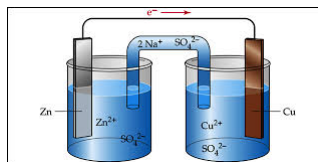


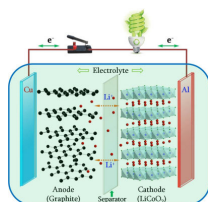
Chemistry 163B W2020
Lectures 24-25- Electrochemistry Quickie



Lectures 24-25 Winter 2020

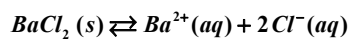
Chemistry 163B

Electrochemistry



1

activity coefficients for ions (HW8 #58)



$$K_{sp} = \frac{(a_{\text{Ba}^{2+}(aq)})(a_{\text{Cl}^-(aq)})^2}{(a_{\text{BaCl}_2(s)})}$$

$$a_{\text{BaCl}_2(s)} = 1$$

$$a_{\text{Ba}^{2+}(aq)} = \gamma_{\text{Ba}^{2+}} [\text{Ba}^{2+}]$$

$$a_{\text{Cl}^-(aq)} = \gamma_{\text{Cl}^-} [\text{Cl}^-]$$

cannot determine $\gamma_{\text{Ba}^{2+}}$ and γ_{Cl^-} independently

but only $\gamma_{\text{Ba}^{2+}} = \gamma_{\text{Cl}^-} = \gamma_{\pm}$ ($\gamma_+ = \gamma_- \equiv \gamma_{\pm}$)

$$K_{sp} = \frac{(\gamma_{\pm})^3 ([\text{Ba}^{2+}]/1M)([\text{Cl}^-]/1M)^2}{1} \quad (1)$$

$$K_{sp} = (\gamma_{\pm})^3 [\text{Ba}^{2+}][\text{Cl}^-]^2$$

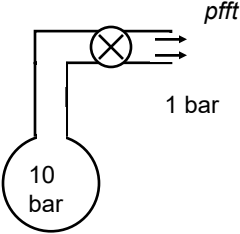
2

Chemistry 163B W2020

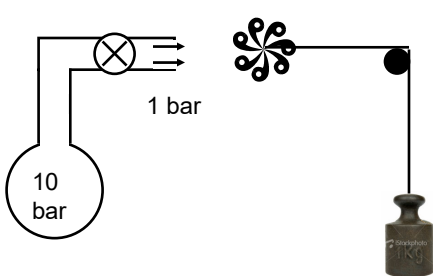
Lectures 24-25- Electrochemistry Quickie

work of expansion

$H_2(10 \text{ bar}) \rightarrow H_2(1 \text{ bar})$



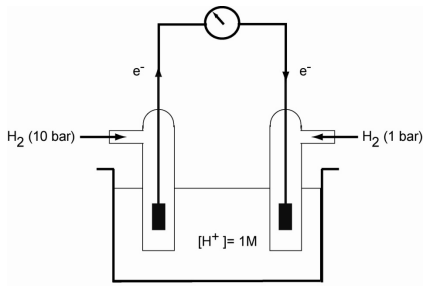
only P-V
useless?



real w_{other}
useful?

3

hydrogen pressure ['concentration'] cell (reaction I of III)



$$H_2(10 \text{ bar}) \rightarrow 2H^+ + 2e^-$$

$$2H^+ + 2e^- \rightarrow H_2(1 \text{ bar})$$

$$H_2(10 \text{ bar}) \rightarrow H_2(1 \text{ bar})$$

$$\Delta\mu = \Delta\mu^\circ + RT \ln Q_{\text{reaction}}$$

$$\Delta\mu^\circ = 0 \quad \Delta\mu^\circ \text{ is for reaction } H_2(P=1 \text{ bar}) \rightarrow H_2(P=1 \text{ bar})$$

$$\Delta\mu = \Delta\mu^\circ + RT \ln \frac{P(1 \text{ bar})}{P(10 \text{ bar})} = -5.706 \text{ kJ per mole } H_2$$

4

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

dμ and work-other (previously done for dG)

$$d\mu = d\bar{H} - Td\bar{S} - \bar{S}dT$$

$$d\mu = \underbrace{d\bar{q} - Td\bar{S}}_{\leq 0 \text{ by 2nd law}} - \bar{S}dT + \bar{V}dP + d w_{\text{other}} \quad (\text{very general})$$

