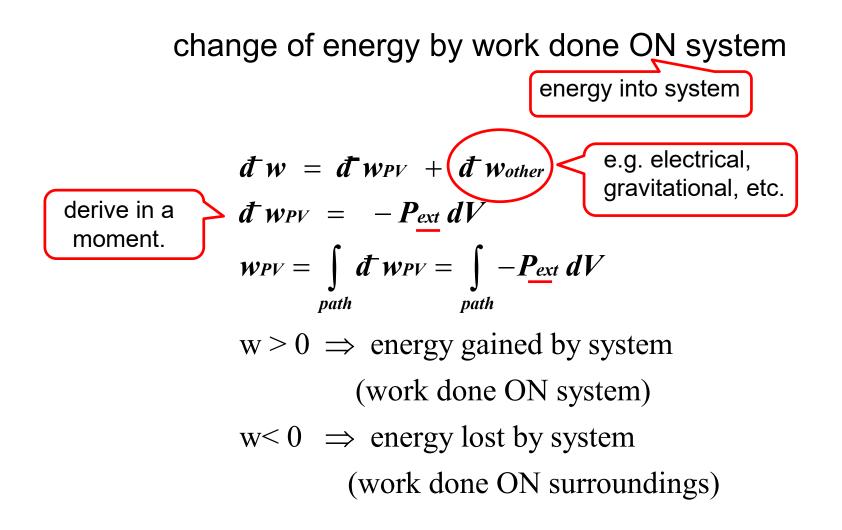
 $E = \frac{3}{2} nRT (true!!)$  but why does it take more heat to raise T at constant P than at constant V ??

change of energy by heat transfer

- $\overline{d} q = C dT = n \overline{C} dT$  (*C* is extensive,  $q = \int_{path} \overline{d} q = \int_{path} n \overline{C} dT$  (*C* is intensive)
- *C* will generally depend on T and path (*i.e. conditions*)
- q > 0 ⇒ energy (heat) gained by system cools surroundings
- q < 0 ⇒ energy (heat) lost by system (exothermic) warms surroundings

#### heat only transfer; thermal equibrium (also zeroth law; E&R p11) [4th]



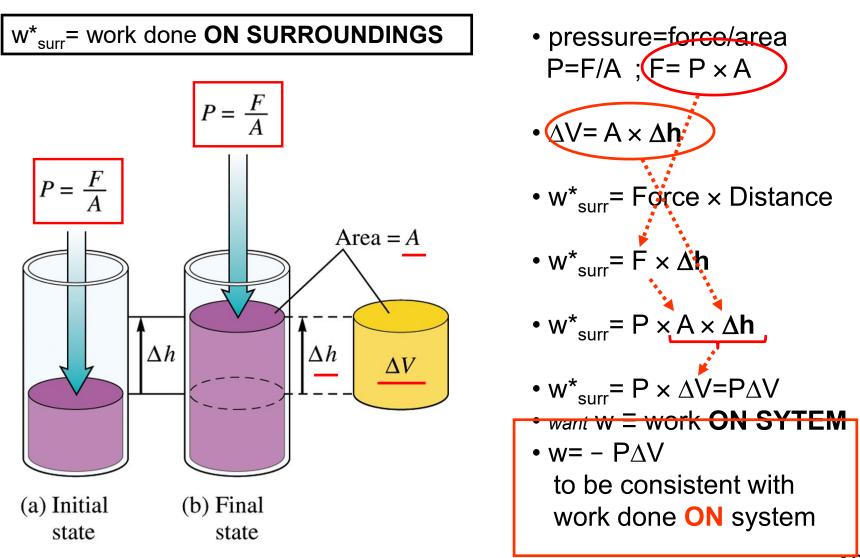


<ul> <li>isolated</li> </ul>	q=0; w=0
<ul> <li>isothermal</li> </ul>	⊿T=0
<ul> <li>adiabatic</li> </ul>	q=0

- "against constant pressure"
   P<sub>ext</sub>= const
- reversible process P<sub>int</sub>= P<sub>ext</sub>

   a (ideal) process that proceeds so slowly that an infinitesimal change of conditions causes the process to proceed in the opposite (reverse) direction
- irreversible process

