Lecture 10

Chemistry 163B Refrigerators and Generalization of Ideal Gas Carnot

(four steps to exactitude)

E&R_{4th} pp 125-129, 132-139 Raff pp. 159-164 E&R_{3rd} pp 86-91, 109-111

statements of the Second Law of Thermodynamics

- Macroscopic properties of an <u>isolated system</u> eventually assume constant values (e.g. pressure in two bulbs of gas_becomes constant; two block of metal reach same T) [Andrews. p37]
- 2. It is impossible to construct a device that operates in cycles and that converts heat into work without producing some other change in the surroundings. Kelvin's Statement [Raff p 157]; Carnot Cycle
- 3. It is impossible to have a natural process which produces no other effect than absorption of heat from a colder body and discharge of heat to a warmer body. Clausius's Statement, refrigerator
- In the neighborhood of any prescribed initial state there are states which cannot be reached by any adiabatic process

~ Caratheodory's statement [Andrews p. 58]

2

perpetual motion and the $1^{\rm st}$ and $2^{\rm nd}$ Laws of thermodynamics



cyclic machines:

1st Law $\Delta U=0$ q=- $w_{sys}=w_{surr}$



2nd Law q_{in} > w_{surr}



It is impossible to construct a device that operates in cycles and that converts heat into work without producing some other change in the surroundings. Kelvin's Statement [Raff p 157]; Carnot Cycle

3

perpetual motion of the first kind (produce work with no heat input) Escher "Waterfall"

cyclic machine (water 'flows downhill' to pillar on left; 'round and 'round) no energy input



VIOLATES 1st LAW



remember Carnot engine

· does net work on surroundings

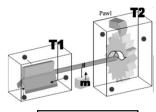
BUT

- extracts heat from surroundings at T_u
- gives off heat to surroundings at T $q_{L(III)} > 0$



perpetual motion of the second kind (produce work extracting heat from cooler source to run machine at warmer temperature)

Brownian Ratchet



get work only if T1 > T2

https://en.wikipedia.org/wiki/Brownian_ratchet.

roadmap for second law

- ✓ 1. Phenomenological statements (what is ALWAYS observed)
- ✓ 2. Ideal gas Carnot [reversible] cycle efficiency of heat \rightarrow work (Carnot cycle transfers heat only at T_U and T_L)
 - Any cyclic engine operating between T_U and T_L must have an equal or lower efficiency than Carnot OR VIOLATE one of the phenomenological statements (observations)
 - 4. Generalize Carnot to any reversible cycle (E&R fig 5.4)
 - 5. Show that for this REVERSIBLE cycle

 $q_U + q_L \neq 0$ (dq inexact differential)

but

 $\frac{q_U}{T_U} + \frac{q_L}{T_L} = 0$ (something special about $\frac{dq_{nn}}{T}$)

6. S, entropy and spontaneous changes

7

goals for lecture[s]

- · Carnot in reverse: refrigerators and heat pumps
- Show that $\epsilon_{\text{ideal gas rev Carnot}} {\ge} \epsilon_{\text{any other machine}}$ otherwise one of the phenomenological statements violated
- Not only for ideal gas but $\epsilon_{\mbox{\tiny ideal gas rev Carnot}}$ = $~\epsilon_{\mbox{\tiny any other rev Carnot}}$

•
$$dS = \frac{dq_{reversible}}{T}$$
 $\oint dS = \oint \frac{dq_{reversible}}{T} = 0$

and S is STATE FUNCTION

8

remember Carnot engine

does net work on surroundings

and

• net heat $q_{\mathrm{U(I)}}$ + $q_{\mathrm{L(III)}}$ = - w_{total}

9

Carn	Carnot engine arithmetic (for below table see handout)					
				_		
ENGINE	q	W _{sys}	Wsurr			
I. isothermal	$+nRT_{-}\ln\frac{P_{1}}{1.3}$	$-nRT_{-}\ln\frac{P_1}{}$ 1.2	$+nRT_{-} \ln \frac{P_1}{}$	heat in at TH		

