#### Chemistry 163B Winter 2020 Lecture 12: ΔS<sub>UNIVERSE</sub> and Thermodynamic Tools

Lecture 12 Chemistry 163B Winter 2020

ΔS of the UNIVERSE

and

Deriving Thermodynamic Relationships

Challenged Penmanship

Notes

goals

- 1.  $\Delta S_{universe} > 0$
- 2. Maxwell-Euler Relationships
- 3.  $\Delta S_{\Phi} = \Delta H_{\Phi} / T_{\Phi}$  ( $\Phi$  is phase transtion)

2<sup>nd</sup> Law of Thermodynamics in terms of entropy

- S is a STATE FUNCTION
- $\Delta S = \int_{rev} \frac{dq_{rev}}{T} > \int_{irrev} \frac{dq_{irrev}}{T}$

 $\Delta S_{universe} \ge 0$ 

soon:

 $\Delta S_{system} + \Delta S_{surroundings} = \Delta S_{universe} \ge 0$ 

disorder increases

the entropy of the UNIVERSE increases

$$dS \ge \frac{dq}{T}$$

$$\Delta S_{system} \ge \int \frac{dq_{sys}}{T}$$
  $\Delta S_{surr} \ge \int \frac{dq_{surr}}{T}$ 

$$\Delta S_{\textit{system}} + \Delta S_{\textit{surr}} \ge \left[ \int \frac{dq_{\textit{sys}}}{T} + \int \frac{dq_{\textit{surr}}}{T} \right]$$

$$da = ? da$$

$$\Delta S_{system} + \Delta S_{surr} \ge \left[ \int \frac{dq_{sys}}{T} - \int \frac{dq_{sys}}{T} \right] =$$

$$\Delta S_{\text{system}} + \Delta S_{\text{surroundings}} = \Delta S_{??} = \Delta S_{\text{UNIVERSE}} \ge 0$$

the entropy of the UNIVERSE increases

$$dS \ge \frac{d}{ds}$$

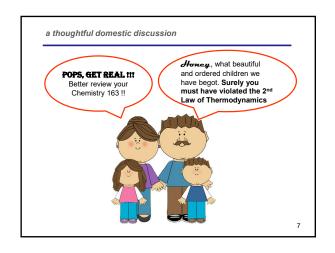
$$\Delta S_{system} \ge \int \frac{dq_{sys}}{T}$$
  $\Delta S_{surr} \ge \int \frac{dq_{surr}}{T}$ 

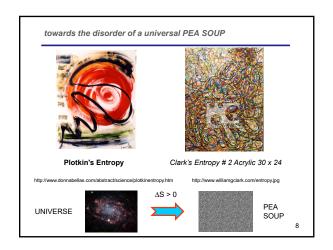
$$\begin{split} \Delta & S_{\textit{system}} + \Delta S_{\textit{surr}} \geq \Bigg[ \int \frac{d q_{\textit{sys}}}{T} + \int \frac{d q_{\textit{surr}}}{T} \Bigg] \\ d q_{\textit{surr}} & = - d q_{\textit{sys}} \end{split}$$

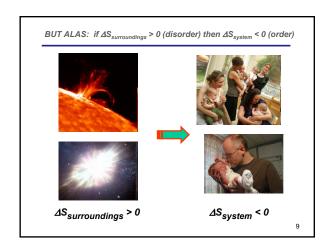
$$da = - da$$

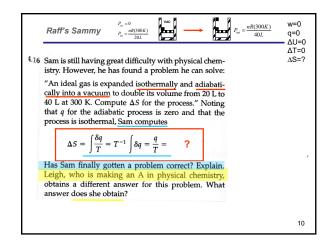
$$\Delta S_{system} + \Delta S_{surr} \ge \left[ \int \frac{d q_{sys}}{T} - \int \frac{d q_{sys}}{T} \right] = 0$$

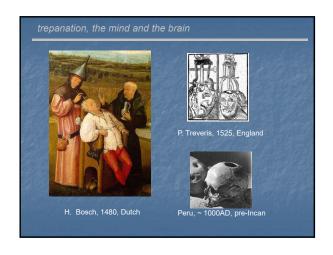
$$\Delta S_{\text{system}} + \Delta S_{\text{surroundings}} = \Delta S_{??} = \Delta S_{\text{UNIVERSE}} \ge 0$$

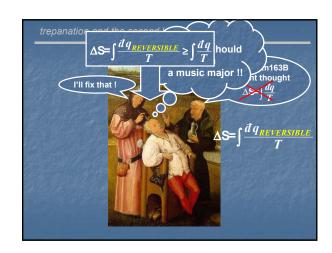












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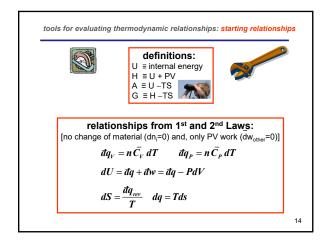
same initial and final states of system:

- $\Delta S = \Delta S_{reversible} = \Delta S_{irreversible}$
- $\Delta S = \int_{initial}^{final} \frac{dq_{reversible}}{T} \ge \int_{initial}^{final} \frac{dq}{T}$

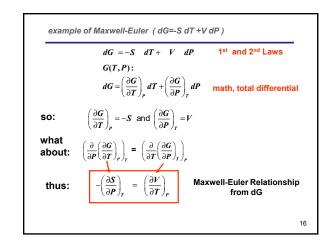
so how will reversible and irreversible processes between same initial and final states of system differ???