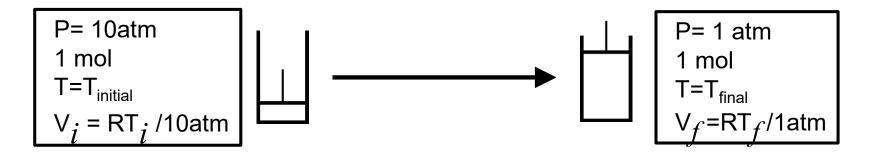
all other (real) processes proceeding at finite rate



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## for **IDEAL GAS**

- U(≡E) depends ONLY on T (ideal gas, previous class)
- isothermal,  $\Delta T=0$ ,
  - ΔU=0=q+w (ideal gas)
  - q=-w
- adiabatic: q=0, ΔU=w (in general)
- monatomic ideal gas
  - U = (3/2) n RT
  - $C_V = (3/2) n R$  (~ prove later)
  - C<sub>P</sub>= (5/2) n R (prove later)



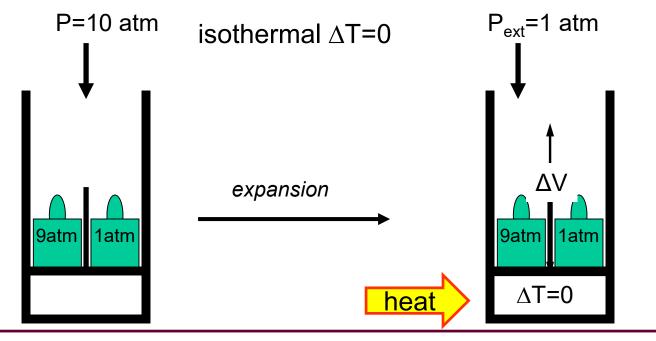
- isothermal against constant P<sub>ext</sub>
- adiabatic against constant P<sub>ext</sub>
- isothermal reversible
- adiabatic reversible (later)

#### why ??

- understanding of thermodynamic conditions
- how to calculate  $w=-\int Pdv$
- compare w<sub>rev</sub> vs w<sub>irrev</sub>
- AND lots of 'rewards' on HW and EXAMS

system is gas inside piston; weights are surrounding gainst

Pres



isothermal expansion against constant pressure (irreversible)

•system is piston and gas inside; weights represent external pressure of surroundings

- $P_{ext}$ =1atm (during volume change) ;  $\Delta V_{sys} > 0$ ;  $w_{sys}$ =  $P \Delta V_{sys} < 0$
- work (<0) is done **BY SYSTEM ON SURROUNDINGS** (1 atm weight lifted)
- E for ideal gas depends only on T isothermal ideal gas ΔT=0 ⇒ ΔU=0 since w< 0; q= -w > 0; heat absorbed by system

gainst system is gas inside piston; weights are surrounding

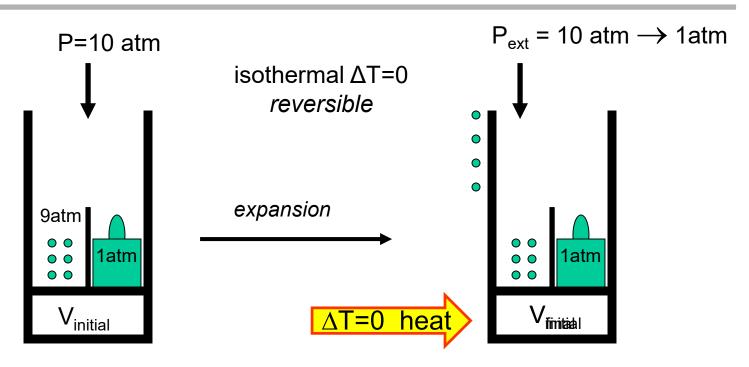
Pres

adiabatic q=0 P=10 atm P<sub>ext</sub>=1 atm 9atm 1atm adiabatic  $\Lambda V$ expansion 9atm 1atm

adiabatic expansion against constant pressure (irreversible)