≤ 0 by 2nd law

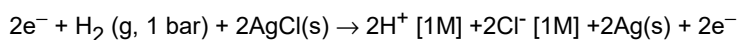
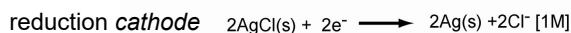
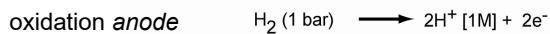
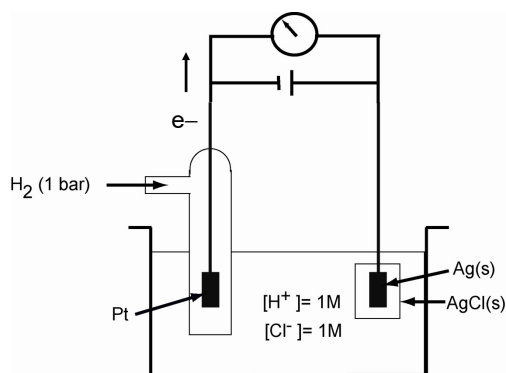
$$\Delta\mu_{T,P} \leq w_{\text{other}}$$

for a spontaneous process at constant T,P
the MAXIMUM work done ON SURROUNDINGS
is $|\Delta\mu|$ and this occurs when the process approaches

REVERSIBILITY

w_{other} (p. 292_{4th}) p. 292_{4th} $\tilde{\mu}$ vs μ 'perhaps' more rigorous If you like 5

responsible for 3 redox reactions; here's II (HW8, prob #60)



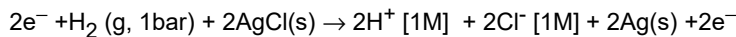
6

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

$\Delta\mu$ for the reaction

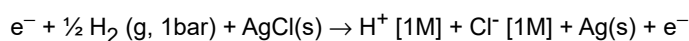
(see Appendix A, Table 4.1 for data; additional decimal places from other tables)



$$\Delta\mu_f^\circ \approx \Delta G_f^\circ \text{ (kJ)} \quad 0 \quad -109.79 \quad 0 \quad -131.23 \quad 0 \quad \text{kJ/mol}$$

$$\Delta\mu^\circ \approx \Delta G^\circ = - (0) - 2(-109.79) + 2(0) + 2(-131.23) + 2(0) = -42.88 \text{ kJ}$$

$$\Delta\mu^\circ = \text{for 2 moles } e^- \text{ transferred}$$



$$\Delta\mu^\circ \approx \Delta G^\circ = -21.44 \text{ kJ per } \frac{1}{2} \text{ mole } H_2$$

$$\Delta\mu^\circ = \text{for 1 mole } e^- \text{ transferred}$$

7

and FINALLY w_{other} !!! (p. 32_{4th})

Table 2.1 Types of Work

Types of Work	Variables, System definition	Equation for System-Based Work	SI Units
Gas expansion and compression	Pressure in the surroundings at the system-surroundings boundary (P_{ext}), volume (V) The gas is the system.	$-\int_{V_i}^{V_f} P_{\text{ext}} dV$	$\text{Pa m}^3 = \text{J}$
Spring stretching and compression	Force (\mathbf{F}), distance (\mathbf{x}) The spring is the system.	$w = \int_{x_i}^{x_f} \mathbf{F} \cdot d\mathbf{x}$	$\text{N m} = \text{J}$
Bubble expansion and contraction	Surface tension (γ), surface area (σ) The content of the bubble is the system.	$w = -\int_{\sigma_i}^{\sigma_f} \gamma d\sigma$	$(\text{N m}^{-1})(\text{m}^2) = \text{J}$
Current passes through conductor	Electrical potential difference (ϕ), electrical charge (Q) The conductor is the system.	$w = \int_0^Q \phi dQ'$	$\text{V C} = \text{J}$

8

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

BUT

w_{other} (p. 292_{4th})

$$d w_{\text{electrical}} = \Phi dQ$$

↑ electric potential
↑ charge transfer

$$dQ = -\mathcal{F}dn$$

↑ from negative charge on e
← moles of e's transferred

\mathcal{F} is Faraday constant
 96,458 coulomb (mole e)⁻¹

$d w_{\text{electrical}} = -\Phi \mathcal{F}dn$
 $w_{\text{electrical}} = -n\mathcal{F} \Phi$ (n electrons transferred)
 $(w = -n\mathcal{F}\mathcal{E})$ \mathcal{E} = electromotive force = Φ_{rev}
 E&R_{4th} p260 $z \equiv -n$

UNITS: [w] = [Q] [Φ]
joule = coulomb × volt

9

sign of Φ and spontaneity

$$\Delta\mu_{T,P} \leq w_{\text{other}}$$

$$\Delta\mu_{T,P} < -n\mathcal{F} \Phi_{\text{cell}}^{\text{irrev}} \quad \Phi_{\text{cell}}^{\text{irrev}} \text{ for irreversible}$$

$$\Delta\mu_{T,P} = -n\mathcal{F} \Phi_{\text{cell}} \quad \Phi_{\text{cell}} = \mathcal{E}_{\text{mf}} \text{ for reversible}$$

$$\Delta\mu_{T,P} < 0 \text{ spontaneous} \Rightarrow \Phi > 0 \text{ spontaneous}$$