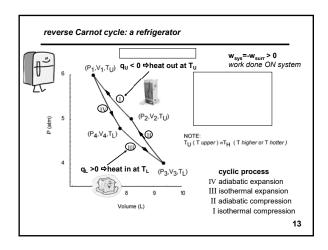
ENGINE	q	W _{sys}	Wsurr	
I. isothermal expansion	$+nRT_U \ln \frac{P_1}{P_2}$ 1.3	$-nRT_v \ln \frac{P_1}{P_2}$ 1.2	$+nRT_U \ln \frac{P_1}{P_2}$	heat in at T _H work out
II adiabatic expansion	0	$n\overline{C_{\scriptscriptstyle V}}(T_{\scriptscriptstyle L}-T_{\scriptscriptstyle U})$ 2.4	$-nC_{_{\! \!$	work out
III. isothermal compression	$nRT_L \ln \frac{P_8}{P_4} = \\ -nRT_L \ln \frac{P_1}{P_2} 3.387.3$	$\begin{split} &-nRT_L\ln\frac{P_{\rm S}}{P_{\rm L}}\\ &=nRT_L\ln\frac{P_{\rm L}}{P_{\rm L}}\\ &=nRT_L\ln\frac{P_{\rm L}}{P_{\rm L}} \end{split}$	$-nRT_L\ln\frac{P_1}{P_2}$	heat lost at T _L work in
IV. adiabatic compression	0	$n\overline{C_{_{V}}}(T_{_{U}}-T_{_{L}})$ 4.4	$-nC_{_{\! \!$	work in
net gain/cost	$q_{in} = q_i = q_U$	(Wtotal)sysr= (Wt+Wii+Wiii+Wiv)sys=	(Wtotal)surr= (W1+W11+W111+W1V)surr= - (Wtotal)sys	€=W _{surr} /q _{in}
	$+nRT_v \ln \frac{P_1}{P_2}$	$-nR(T_U-T_L)\ln\frac{P_1}{P_2}$	$nR(T_U - T_L) \ln \frac{P_1}{P_2}$	ε= (T _U -T _L)/T _U

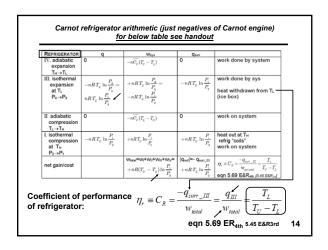
10

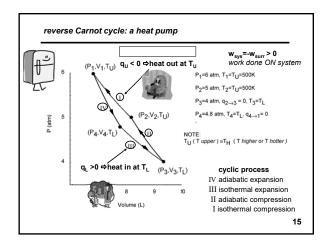
refrigerators and heat pumps: running the Carnot cycle in REVERSE

- it only makes 'sense' to talk about running a process in REVERSE for reversible processes (on a PV diagram there is no 'reverse' process for irreversible expansion against constant P_{ext})
- however the Carnot cycle is a combination of reversible processes

Figure 5.20 Application of the principle of a reverse Carnot heat engine to refrigeration and household heating. The reverse Carnot heat engine can be used to induce heat flow from a cold reservoir to a hot reservoir with the input of work. The hot reservoir in both (a) and (b) is a room. The cold reservoir can be configured as the inside of a refrigerator or outside ambient air, earth, or water for a heat pump





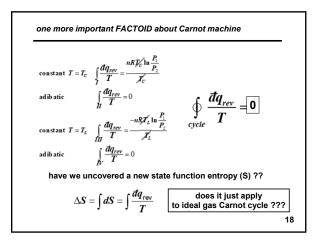


Since refrigerators and heat pumps are just Carnot machines in reverse, the relationship for ε =- w_{total}/q_1 = $(T_U - T_L)/T_U$ holds for these cycles. However only for "engines" does it represent the efficiency or "goodness of performance" (work_{total out}/heat $_{in}$).