- system is piston and gas inside; weights represent external pressure of surroundings
- $P_{ext}$ =1atm (during volume change);  $\Delta V_{sys} > 0$ ;  $W_{sys}$ =  $P_{ext} \Delta V_{sys} < 0$  work (<0) is done **BY SYSTEM ON SURROUNDINGS** (1 atm weight lifted)
- w< 0; q=0 (adiabatic); E<sub>sys</sub>(≡U<sub>sys</sub>)< 0; energy (potential) of surroundings increases ⇒energy of system decreases⇒gas cools ∆T<0</li>

#### Pressure-Volume work reversible expansion



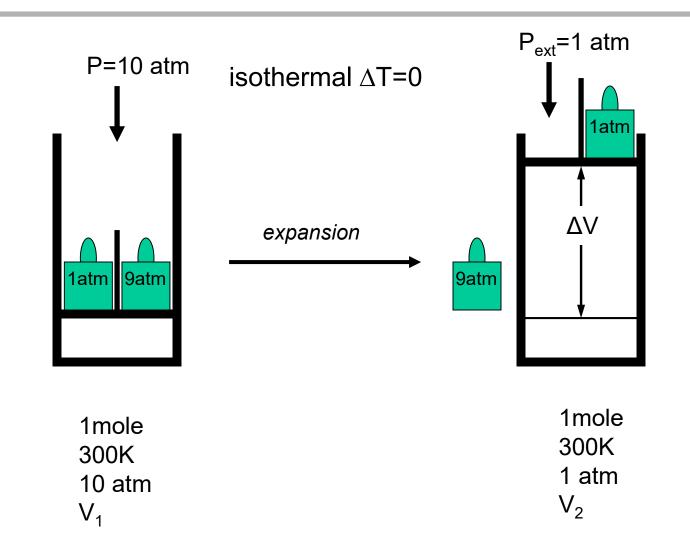
• W ON SURT rev > W ON SURT irrev (more weights raised in irrev)

• w= 
$$-\int P_{ext} dV$$

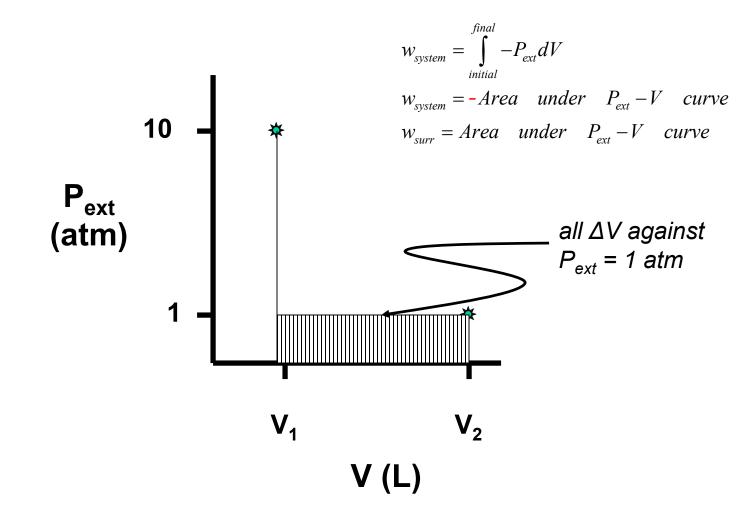
- $P_{ext} = P_{int} = nRT/V \implies w = -\int nRT/V dV$
- isothermal ⇒T=const ⇒ w=- nRT ∫ dV/V
   w = nRT ln (V<sub>final</sub>/V<sub>initial</sub>)

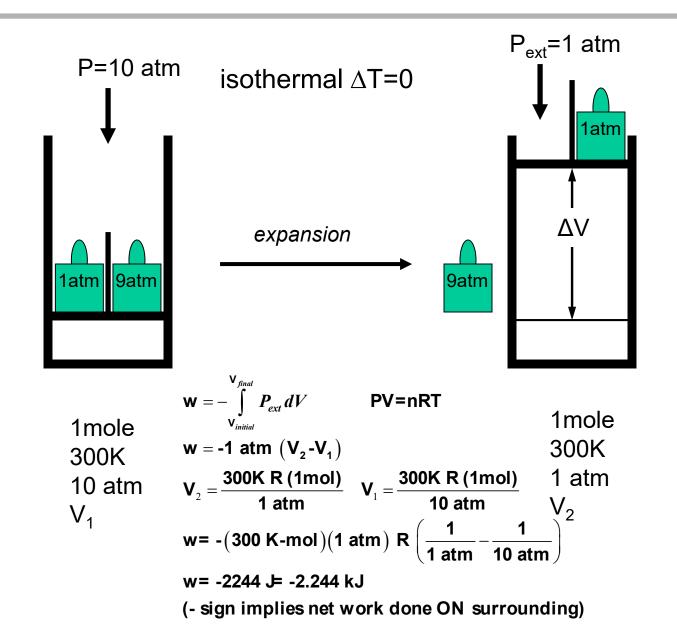
## change of energy by work done ON system $d^*w = d^*w_{PV} + d^*w_{other}$ $d^*w = -P_{ext} dV + d^*w_{other}$ $w = \int -P_{ext} dV + \int d^*w_{other}$