$\Delta\mu_{T,P} < 0 \text{ spontaneous} \Rightarrow \Phi > 0 \text{ spontaneous}$
 when an external 'reverse potential' is applied so no electrons flow, the value will be that for reversible
 $-n\mathcal{F} \mathcal{E}_{\text{mf,rev}} = \Delta\mu$ even if the reactants and products are not at equilibrium conditions, in the absence of reverse potential,

10

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

Φ vs concentration

$$\Delta\mu = \Delta\mu^\circ + RT \ln Q_{\text{reaction}} = -n\mathcal{F}\Phi$$

$$\Phi = \underbrace{-\frac{\Delta\mu^\circ}{n\mathcal{F}}}_{\Phi^\circ} - \frac{RT}{n\mathcal{F}} \ln Q_{\text{reaction}}$$

$$\Phi = \Phi^\circ - \frac{RT}{n\mathcal{F}} \ln Q_{\text{reaction}}$$

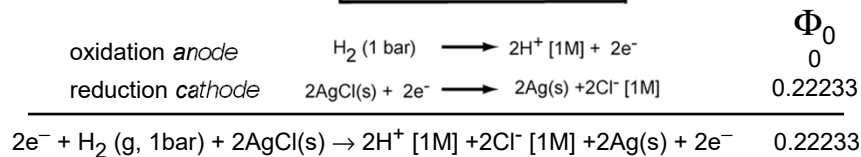
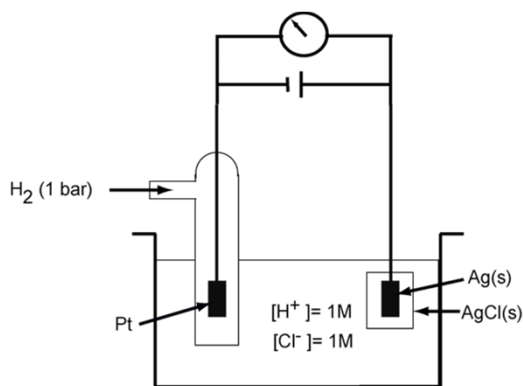
$T = 298\text{K}$

$$\Phi = \Phi^\circ - \left[\frac{0.02569}{\bar{n}} \ln Q_{\text{reaction}} \right] \text{V}$$

n = moles electrons transferred
 $[n]$ = mol
 $\bar{n} = n \times \text{mol}^{-1}$
 $[\bar{n}]$ = *unitless*

11

responsible for 3 redox reactions; here's II (HW8, prob #60)

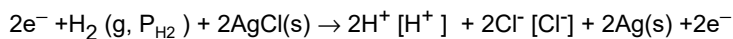


12

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

example incorporating activities



$$\Phi = \Phi^\circ - \frac{0.02569}{\bar{n}} \ln \left[\frac{a_{H^+}^2 a_{Cl^-}^2 a_{Ag(s)}^2}{a_{H_2} a_{AgCl(s)}^2} \right]$$

$$a_{AgCl} = a_{Ag} = 1$$

$$a_{H^+} = \gamma_{H^+} [H^+] \quad a_{Cl^-} = \gamma_{Cl^-} [Cl^-]$$

can't independently measure γ_{H^+} and γ_{Cl^-}

$$\gamma_{H^+} = \gamma_{Cl^-} = \gamma_{\pm}$$

$$\Phi = \Phi^\circ - \frac{0.02569}{\bar{n}} \ln \left[\frac{\gamma_{\pm}^4 [H^+]^2 [Cl^-]^2}{\gamma_{H_2} P_{H_2}} \right]$$

13

example incorporating activities

$$\Phi = \Phi^\circ - \frac{0.02569}{\bar{n}} \ln \left[\frac{\gamma_{\pm}^4 [H^+]^2 [Cl^-]^2}{\gamma_{H_2} P_{H_2}} \right]$$

↙
↙
n

0.22233 V
2 e's

$$\Phi = 0.22233 - \frac{0.02569}{2} \ln \left[\frac{\gamma_{\pm}^4 [H^+]^2 [Cl^-]^2}{\gamma_{H_2} (P_{H_2(g)})} \right]$$

unitless; have dropped
 standard state concs
 and pressure from
 denominators

- Calculate γ 's from observed Φ (HW#8, prob 60)