For a refrigerator performance is (heat $_{in \text{ at } TL}/\text{work}_{total}$) $\eta_r \equiv C_R = \frac{-q_{from freezer}}{w_{total}} = \frac{q_{III}}{w_{total}} = \frac{T_L}{T_U - T_L} \qquad \text{eqn 5.69 ER}_{4th} \xrightarrow{5.45 \text{ EAR3rd}} \frac{1}{W_{total}}$ For a heat pump performance is (heat $_{out \text{ at } TU}/\text{work}_{total}$) $\eta_{hp} \equiv C_{HP} = \frac{q_{given \text{ off}}}{w_{total}} = \frac{-q_I}{w_{total}} = \frac{T_U}{T_U - T_L} \qquad (> 1)$ eqn 5.68 ER_{4th} 5.44 EAR3rd

one more important FACTOID about Carnot machine

for complete reversible Carnot cycle: $\oint dU = \Delta U = 0$ $\oint dH = \Delta H = 0$ $\oint dq_{rev} = q = \neq 0$ $\oint dw_{rev} = w = \neq 0$ BUT ALSO LET'S LOOK AT: $\oint \frac{dq_{rev}}{T}$



Generalization of Ideal Gas Carnot Cycle

Our work on the (reversible) Carnot Cycle using an ideal gas as the 'working substance' lead to the relationship

$$\epsilon = \frac{-w_{total}}{q_U} = \frac{T_U - T_L}{T_U}$$

However, the second law applies to machines with any 'working substance' and general cycles.

- 2. The following presentation shows that a (reversible) Carnot machine with 'any working substance' cannot have $\mathcal{E}_{rev\ any\ ws}$ > $\mathcal{E}_{carnot\ ideal\ gas}$.
- 3. REVERSING the directions of the ideal gas and 'any rev Carnot' (e.g. Raff, pp 160-162) shows that $\mathcal{E}_{rev\ any\ ws} = \mathcal{E}_{carnot\ ideal\ gas}$
- One can also show (E&R_{4th} Fig 5.15 Fig 5.43_{3rd} , Raff 162-164) that any Carnot machine has ∮ dq_{rev}/T =0 and that any reversible machine cycle can be expressed as a sum of Carnot cycles.

19

Carnot machine

 $\begin{aligned} & \textbf{Carnot machine: } \underline{\textbf{cyclic}}, \underline{\textbf{reversible}}, \\ & \textbf{machine} \\ & \textbf{exchanging heat with environment at only} \\ & \textbf{two temperatures } \textbf{T}_{\textbf{U}}, \\ & \textbf{T}_{\textbf{L}} \end{aligned}$

Carnot engine: 'forward' Carnot cycle

Carnot heat pump: 'reverse' Carnot cycle

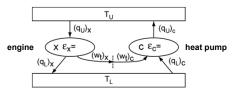
$$arepsilon = 1 - rac{T_L}{T_U} = rac{-w_{total}}{q_U}$$
 applies to both forward and

reverse Carnot cycles

20

can $\mathcal{E}_x > \mathcal{E}_c$ for any Carnot machine X vs ideal gas Carnot machine C??? (generalizing ε_{vv} -1- T_L/T_v that was derived for reversible ideal gas Carnot cycle)

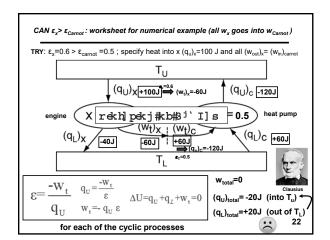
machine X: any 'working substance" (not necessarily ideal gas) exchanges heat at only two temperatures $\mathbf{T}_{\mathbf{U}}$ and $\mathbf{T}_{\mathbf{L}}$



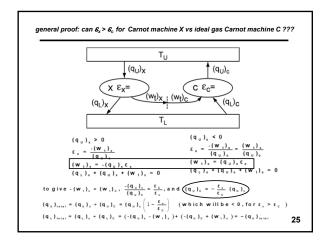
the machine X operates as a Carnot engine doing work, while the machine C operates as a reverse Carnot ideal gas engine acting as a heat pump.