Types of Work	Variables, System definition	Equation for System-Based Work	SI Units
Gas expansion and compression	Pressure in the surroundings at the system– surroundings boundary ( $P_{ext}$ ), volume ( $V$ ) The gas is the system.	$-\int_{V_i}^{V_f} P_{\text{ext}} dV$	$\mathrm{Pa}\mathrm{m}^3=\mathrm{J}$
Spring stretching and compression	Force (F), distance (x) The spring is the system.	$w = \int_{x_i}^{x_f} \mathbf{F} \cdot d\mathbf{x}$	Nm=J
Bubble expansion and contraction	Surface tension ( $\gamma$ ), surface area ( $\sigma$ ) The content of the bubble is the system.	$w = -\int_{\sigma_i}^{\sigma_f} \gamma d\sigma$	$(N \ m^{-1}) \ (m^2) = J$
Current passes through conductor	Electrical potential difference $(\phi)$ , electrical charge $(Q)$ The conductor is the system.	$w = \int_0^Q \phi  dQ'$	V C = J
Done lifting a weight against gravity (weight is surroundings)	Mass (m), position (h)	$w = -\int_{h_1}^{h_2} m g  dh$	kg m² s⁻² = J

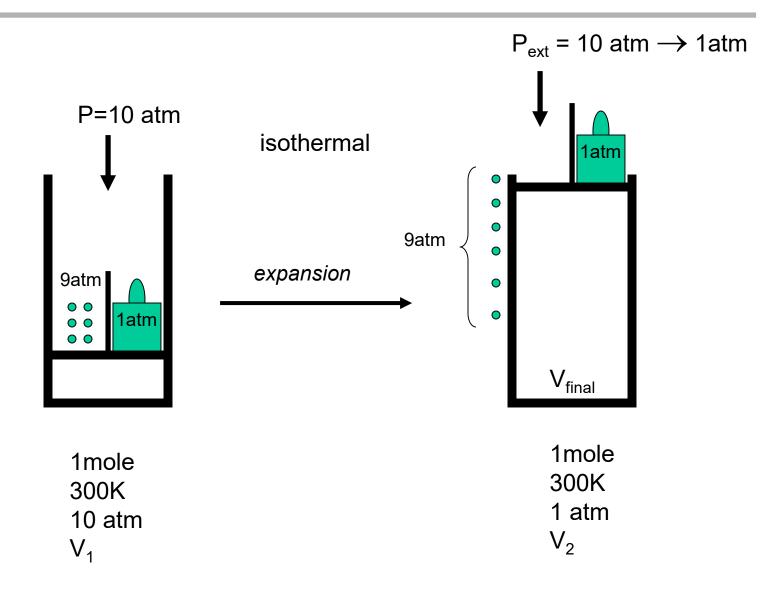


*Isothermal expansion: P*<sub>ext</sub>= const; *ideal gas; Graphical Interpretation* 