14

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

calculate $\Delta\mu$ from Φ

$\Delta\mu^\circ$ from Φ° ($\gamma_s=1$)

$$\Phi = 0.22233 - \frac{0.02569}{2} \ln[1] = 0.22233 = \Phi^\circ$$

$$\Delta\mu^\circ = -n\mathcal{F}\Phi^\circ$$

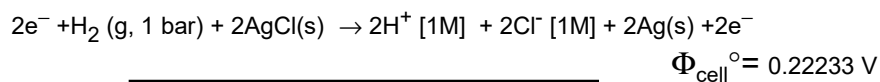
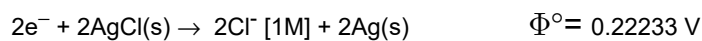
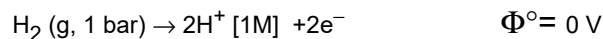
$$\Delta\mu^\circ = -2 \text{ mol} (96,485 \text{ C mol}^{-1})(0.22233 \text{ V})$$

$$\Delta\mu^\circ = -4.290 \times 10^4 \text{ CV} = -42.90 \text{ kJ}$$

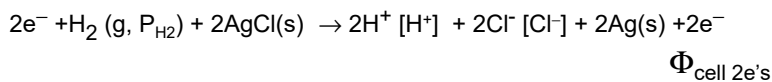
$\Delta\mu^\circ = -42.88 \text{ kJ for 2 moles } e^- \text{ transferred [from } \Delta\mu_f^\circ \text{ earlier]}$

15

intensive Φ vs extensive $\Delta\mu$ $\Phi = -(\Delta\mu/n\mathcal{F})$



$\Delta\mu^\circ = -42.88 \text{ kJ for 2 moles } e^- \text{ transferred}$



$$\Phi_{\text{cell } 2e's} = \Phi_{\text{cell}}^\circ - \frac{0.02569}{2} \ln \left[\frac{a_{\text{H}^+}^2 a_{\text{Cl}^-}^2 a_{\text{Ag}(\text{s})}^2}{a_{\text{H}_2} a_{\text{AgCl}(\text{s})}^2} \right]$$

16

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

intensive Φ vs extensive $\Delta\mu$ $\Phi = -(\Delta\mu/n\mathcal{F})$

$\frac{1}{2}\text{H}_2(\text{g}, 1 \text{ bar}) \rightarrow \text{H}^+ [1\text{M}] + \text{e}^-$

$\text{e}^- + \text{AgCl}(\text{s}) \rightarrow \text{Cl}^- [1\text{M}] + \text{Ag}(\text{s})$

$\text{e}^- + \frac{1}{2}\text{H}_2(\text{g}, 1 \text{ bar}) + \text{AgCl}(\text{s}) \rightarrow \text{H}^+ [1\text{M}] + \text{Cl}^- [1\text{M}] + \text{Ag}(\text{s}) + \text{e}^-$

$\Delta\mu^\circ = -n\mathcal{F}\Phi^\circ$

$= -(\mathbf{1\text{mol e}^-})(96485 \text{ C mol}^{-1})(0.22233 \text{ V})$

$= 2.145 \times 10^4 \text{ C V} = \mathbf{21.45 \text{ kJ}}$

$\Delta\mu^\circ = -21.44 \text{ kJ for 1 moles e}^- \text{ transferred}$

$\text{e}^- + \frac{1}{2}\text{H}_2(\text{g}, P_{\text{H}_2}) + \text{AgCl}(\text{s}) \rightarrow \text{H}^+ [\text{H}^+] + \text{Cl}^- [\text{Cl}^-] + \text{Ag}(\text{s}) + \text{e}^-$

$\Phi^\circ = 0 \text{ V}$

$\Phi^\circ = 0.22233 \text{ V}$

$\Phi_{\text{cell}}^\circ = 0.22233 \text{ V}$

↑
 Φ° intensive
same as for 2 mole e's
 Φ is oomph per electron

$\Phi_{\text{cell } 1\text{e}}$

17

$$\Phi_{\text{cell } 1\text{e}} = \Phi_{\text{cell}}^\circ - \frac{0.02569}{1} \ln \left[\frac{a_{\text{H}^+}^1 a_{\text{Cl}^-}^1 a_{\text{Ag}(\text{s})}^1}{a_{\text{H}_2}^{1/2} a_{\text{AgCl}(\text{s})}^1} \right]$$

intensive Φ vs extensive $\Delta\mu$ $\Phi = -(\Delta\mu/n\mathcal{F})$

$\Delta\mu_{2\text{e}} = 2\Delta\mu_{1\text{e}}$
two times greater

$\Delta\mu = -42.88 \text{ kJ for 2 moles e}^- \text{ transferred}$

$$\Phi_{\text{cell } 2\text{e}^-} = \Phi_{\text{cell}}^\circ - \frac{0.02569}{2} \ln \left[\frac{a_{\text{H}^+}^2 a_{\text{Cl}^-}^2 a_{\text{Ag}(\text{s})}^2}{a_{\text{H}_2} a_{\text{AgCl}(\text{s})}^2} \right]$$