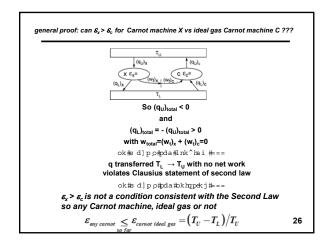
In this example the work done by X, $(w_i)_x$ is totally used by C: $(w_i)_c = -(w_i)_x$

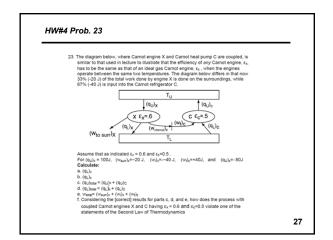
21

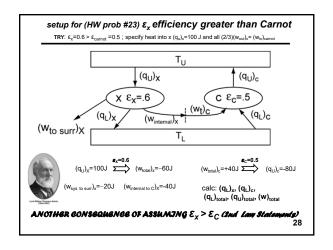


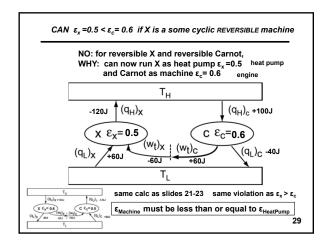
CAN $\varepsilon_x > \varepsilon_{Carnot}$: worksheet for numerical example (all w_x goes into w_{Carnot}) TRY: ε_x =0.6 > ε_{carnot} =0.5 ; specify heat into x (q_u)_x=100 J and all (w_{out})_x= (w_{in})_{carnot} $(q_U)_{c}$ -120J $(q_U)_{X + 100J}$ $c \epsilon_{c} = 0.5$ $\times \epsilon_{x} = 0.6$ $(w_t)_{x}$ $(w_t)_c$ $(q_L)_{C +60J}$ +60J -60J T_L $w_{total} = 0$ $\Delta U = q_U + q_L + w_t = 0$ $(q_U)_{total} = -20J$ (into T_U) $(q_L)_{total}$ =+20J (out of T_L) rekhlpekj#kb#8^j`I]s for each of the cyclic processes

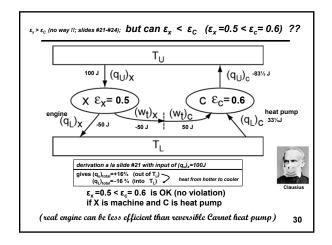












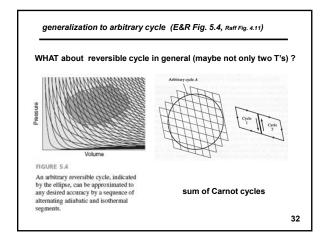
moral of the story for machines exchanging heat at T_U and T_L

- $\mathbf{E}_{\text{reversible Carnot ideal gas}} = (1 T_L / T_U)$
- ε reversible any working substance Cannot be > ε reversible Carnot ideal gas (slides 21-27)
- ξ reversible any working substance cannot be < ξ reversible Carnot ideal gas (slide 29)
- $\epsilon_{\text{reversible IN GENERAL}} = \epsilon_{\text{reversible Carnot ideal gas}} = (1-T_L/T_U)$
- $(\mathbf{E}_{\text{irreversible}})_{\text{engine}} < \mathbf{E}_{\text{maximum}} = (1 T_{\text{L}}/T_{\text{U}})$ is OK (slide 30)

$$\mathbf{\xi}_{\text{maximum}} = \mathbf{\xi}_{\text{reversible}} = (1 - T_{\text{L}}/T_{\text{U}})$$

$$general$$

31



a REALLY BIG RESULT: connecting ϵ and entropy

have shown generally for any reversible CYCLIC engine operating between $\rm T_U$ and $\rm T_L$:

$$\varepsilon = \frac{-w_{total}}{q_U} = 1 - \frac{T_L}{T_U} \qquad \text{now} \qquad \qquad \varepsilon = \frac{q_U + q_L}{q_U} = 1 + \frac{q_U}{q_U}$$

thus

$$1 + \frac{q_L}{q_U} = 1 - \frac{T_L}{T_U}$$

$$\frac{q_L}{T_L} + \frac{q_U}{T_U} = 0 \quad \text{FOR THE CYCLE}$$

(ANY REVERSIBLE cyclic process operating between T_U and T_L)₃₃

the **BOTTOM LINE**

so generally for this reversible cycle

DEFINE:

$$dS = \frac{dq_{reversible}}{T}$$

$$\oint dS = \oint \frac{dq_{reversible}}{T} = 0$$

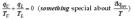
and S is STATE FUNCTION

34

roadmap for second law

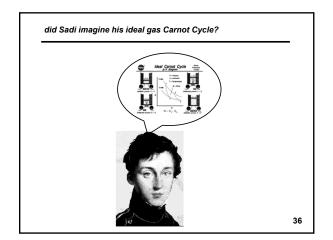
- ✓ 1. Phenomenological statements (what is ALWAYS observed)
- ✓ 2. Ideal gas Carnot [reversible] cycle efficiency of heat \rightarrow work (Carnot cycle transfers heat only at T_U and T_L)
- 3. Any cyclic engine operating between T_U and T_L must have an equal or lower efficiency than Carnot OR VIOLATE one of the phenomenological statements (observations)
- ✓ 4. Generalize Carnot to any reversible cycle (E&R fig 5.4)
- ✓ 5. Show that for this REVERSIBLE cycle $q_U + q_L \neq 0 \ \ ({\rm d}{\rm q}\ {\rm inexact}\ {\rm differential})$

 $q_U + q_L \neq 0$ (and measure differential)



✓ 6. STATE FUNCTION S, entropy and spontaneous changes re to come)





4th IASMEWSEAS International Conference on ENERGY, ENVIRONMENT, ECOSYSTEMS and SUSTAINABLE DEVELOPMENT (EEESD'08) Algarve, Portugal, June 11-13, 2008

Sadi Carnot's Ingenious Reasoning of Ideal Heat Engine Reversible Cycles

MILIVOJE M. KOSTIC Department of Mechanical Engineering Northern Illinois University DeKalb, IL 60115 U.S.A. kostic@niu.edu; http://www.kostic.niu.edu

37

1. Introduction: Sadi Carnot's Far-Reaching Treatise of Heat Engines Was Not Noticed at His Time and Even Not Fully Recognized Nowadays

Carnot laid ingenious foundations for the Second Law of Thermodynamics before the Fist Law of energy conservation was known and long before Thermodynamic concepts were established. Sadi Carnot may had not been aware of ingenuity of his reasoning, and we may have never known since he died at age 36 from cholera epidemic.

38

2. Sadi Carnot's Ingenious Reasoning of Ideal Heat Engine Reversible

MOTIVE POWER OF HEAT.

The operations which we have just described might have been performed in an inverse direction and order. There is nothing to prevent forming vapor with the calorio of the body β , and at the temperature of that body, compressing it in such a way as to make it sequire the temperature of the body A, finally condensing it by contact with this latter body, and continuing the compression to complete liquefaction.

The most importantly, Carnot introduced the reversible processes and cycles and, with ingenious reasoning, proved that maximum heat engine efficiency is achieved by any reversible cycle (thus all must have the same efficiency), i.e.:

"The motive power of heat is independent of the agents employed to realize it; its quantity is fired solely by the temperatures of the bodies between which is effected, finally, the transfer of the caloric."

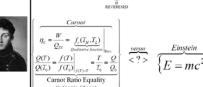
[1], i.e.:

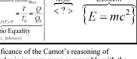
$$W = W_{sciOUT} = Q_{IN} \cdot f_c(T_H, T_L)$$

$$\eta_{Ci} = \frac{W_{sciOUT}}{Q_{IN}} \Big|_{Max} = \underbrace{f_c(T_H, T_L)}_{Qoalitative function} \Big|_{Rev.}$$
(1)

39

Carnot vs Einstein ??? (Milivoje Kostic)





 $\{-Q_H, -Q_L, -W_C\}$

Fig. 8: Significance of the Carnot's reasoning of reversible cycles is in many ways comparable with the Einstein's relativity theory in modern times. The Carnot Ratio Equality is much more important than what it appears at first. It is probably the most important equation in Thermodynamics and among the most important equations in natural sciences.

40

End of Lecture 10

(four steps to exactitude)