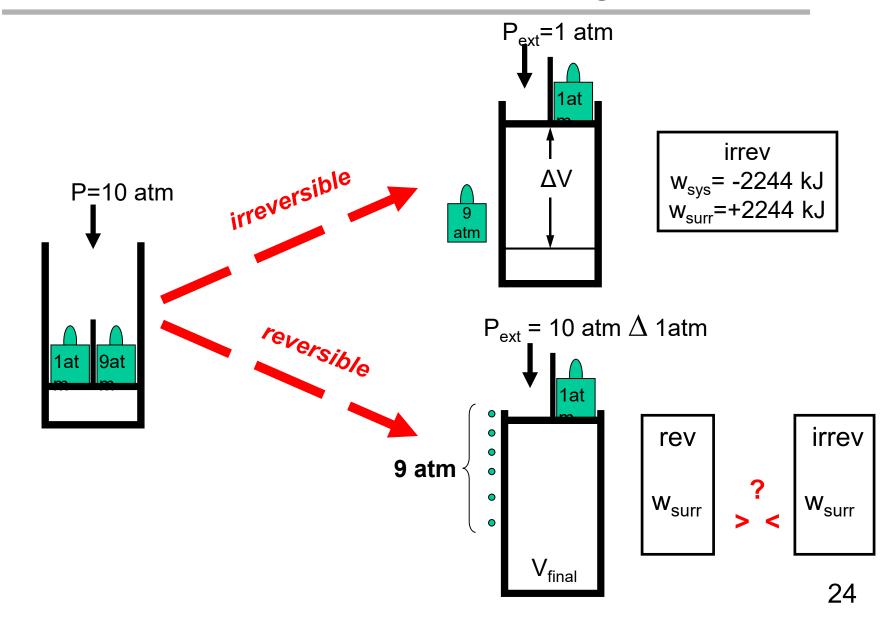


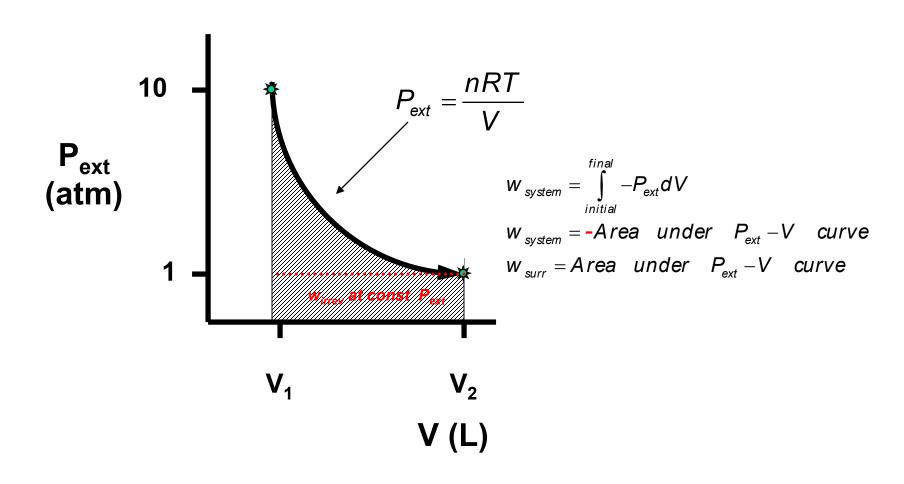


Pressure-Volume work reversible isothermal expansion; P<sub>ext</sub>=P<sub>int</sub>