$\Phi_{\text{cell } 2\text{e}} = \Phi_{\text{cell } 1\text{e}}$
same

$\Delta\mu = -21.44 \text{ kJ for 1 moles e}^- \text{ transferred}$

$$\Phi_{\text{cell } 1\text{e}} = \Phi_{\text{cell}}^\circ - \frac{0.02569}{1} \ln \left[\frac{a_{\text{H}^+}^1 a_{\text{Cl}^-}^1 a_{\text{Ag}(\text{s})}^1}{a_{\text{H}_2}^{1/2} a_{\text{AgCl}(\text{s})}^1} \right]$$

$\Delta\mu$ extensive: depends on stoichiometry

$\rightarrow \Delta\mu = -n\mathcal{F}\Phi$

Φ intensive: independent of 'how reaction is written' oomph PER electron

18

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

biological example: cytochrome C iron containing enzyme (reaction III)

CytC=cytochrome C
standard state pH=7, $[H^+]=10^{-7}$

standard REDUCTION potentials		$\Phi^{\circ'}_{red}(V)$ pH7
	$2e^- + 2CytC(Fe^{3+}) \rightarrow 2CytC(Fe^{2+})$	0.25
	$2e^- + \frac{1}{2}O_2(g) + 2H^+(aq) \rightarrow H_2O(l)$	0.816
reaction: the oxidation of CytC(Fe^{2+})		$\Phi^{\circ'}(V)$
oxidation	$2CytC(Fe^{2+}) \rightarrow 2CytC(Fe^{3+}) + 2e^-$	- 0.25
reduction	$2e^- + \frac{1}{2}O_2(g) + 2H^+(aq) \rightarrow H_2O(l)$	0.816
$\frac{1}{2}O_2(g) + 2H^+(aq) + 2CytC(Fe^{2+}) \rightarrow 2CytC(Fe^{3+}) + H_2O(l)$? = $\Phi^{\circ'}_{cell}$
	\uparrow standard state $[H^+]=10^{-7}$	19


biological example (redox equation III)

$\frac{1}{2}O_2(g) + 2H^+(aq) + 2CytC(Fe^{2+}) \rightarrow 2CytC(Fe^{3+}) + H_2O(l)$

$$\Phi_{cell} = \Phi_{cell}^{\circ'} - \frac{RT}{n\mathcal{F}} \ln[Q] = \Phi_{cell}^{\circ'} - \frac{RT}{n\mathcal{F}} \ln \left[\frac{\dots\dots}{\dots\dots \left(\frac{\gamma_{\pm}[H^+]}{10^{-7}M} \right)^2 \left(\frac{\gamma_{O_2} P_{O_2}}{1bar} \right)^{1/2} \dots} \right]$$

\uparrow
 standard state '

what's $\Phi^{\circ'}$?
what's Q ?
what's n ?



20

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

Φ and thermodynamic derivatives, etc. (HW8, prob #59)

$$\Delta\mu = -n\mathcal{F}\Phi$$

$$\Phi = -\frac{\Delta\mu}{n\mathcal{F}}$$

$$\Delta\mu^\circ = -RT \ln K_{eq} \Rightarrow \Phi^\circ = \frac{RT}{n\mathcal{F}} \ln K_{eq}$$

$$\left(\frac{\partial\Delta\mu}{\partial T}\right)_p = -\Delta\bar{S} \Rightarrow \left(\frac{\partial\Phi}{\partial T}\right)_p = \frac{\Delta\bar{S}}{n\mathcal{F}}$$

$$\left(\frac{\partial\frac{\Delta\mu}{T}}{\partial T}\right)_p = -\frac{\Delta\bar{H}}{T^2} \Rightarrow \left(\frac{\partial\frac{\Phi}{T}}{\partial T}\right)_p = \frac{\Delta\bar{H}}{n\mathcal{F}T^2}$$

21

ΔC_p from Φ

$$\left(\frac{\partial\Delta\mu}{\partial T}\right)_p = -\Delta\bar{S} \Rightarrow \left(\frac{\partial\Phi}{\partial T}\right)_p = \frac{\Delta\bar{S}}{n\mathcal{F}}$$

$$\Delta\mu = \Delta\bar{H} - T\Delta\bar{S}$$

$$\Delta\bar{H} = \Delta\mu + T\Delta\bar{S} = -n\mathcal{F}\Phi + T n\mathcal{F} \left(\frac{\partial\Phi}{\partial T}\right)_p$$

$$\left(\frac{\partial\Delta\bar{H}}{\partial T}\right)_p = \Delta C_p = -n\mathcal{F} \left(\frac{\partial\Phi}{\partial T}\right)_p + n\mathcal{F} \left(\frac{\partial\Phi}{\partial T}\right)_p + n\mathcal{F}T \left(\frac{\partial^2\Phi}{\partial T^2}\right)_p$$

$$\Delta C_p = n\mathcal{F}T \left(\frac{\partial^2\Phi}{\partial T^2}\right)_p$$