- $\Delta S_{\text{system}} + \Delta S_{\text{surroundings}} \equiv \Delta S_{\text{universe}} \ge 0$ ( = for reversible, > for irreversible)
- $\Delta S_{surroundings}$  will differ

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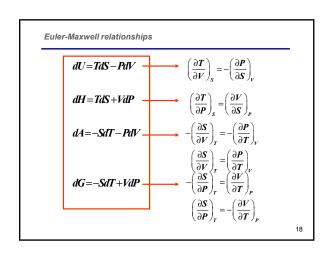
differential relationships U ≡ internal energy dU = dq + dw = dq - PdVH ≡ U + PV A ≡ U –TS  $dS = \frac{dq_{rev}}{T} \quad dq = TdS$ G≡H-TS dU = TdS - PdVU(S,V)dH = dU + PdV + VdPdH = TdS + VdPH(S,P)dA = dU - TdS - SdTdA = -SdT - PdVA(T,V)dG = dH - TdS - SdT $dG = -S\underline{dT} + V\underline{dP}$ G(T, P)15

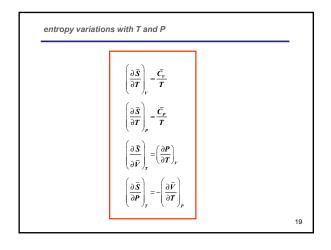


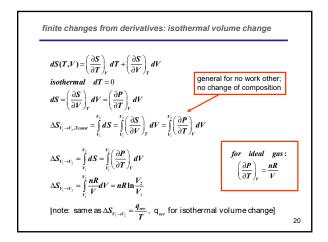
5. Suppose we know that a differential is of the form and is an exact differential:  $d \ \forall (x, y) = M \ dx + N \ dy$  (where M and N are some functions or variables)

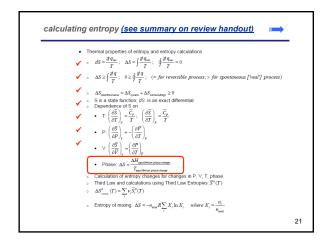
example  $(1^{th} \ \text{and} \ 2^{th} \ \text{Laws} \ \text{of}$  Thermodynamics give dG as exact differential)  $d \ G(T,P) = S \ dT + V \ dP$  (G and S are free energy and entropy)

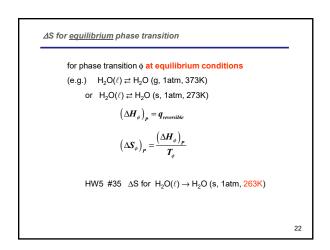
THEN WE HAVE THE FOLLOWING USEFUL RELATIONSHPS:  $\left(\frac{\partial \psi}{\partial x}\right)_g = M \ \text{and} \ \left(\frac{\partial \psi}{\partial y}\right)_g = N \qquad d\psi(x,y) = \left(\frac{\partial \psi}{\partial x}\right)_g dx + \left(\frac{\partial \psi}{\partial y}\right)_g dy$ a. or  $\left(\frac{\partial G}{\partial T}\right)_g = -S \ \text{and} \ \left(\frac{\partial G}{\partial P}\right)_g = V \qquad d\psi(x,y) = M \ dx + N \ dy$ b. and since, for well behaved functions, "mixed" second partial derivatives are equal (i.e. the order of differentiation does not matter)  $\left(\frac{\partial^2 \psi}{\partial y \partial x}\right)_{xy} = \left(\frac{\partial M}{\partial x}\right)_g = \left(\frac{\partial M}{\partial x}\right)_g = \left(\frac{\partial W}{\partial x}\right)_g = \left(\frac{\partial W}{\partial x}\right)_g + \left(\frac{\partial W}{\partial x}\right)_g = \left(\frac{\partial W}{\partial x}\right)_g = \left(\frac{\partial W}{\partial x}\right)_g + \left(\frac{\partial W}{\partial x}\right)_g = \left(\frac{\partial W}{\partial x}\right)_g + \left(\frac{\partial W}{\partial x}\right)_g = \left(\frac{\partial W}{\partial x}\right)_g + \left(\frac{\partial W}{\partial x}\right)_g + \left(\frac{\partial W}{\partial x}\right)_g = \left(\frac{\partial W}{\partial x}\right)_g + \left(\frac{\partial$ 

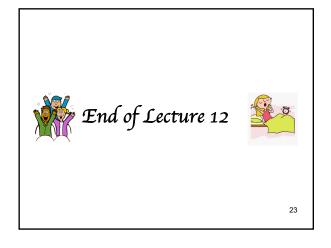












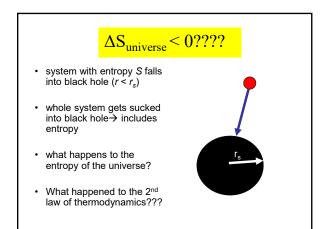


Thermodynamics and Black Holes (and other cosmology?)

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Thermodynamics of Black Holes

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#### Striking Similarity

- $2^{\text{nd}}$  Law of Thermodynamics:  $dS \ge 0$ 
  - VS.
  - Hawking Area Theorem:  $dA \ge 0$
- a coincidence? Bekenstein, 1973, says "no"
- · Hawking, Bekenstein derived entropy of black hole:

 $S_{BH} = A/4$ 

#### Generalized Second Law (GSL)

- In words:
- "The common entropy in the black-hole exterior plus the black-hole entropy never decreases."
   Bekenstein, J. Black Holes and Entropy, Phys. Rev. D., 7, 2333, (1973).
  - In math:
- $\Delta S_{BH} + \Delta S_c \ge 0$  ( $S_c$  is common entropy to the exterior)