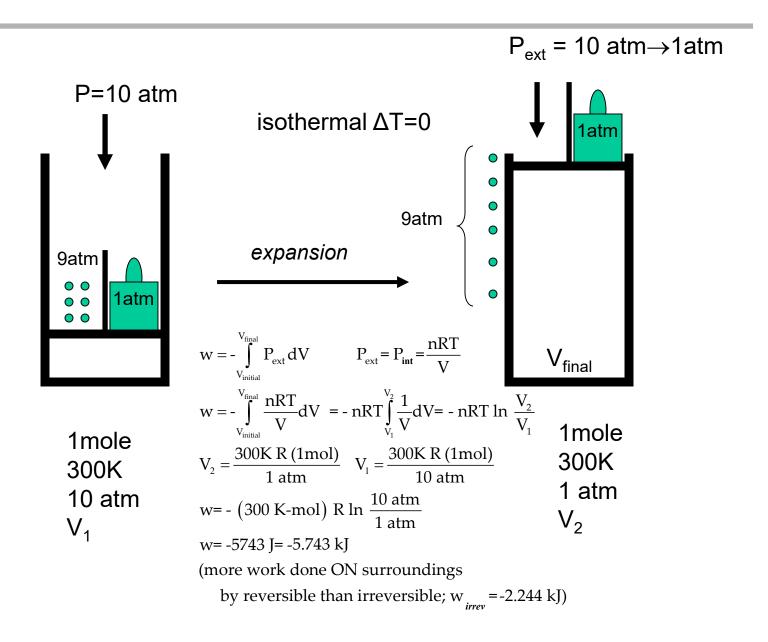


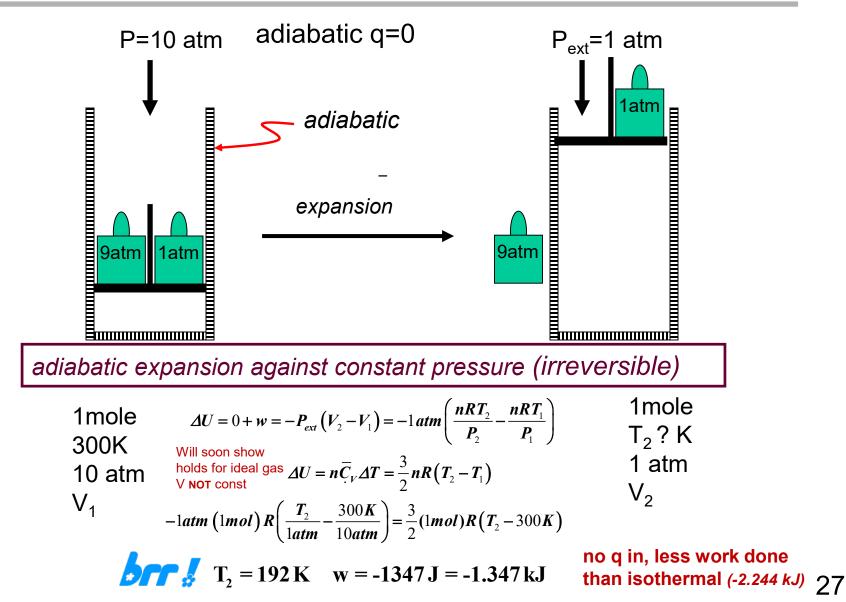
isothermal irreversible vs isothermal reversible: which does more work on surroundings ??



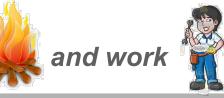


Pressure-Volume work reversible isothermal expansion; P<sub>ext</sub>=P<sub>int</sub>





molecular correlates of heat



• total energy:

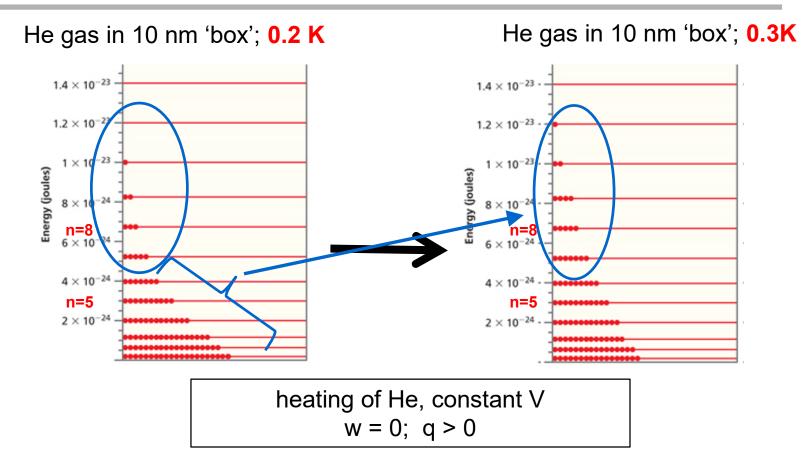
sum of [number of particles in energy level (v) × energy of that level ( $\epsilon$ )]

 $\mathsf{E}=\Sigma_n \mathsf{v}_n \mathfrak{E}_n$ 

- heat only (no work): redistributes particles among levels q>0 ⇒ more particles to higher energy levels q<0 ⇒ more particles to lower energy levels</li>
- P-V work only (adiabatic) particle in 3D cube: CHEM 163A DON'T FRET  $\varepsilon_n \approx \frac{3h^2}{8mV^{\frac{2}{3}}}n^2$  where *n* is an integer (1, 2, ...)

larger volume  $(w<0) \Rightarrow$  energy levels lower and get more closely spaced smaller volume  $(w>0) \Rightarrow$  energy levels higher and less closely spaced