22

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

relationships on final

Electrochemistry:

$$\bullet \Delta\mu_{\text{reaction}} = -n\mathcal{F}\Phi_{\text{cell}}$$

$$\Phi = \Phi^{\circ} - \frac{RT}{n\mathcal{F}} \ln Q$$

$$\Phi = \Phi^{\circ} - \frac{0.02569}{\bar{n}} \ln Q \quad \text{at } T = 298K$$

23

batteries and fuel cells

battery -

- nicely package electrochemical cell
- closed system
- runs irreversibly ($\Phi < \mathcal{E}$)
- may be recharged (storage battery)

fuel cell-

- electrochemical cell
- open system (reactants continuously flow in)

24

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

efficiency of $w_{\text{electrical}}$ vs w_{P-V}

compare:

$w_{\text{electrical}}$ (on surr) from lead storage battery
 $\Delta G = -377 \text{ kJ mol}^{-1}$, $\Delta H = -228 \text{ kJ mol}^{-1}$

with

w_{P-V} (on surr) of heat engine using $q_{\text{upper}} = -\Delta H_{\text{storage battery}}$

heat engine: $T_U = 600\text{K}$, $T_L = 300\text{K}$

$\epsilon = (600 - 300) / 600 = 0.5$

$w_{P-V} = (0.5) * 228 \text{ kJ mol}^{-1} = 114 \text{ kJ mol}^{-1}$

battery: $\Delta G = -377 \text{ kJ mol}^{-1}$, $T = 300\text{K}$

$w_{\text{electrical}} = -\Delta G = 377 \text{ kJ mol}^{-1}$

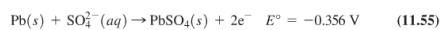
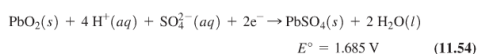
the winner:

$$\frac{w_{\text{electrical}}}{w_{P-V}} = \frac{377}{114} = 3.31$$

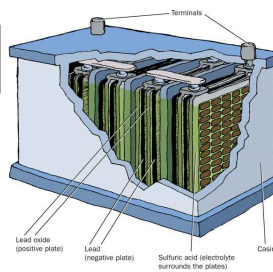
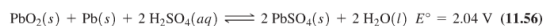
25

types of batteries

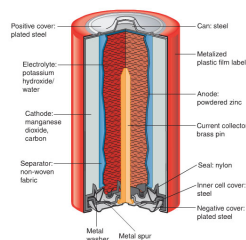
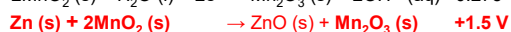
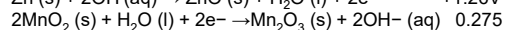
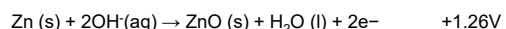
Lead storage
Pb(s) oxidized to Pb^{2+} PbO_2 reduced to Pb^{2+}



respectively, and the overall reaction is



Alkaline storage (no liquids)
Zn(s) oxidized to Zn^{2+} MnO_2 reduced to Mn_2O_3



26

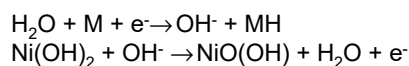
Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

types of batteries

NiMH- Nickel Metal Hydride
 M='intermetallic compound', e.g. $M=AB_5$,
 A is a rare earth mixture of lanthanum, cerium, neodymium, praseodymium
 B is nickel, cobalt, manganese, and/or aluminum

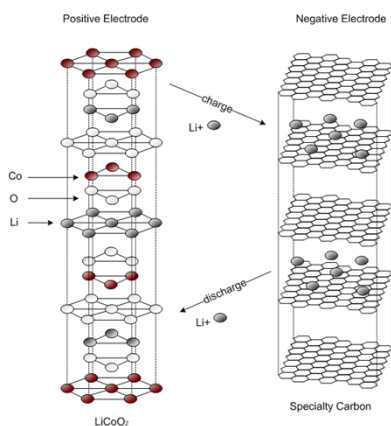
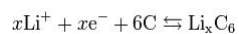
Ni^{2+} oxidized to Ni^{3+} H^+ reduced to H^- , "M" oxidized



High power Ni-MH battery of Toyota NHW20 Prius

27

Li-ion batteries



Li-ion batteries can pack more energy into smaller and lighter weight units than other types of batteries. Those attributes have spurred enormous growth in their use for cell phones, laptop computers, and other portable electronic devices.



A downside of Li-ion cells, however, is that they contain a flammable electrolyte solution consisting of lithium salts in organic solvents such as ethylene carbonate and ethyl methyl carbonate. This is not the case for other commercial battery types.

28

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

battery property comparison

Zinc	1.5V	Non-rechargeable —first the forerunner and later an inexpensive alternative to Alkaline batteries. However, reductions in the price of Alkalines have made both Zinc-Carbon and Zinc-Chloride batteries all but obsolete.
-------------	-------------	--

http://batteryuniversity.com/learn/article/whats_the_best_battery

29

battery property comparison

Zinc	1.5V	Non-rechargeable —first the forerunner and later an inexpensive alternative to Alkaline batteries. However, reductions in the price of Alkalines have made both Zinc-Carbon and Zinc-Chloride batteries all but obsolete.
Alkaline	1.5V	Rechargeable — Alkaline rechargeable batteries are lower capacity (don't hold a charge as long) than the more popular NiMH rechargeables. The advantage of the rechargeable Alkaline over the NiMH or the NiCAD is that it loses its charge gradually,
Nickel-Metal Hydride (NiMH)	1.25V	Rechargeable - Lightweight and rechargeable, the NiMH has a higher capacity than the NiCAD plus you can throw it away since it doesn't contain toxic metals and it isn't classed as a hazardous waste item.
Lithium ion	3.6V	Rechargeable — For a given voltage, a lithium ion battery is smaller in size and lighter in weight than a nickel cadmium (NiCd) or nickel metal hydride (NiMH) battery. In addition, lithium ion has virtually no self-discharge. This allows a lithium ion battery to be stored for months without losing charge. The battery chemistries can be compared as follows:

http://batteryuniversity.com/learn/article/whats_the_best_battery

30

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

fuel cells

PEM- proton exchange membrane

Flow field Catalyst layer Membrane H₂O

Anode H₂ H⁺ Cathode O₂ H₂O

load

Electric Current

Fuel In Air In H₂O

Excess Fuel Unused Gases Out

Anode Electrolyte Cathode

$$\text{H}_2 \rightarrow 2\text{H}^+ + 2\text{e}^- \quad 0 \text{ V}$$

$$\frac{1}{2}\text{O}_2 + 2\text{H}^+ + 2\text{e}^- \rightarrow \text{H}_2\text{O} \quad 1.23 \text{ V}$$

Fuel cells come in a variety of sizes. Individual fuel cells produce relatively small electrical potentials, about 0.7 volts. The energy efficiency of a fuel cell is generally between 40–60%.

31

End of Lecture

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

$\tilde{\mu}_i$ the electrochemical potential

$$dG = -SdT + VdP + \sum_{i,\gamma} \mu_i^{(\gamma)} dn_i^{(\gamma)} \leq \delta w_{elec}$$

$$(\Delta G)_{T,P} = \sum_{i,\gamma} \nu_i^{(\gamma)} \mu_i^{(\gamma)} + (\Delta \mu_{reaction}) \leq w_{elec}$$

VS

$$dG = -SdT + VdP + \sum_{i,\gamma} \tilde{\mu}_i^{(\gamma)} dn_i^{(\gamma)}$$

$$(\Delta G)_{T,P} = \sum_{i,\gamma} \nu_i^{(\gamma)} \tilde{\mu}_i^{(\gamma)} \leq 0$$

$$\tilde{\mu}_i^{(\gamma)} = \mu_i^{(\gamma)} + (\Phi_i^{(\gamma)})_{elec}$$

$\tilde{\mu}_i$ assigns electrical potential to each species including electrons transferred


 back more
 33

free energy of charged species in the presence of electrostatic potential

$$d\tilde{\mu}_i^{(\gamma)} = d\mu_i^{(\gamma)} + (dw_i^{(\gamma)})_{other} = -\bar{S}_i^{(\gamma)} dT + \bar{V}_i^{(\gamma)} dP + \underbrace{\phi^{(\gamma)} dQ_i^{(\gamma)}}_{\delta w_{other}}$$

$$\tilde{\mu}_i^{(\gamma)} = \mu_i^{(\gamma)} + z_i \mathcal{F} \phi^{(\gamma)}$$

Faraday
96,485 Coulombs mole⁻¹ → \mathcal{F}
integer (signed) charge → z_i
electrostatic potential in phase γ → $\phi^{(\gamma)}$
 $\mu_i^{(\alpha)} = \mu_i^{(\beta)}$

a charge in two phases (different potential ϕ ; otherwise same)

$$\tilde{\mu}_i^{(\alpha)} - \tilde{\mu}_i^{(\beta)} = z_i \mathcal{F} (\phi^{(\alpha)} - \phi^{(\beta)}) = z_i \mathcal{F} \Delta \phi$$

$\mu_i^{(\alpha)}$ is escaping tendency from phase (α), $\mu_i^{(\beta)}$ from phase β
 + charge ($z_i > 0$): ion 'escapes' to phase of lower (more negative) potential ϕ
 - charge ($z_i < 0$): ion 'escapes' to phase of higher (more positive) potential ϕ