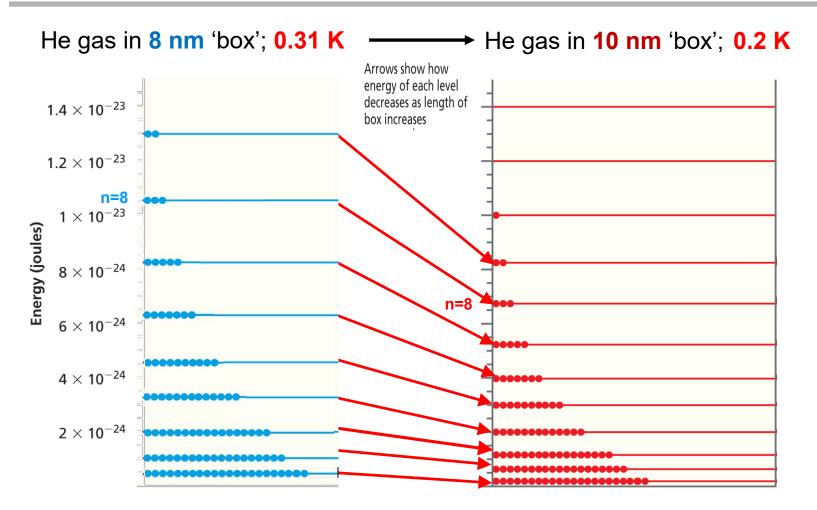
*molecular picture of heat and work: constant volume heating (E&R p 44-45)*<sub>4th</sub>



- 1. energy levels same spacing:  $\Delta V=0$ , w=0 (no change in size of box)
- 2. greater number of atoms in higher energy levels: q> 0 raises U;

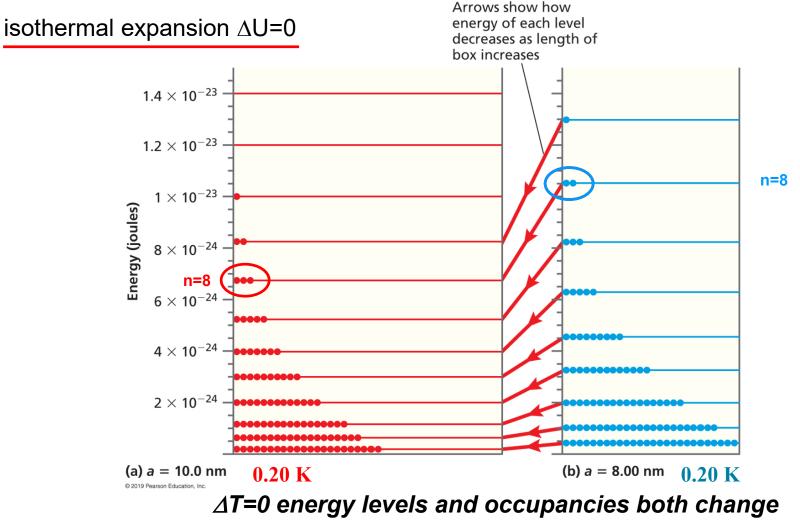
3. *∆U>0* (*∆E>0*)

#### *molecular picture of heat and work: reversible adiabatic* expansion (E&R p Fig 2-10)<sub>4th</sub>



- for reversible adiabatic expansion (no heat in) populations in levels do not change
- does total energy  $E=\Sigma n_i \varepsilon_i$  and thus temperature increase or decrease ??

Figure 2-10 Energy levels for a He atom confined to a one-dimensional box. Boxes are of length (a) 10.0 nm and (b) 8.00 nm. Circles indicate the probability that the He atom has an energy corresponding to each of the energy levels at 0.20 K. Each circle indicates a probability of 0.010. For example, the probability that the energy of the He atom corresponds to the lowest energy level in the 10.0 nm box is 0.21





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- ✓ Heat (q), Work (w) and the First Law of Thermodynamics
   ∆U≡q+w
- Example calculations of q, w, U for reversible and irreversible expansions of ideal gas (comparisons and 'take home messages')
- ✓ Molecular picture of heat and work energy transfers

End of

# Lectures 2-3