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

$\tilde{\mu}_i$ electrochemical potential

$$\tilde{\mu}_i^{(\gamma)} = \mu_i^{(\gamma)} + z_i \mathcal{F} \phi^{(\gamma)}$$

$$\Delta G_{\text{reaction}} = \sum_{i,\gamma} \nu_i^{(\gamma)} \tilde{\mu}_i^{(\gamma)} \quad \text{where } \nu_i^{(\gamma)} \text{ are the stoichiometric coefficients}$$

note: these must now include $\nu_e^{(\gamma)} \tilde{\mu}_e^{(\gamma)}$ for electrons involved in stoichiometry

assume the phases are metal electrodes and solutions with ions.

for ions in a given solution phase α

$$\sum_{i=\text{ions}} \nu_i^{(\alpha)} \tilde{\mu}_i^{(\alpha)} = \sum_i \nu_i^{(\alpha)} \mu_i^{(\alpha)} + \sum_i \nu_i^{(\alpha)} z_i \mathcal{F} \phi^{(\alpha)}$$

for any neutral species $z_i = 0$

$$\tilde{\mu}_i^{(\alpha)} = \mu_i^{(\alpha)}$$

$$\sum_i \nu_i^{(\alpha)} z_i \mathcal{F} \phi^{(\alpha)} = \mathcal{F} \phi^{(\alpha)} \sum_i \nu_i^{(\alpha)} z_i$$

and $\sum_{i=\text{ions}} \nu_i^{(\alpha)} z_i = 0$ for charge neutrality

thus $\sum_i \nu_i^{(\alpha)} \tilde{\mu}_i^{(\alpha)} = \sum_i \nu_i^{(\alpha)} \mu_i^{(\alpha)}$ for all reactants and products except
for electrons at metal electrodes

35

$\tilde{\mu}_i$ electrochemical potential

$$\Delta G_{\text{reaction}} = \sum_{i,\gamma} \nu_i^{(\gamma)} \tilde{\mu}_i^{(\gamma)} \quad \text{where } \nu_i^{(\gamma)} \text{ are the stoichiometric coefficients}$$

$$\text{thus: } \Delta G_{\text{reaction}} = \sum_{i,\gamma} \nu_i^{(\gamma)} \mu_i^{(\gamma)} + \nu_{e^-}^{(\text{oxidation})} z_{e^-} \mathcal{F} \phi^{(\text{oxidation electrode})} + \nu_{e^-}^{(\text{reduction})} z_{e^-} \mathcal{F} \phi^{(\text{reduction electrode})}$$

$$\nu_{e^-}^{(\text{reduction})} = +n_{\text{transferred electrons}} \quad \text{and} \quad \nu_{e^-}^{(\text{oxidation})} = -n_{\text{transferred electrons}}$$

$$\text{and } \left(\mu^{(\text{reactant electrode})} \right)_{e^-}^0 = \left(\mu^{(\text{product electrode})} \right)_{e^-}^0$$

$$\Delta G_{\text{reaction}} = \sum_{\substack{\gamma, i = \text{species} \\ \text{other than } e^-}} \nu_i^{(\gamma)} \mu_i^{(\gamma)} - n \mathcal{F} \left(\phi^{(\text{reduction electrode})} - \phi^{(\text{oxidation electrode})} \right)$$

$$\text{emf} \equiv \mathcal{E} \equiv \left(\phi^{(\text{oxidation electrode})} - \phi^{(\text{reduction electrode})} \right) \quad (\text{IUPAC convention})$$

$$\Delta G_{\text{reaction}} = \sum_{\substack{\gamma, i = \text{species} \\ \text{other than } e^-}} \nu_i^{(\gamma)} \mu_i^{(\gamma)} + n \mathcal{F} \mathcal{E}$$

36

Chemistry 163B W2020

Lectures 24-25- Electrochemistry Quickie

so it boils down to

from $\tilde{\mu}_i$

$$\Delta G_{\text{reaction}} = \sum_{\substack{\gamma, i = \text{species} \\ \text{other than } e^-}} \nu_i^{(\gamma)} \mu_i^{(\gamma)} + nF\mathcal{E} \leq 0$$

$$\Delta G_{\text{reaction 'regular'}} = \sum_{\substack{\gamma, i = \text{species} \\ \text{other than } e^-}} \nu_i^{(\gamma)} \mu_i^{(\gamma)} \leq -nF\mathcal{E}$$

VS

from μ_i
 $\Delta\mu_{\text{reaction}} \approx \Delta G_{\text{reaction}}$

$$\left(\Delta G_{\text{reaction 'regular'}} \right)_{T,P} \leq w_{\text{electrical}}$$

$$\left(\Delta G_{\text{reaction 'regular'}} \right)_{T,P} \leq -n_{\text{electrons transferred}} \mathcal{F} \mathcal{E}$$

'regular' \Rightarrow not including μ_{e^-}

RETURN TO
SANITY


37